

# Self-Organization and Self-Optimization of Traffic Flows on Freeways and in Urban Networks

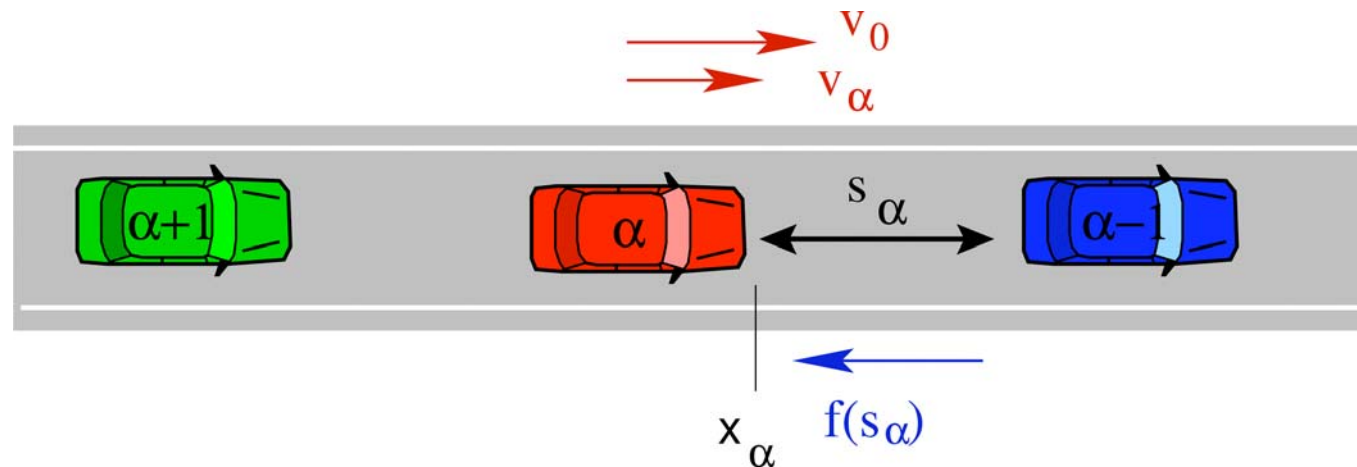
Prof. Dr. rer. nat. Dirk Helbing  
Chair of Sociology, in particular of Modeling and Simulation

[www.soms.ethz.ch](http://www.soms.ethz.ch)

with Amin Mazloumian, Stefan Lämmer, Reik Donner,  
Johannes Höfener, Jan Siegmeier, ...



# The Intelligent-Driver Model (IDM)



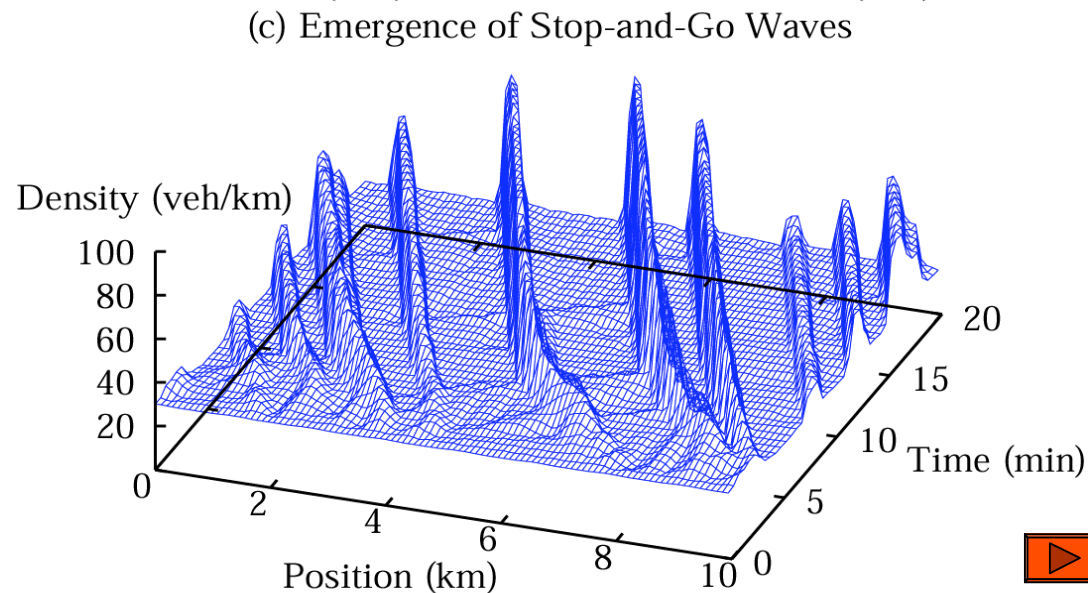
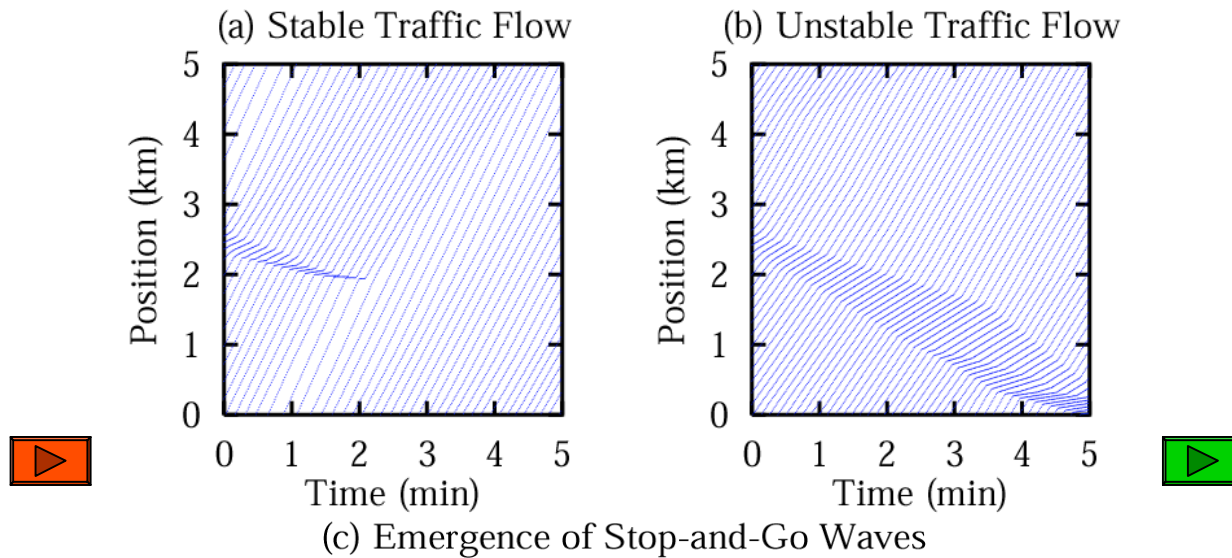
- Equations of motion:

$$\begin{aligned} \dot{x}_\alpha &= v_\alpha, \\ \dot{v}_\alpha &= a \left[ \underbrace{1 - \left(\frac{v_\alpha}{v_0}\right)^\delta}_{\text{Beschleunigung}} - \underbrace{\left(\frac{s^*(v_\alpha, \Delta v_\alpha)}{s_\alpha}\right)^2}_{\text{Bremsverzögerung}} \right] \end{aligned}$$

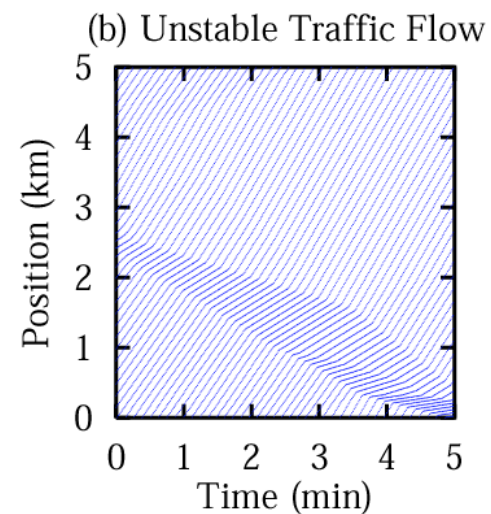
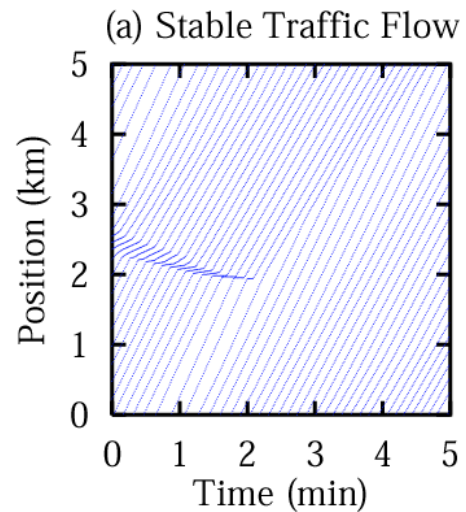
- Dynamic desired distance

$$s^*(v, \Delta v) = \underbrace{s_0}_{\text{Mindestabstand}} + \underbrace{vT}_{\text{"Sicherheits"-abstand}} + \underbrace{\frac{v\Delta v}{2\sqrt{ab}}}_{\text{dynamischer Teil}}$$

# Instability of Traffic Flow

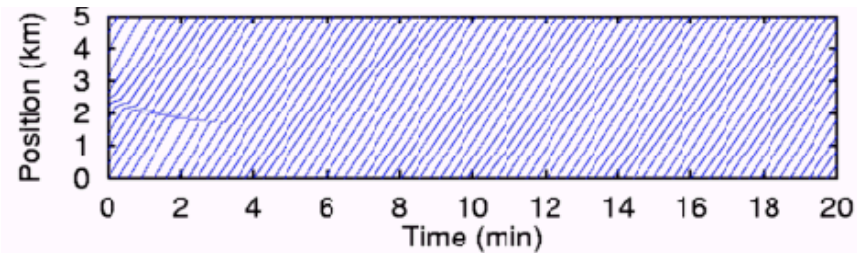


# Instability of Traffic Flow

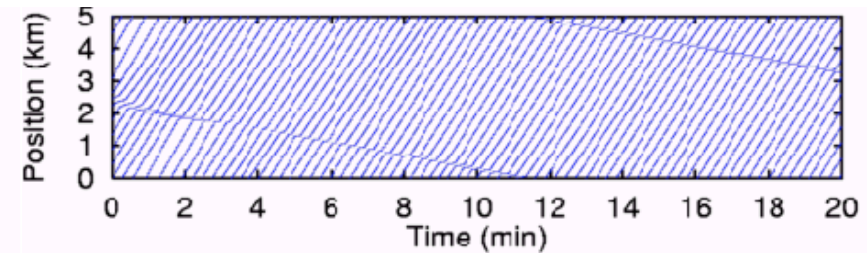


Source: Sugiyama et al.

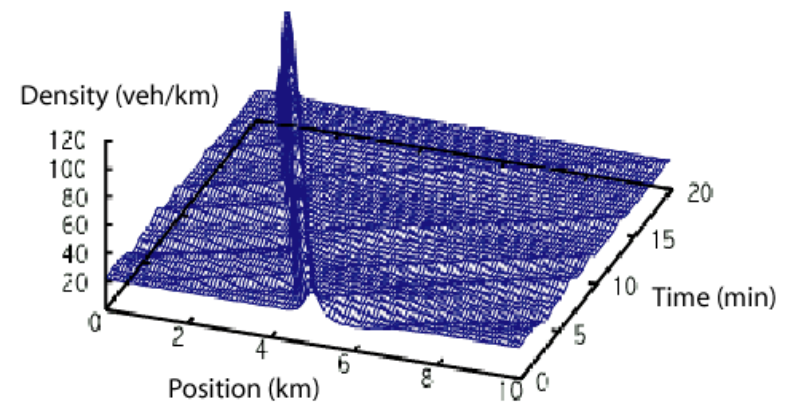
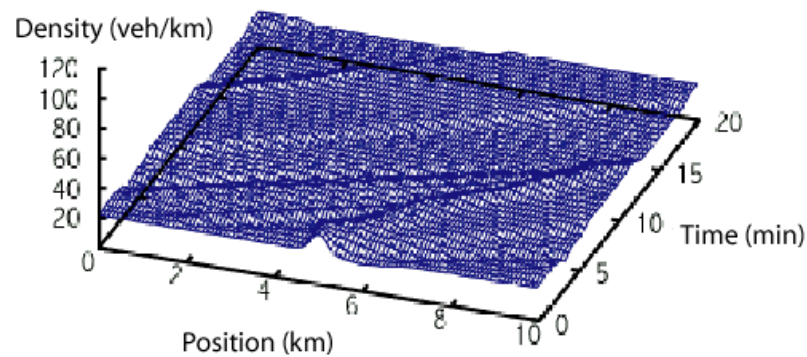
# Metastability of Traffic Flow



Decay of a Subcritical Perturbation

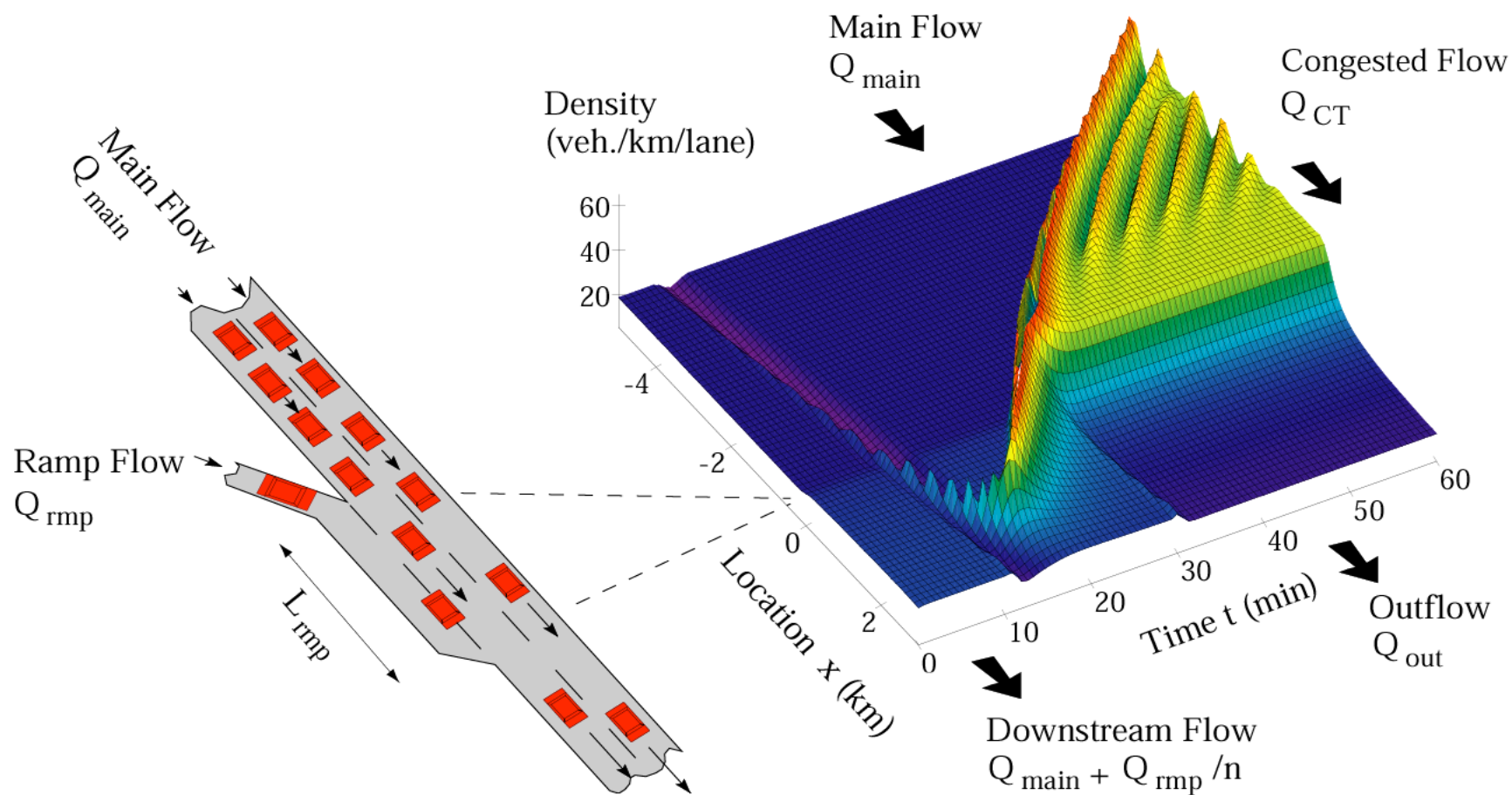


Growth of a Supercritical Perturbation

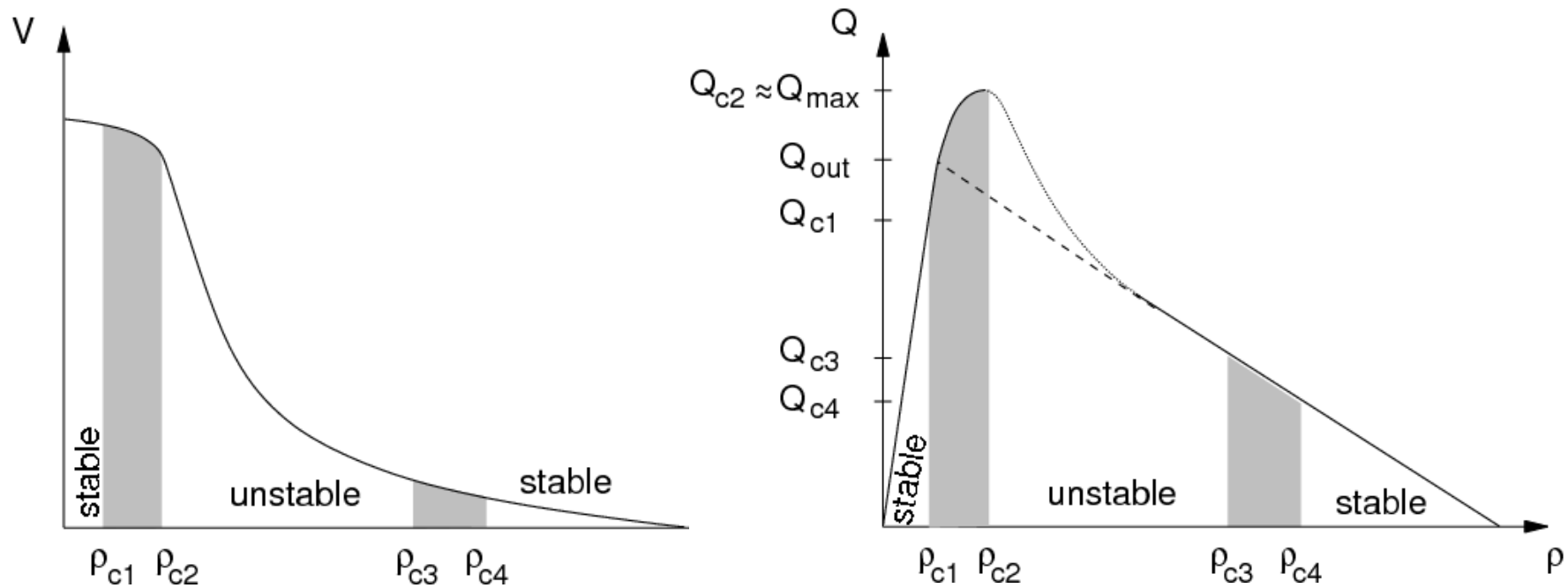


# Breakdown of Traffic due to a Supercritical Reduction of Traffic Flow

## Negative Perturbation Triggering Oscillating Congested Traffic



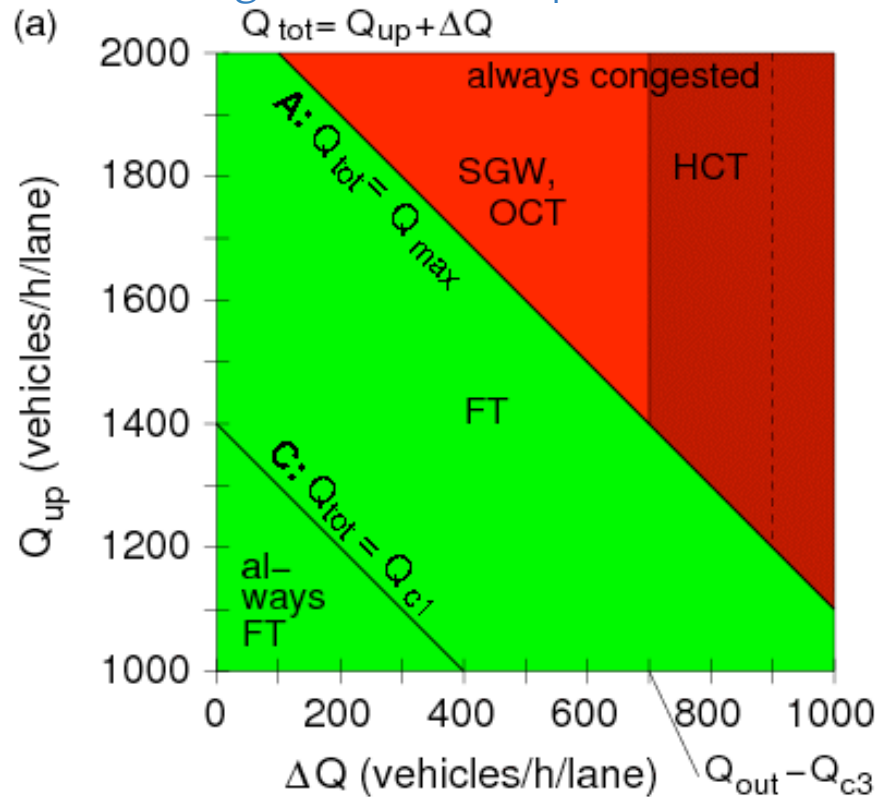
## Assumed Instability Diagram



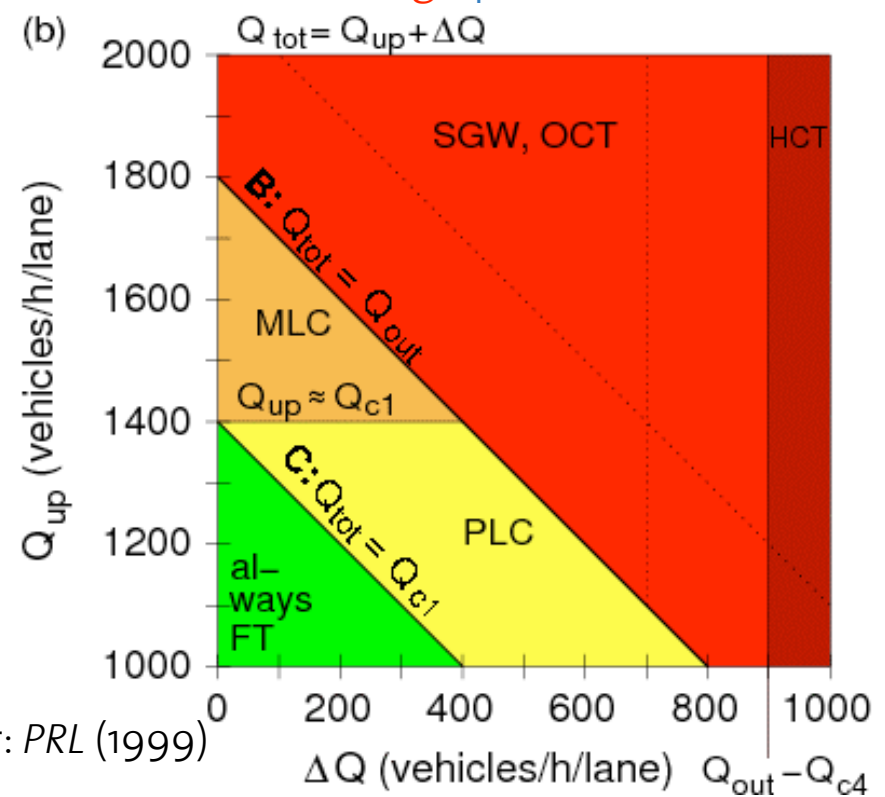
Grey areas = metastable regimes, where result depends on perturbation amplitude

# Phase Diagram of Traffic States and Universality Classes

Phase diagram for **small** perturbations



for **large** perturbations



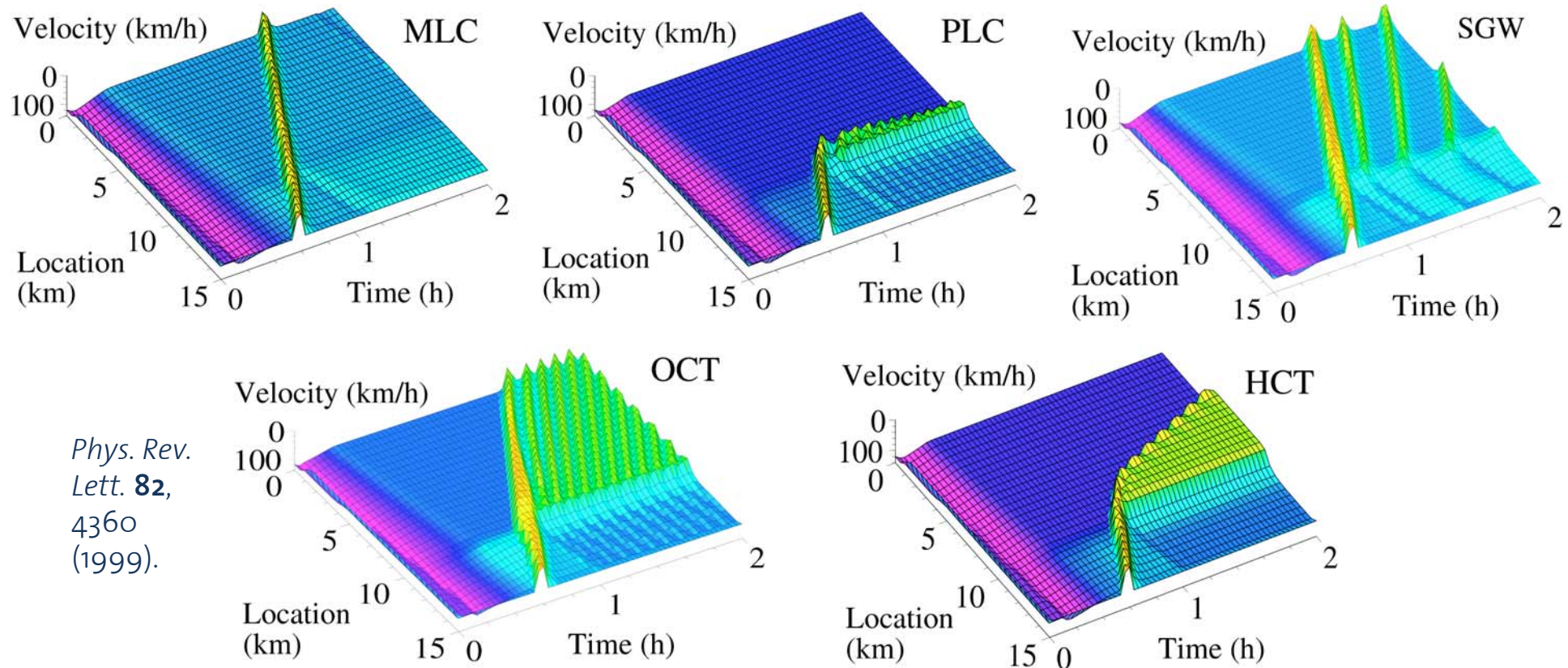
After: PRL (1999)

Phase diagrams are not only important to **understand the conditions** under which certain traffic states emerge. They also allow one to **categorize** the more than 100 traffic models into different **universality classes**. From the universality class that reproduces the empirically observed stylized facts, one may choose any representative, e.g. the **simplest** or the **most accurate** one, **depending on the purpose**.



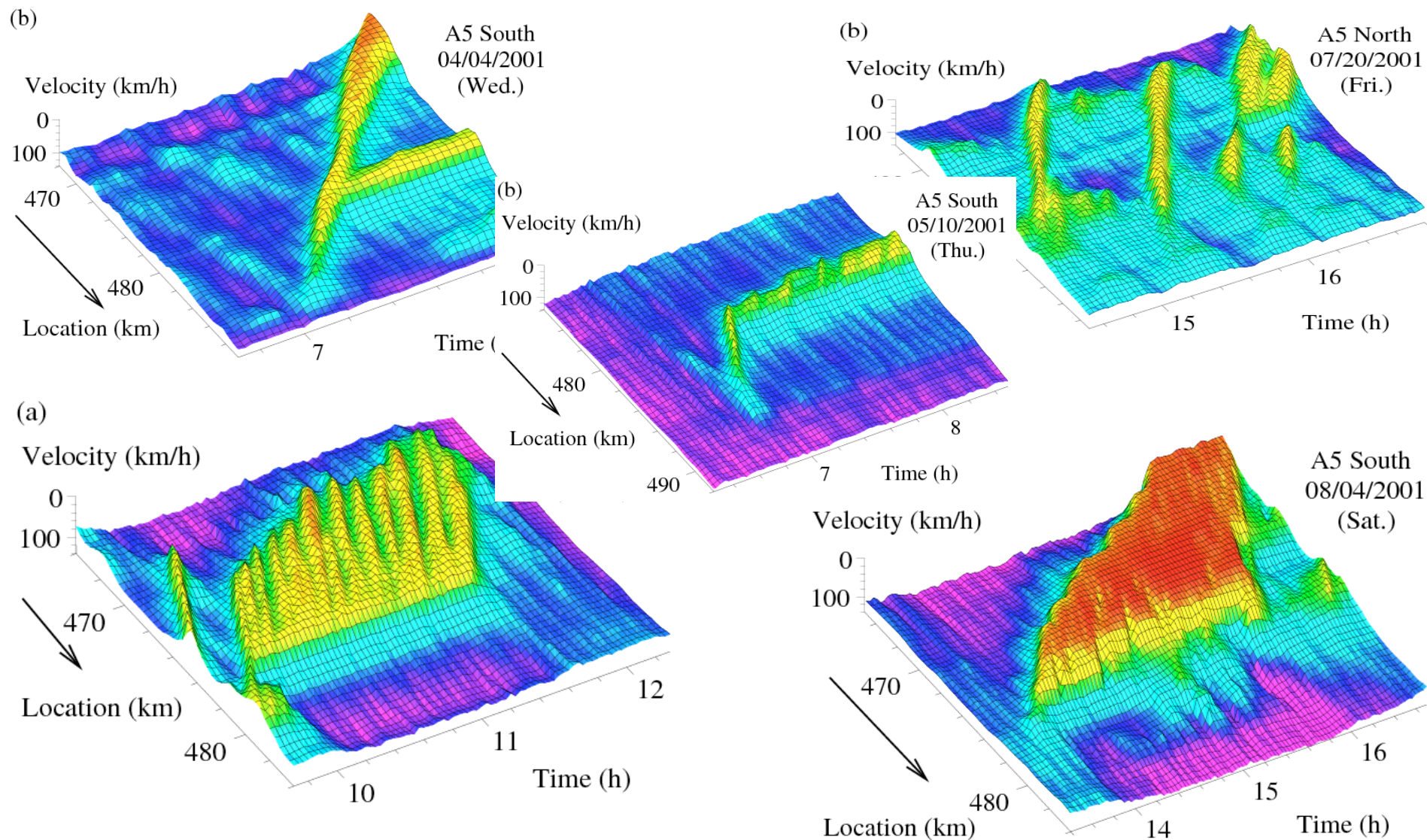
# Congested Traffic States Simulated with a Macroscopic Traffic Model

Perturbing traffic flows and, paradoxically, even *decreasing* them may sometimes cause congestion.

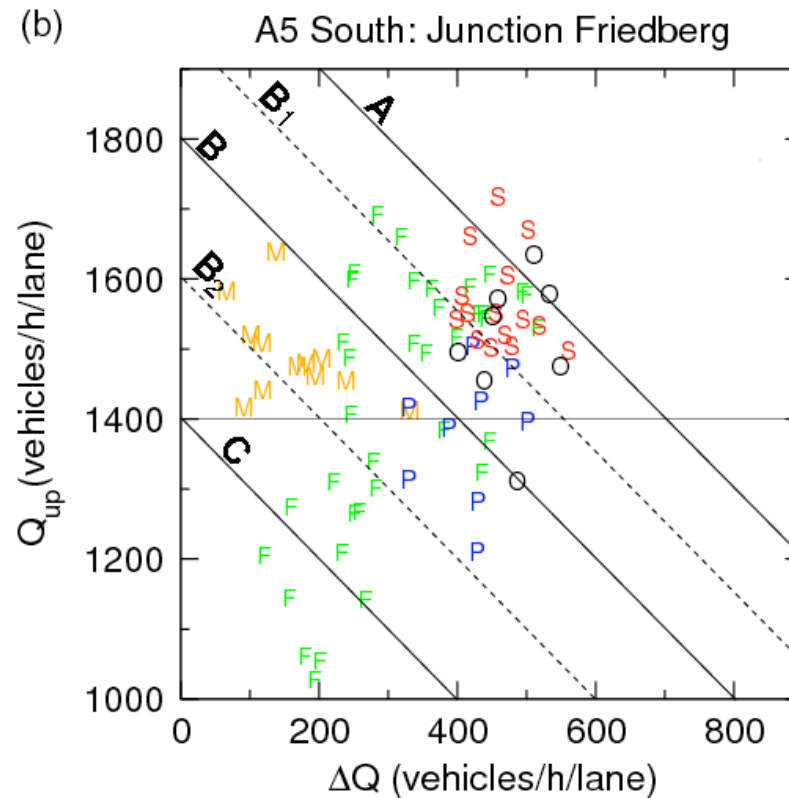
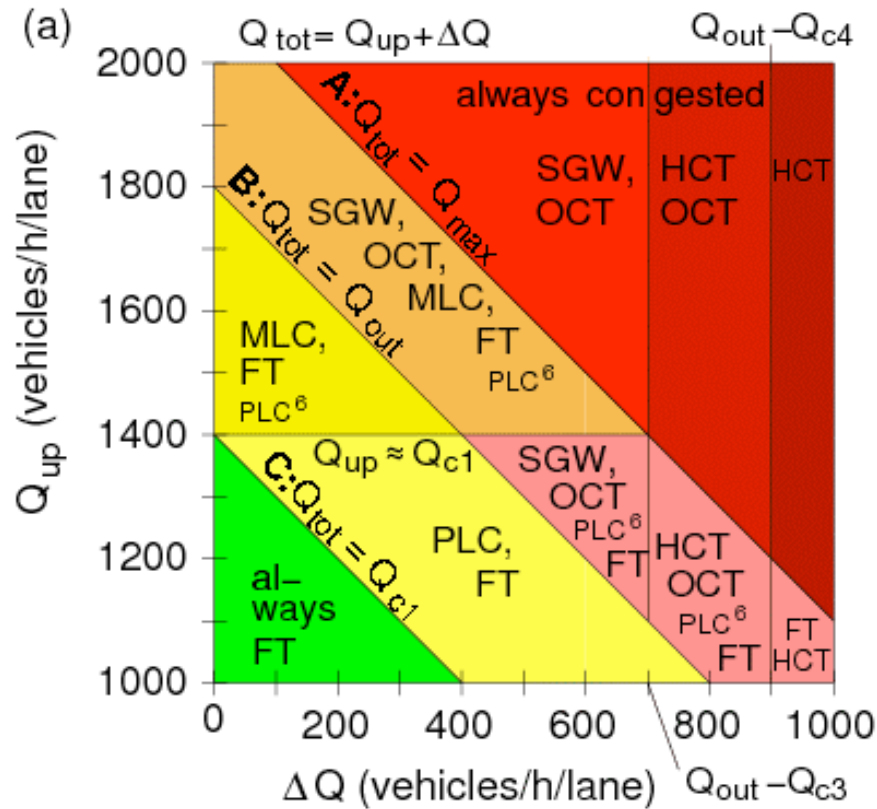


Similar congested traffic states are found for several other traffic models, including “microscopic” car-following models.

# Summary of Elementary Congestion Patterns

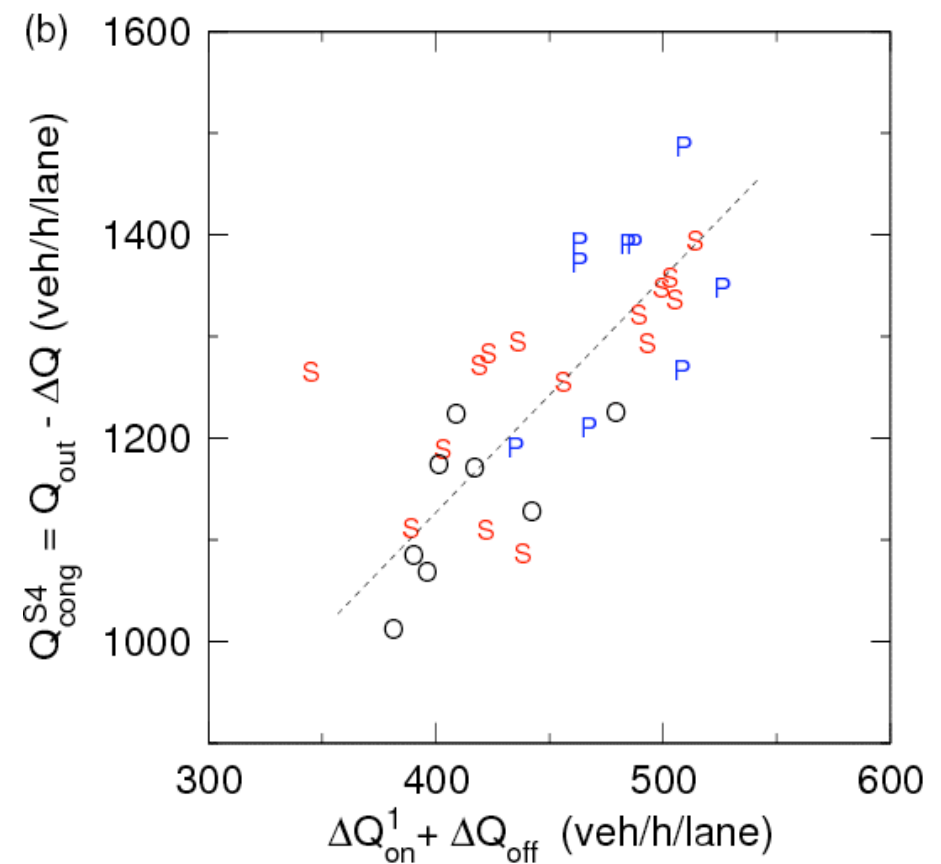
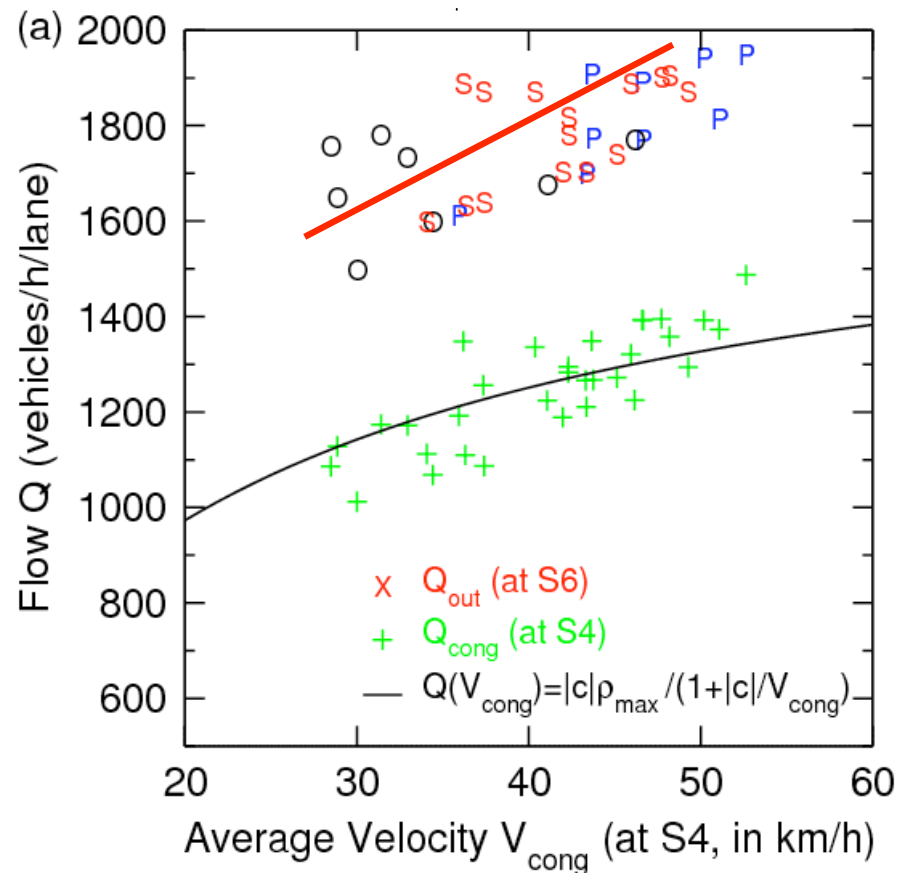


# Theoretical vs. Empirical Phase Diagram



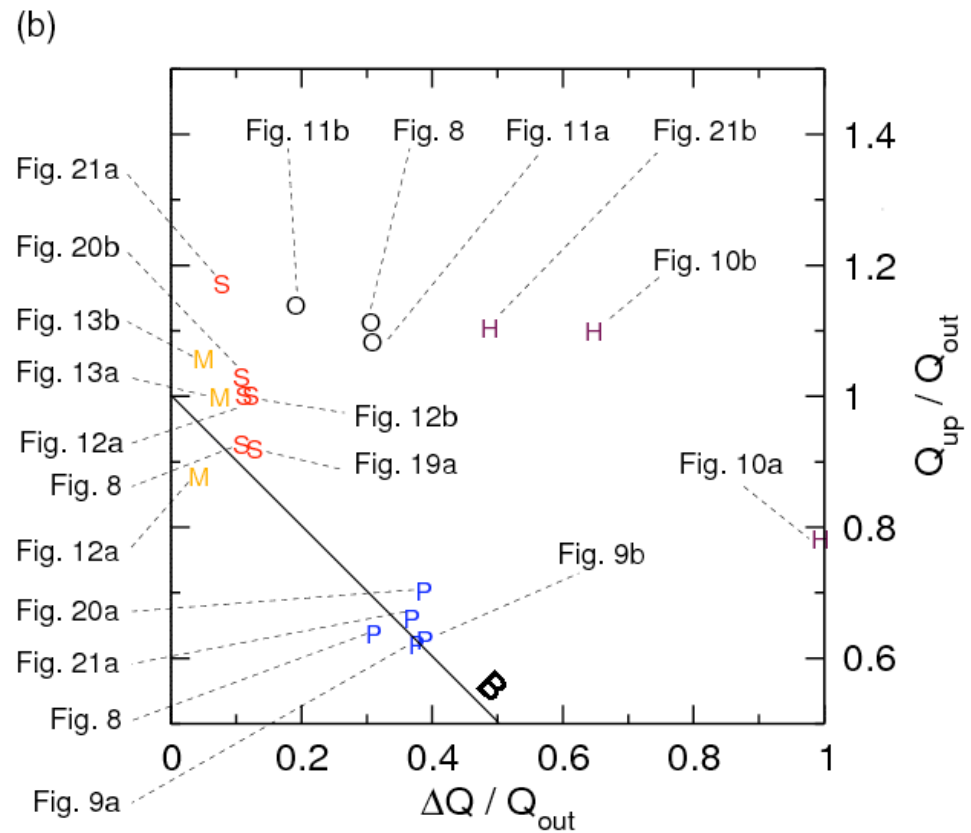
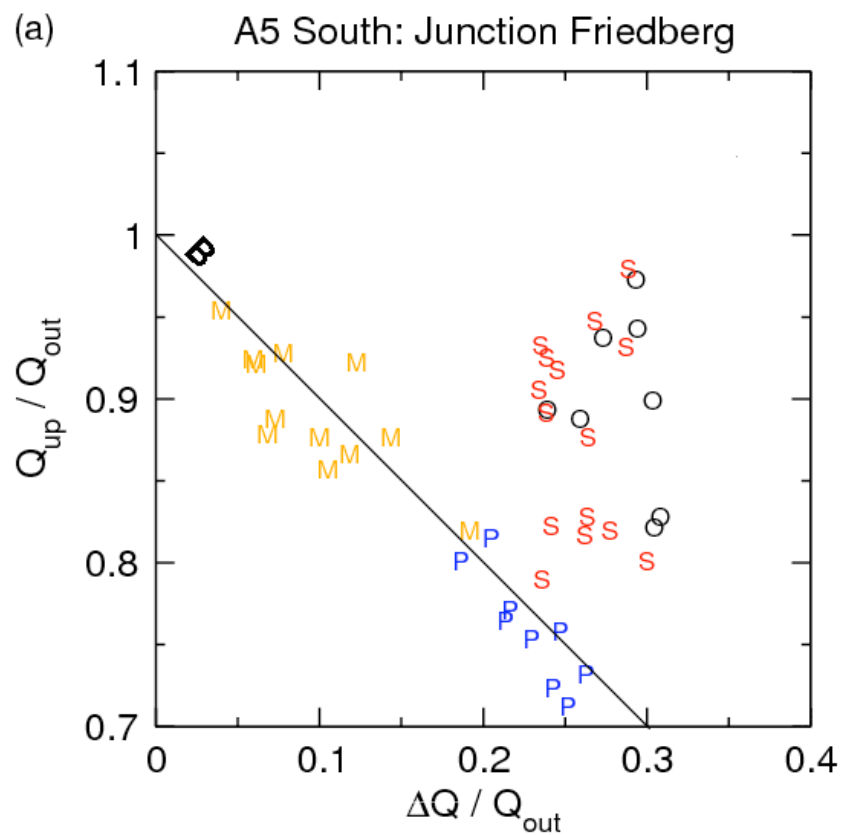
The outflow varies between B1 and B2. For statistical reasons?

# The Outflow Correlates with Other Traffic Variables



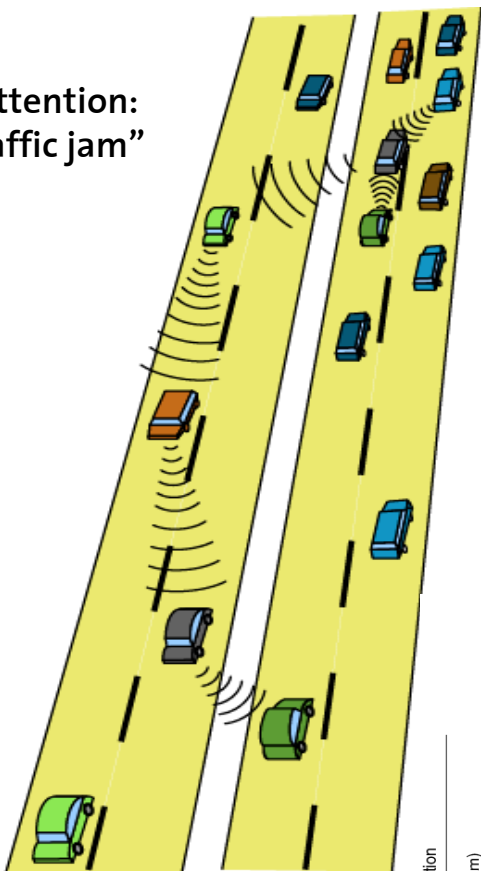
# Empirical Phase Diagram for Scaled Flows

A scaling by the outflow, that varies from day to day, gives a clearer picture.



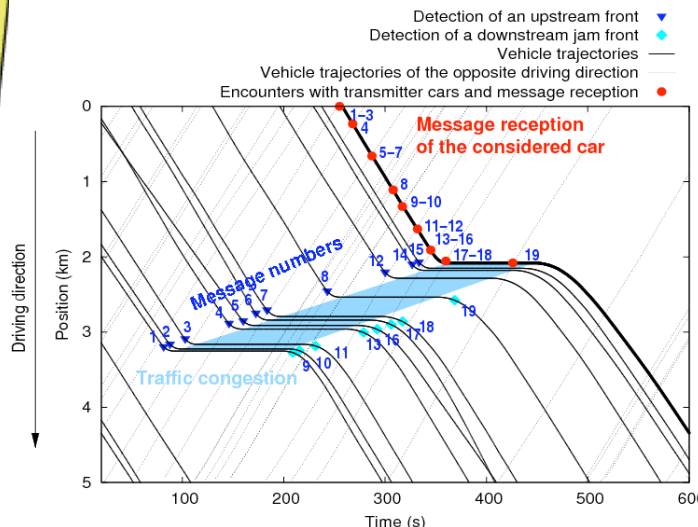
# Cooperative Driving Based on Autonomous Vehicle Interactions

“Attention: Traffic jam”



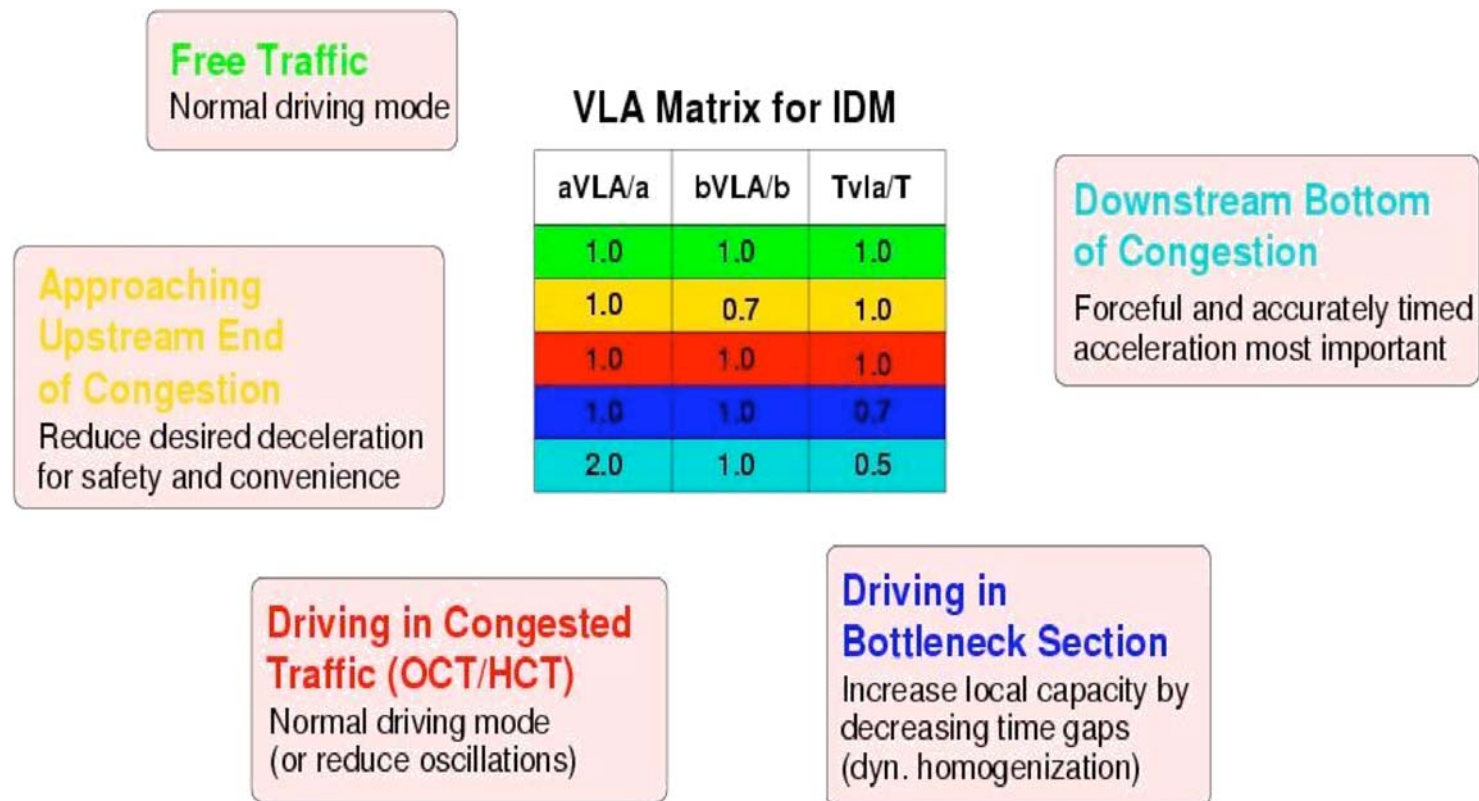
In: *Transportation Research Record* (2007)

- On-board data acquisition („perception“)
- Inter-vehicle communication
- Cooperative traffic state determination (“cognition“)
- Adaptive choice of driving strategy (“decision-making“)
- Driver information
- Traffic assistance (higher stability and capacity of traffic flow)



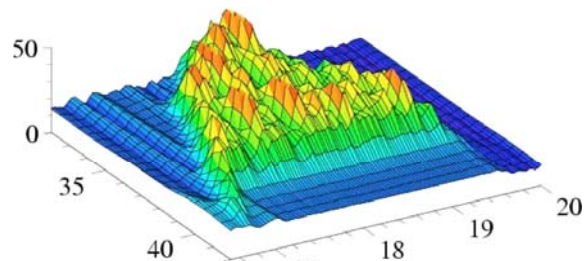
# Design of Traffic State Adaptive Cruise Control

Invent-VLA: Intelligent Adaptive Cruise Control (IACC) for the avoidance of traffic breakdowns and a faster recovery from congested traffic

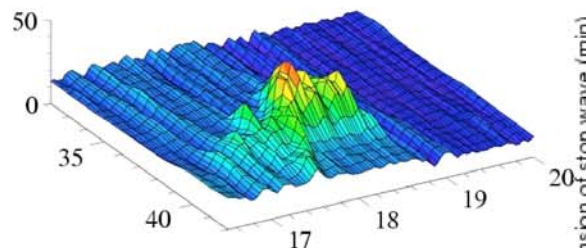


# Enhancing Traffic Performance by Adaptive Cruise Control

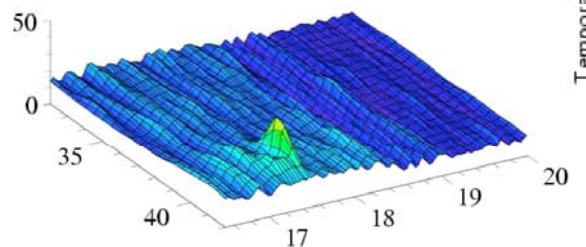
$\rho$ (veh./km/lane)



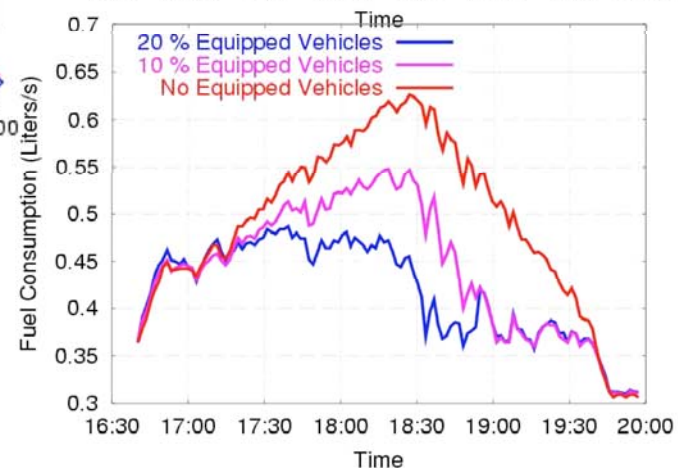
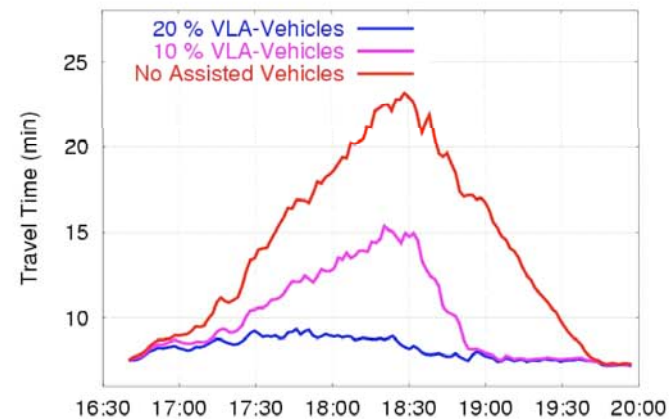
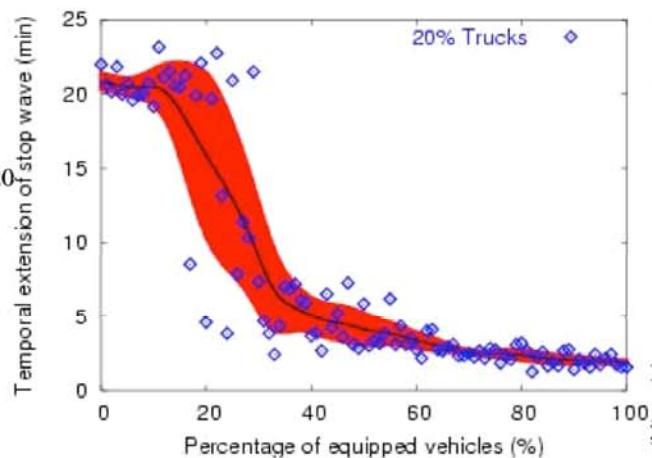
10% Equipped Vehicles



20% Equipped Vehicles



- Traffic breakdowns delayed
- Faster recovery to free traffic
- High impact on travel times
- Reduced fuel consumption and emissions



“Mechanism design”,  
in cooperation with

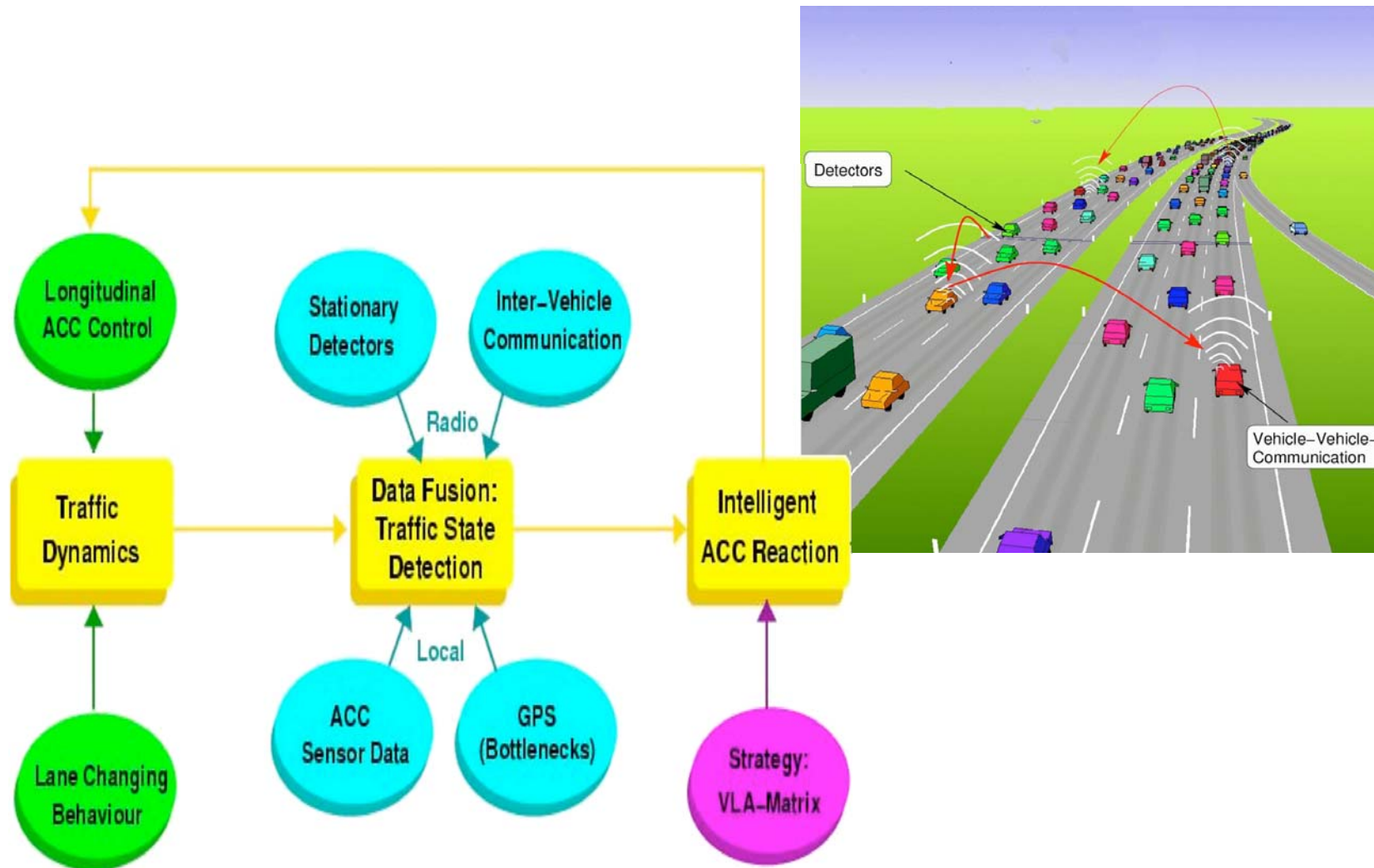




## 3D Assessment of Traffic Scenarios



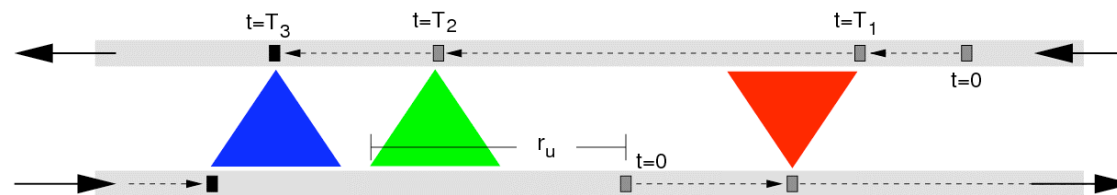
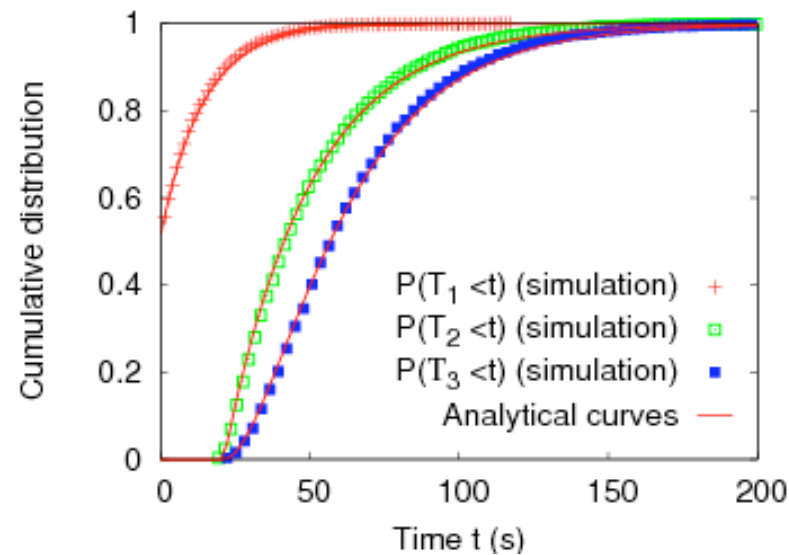
# Data Fusion for Dynamic Traffic State Detection



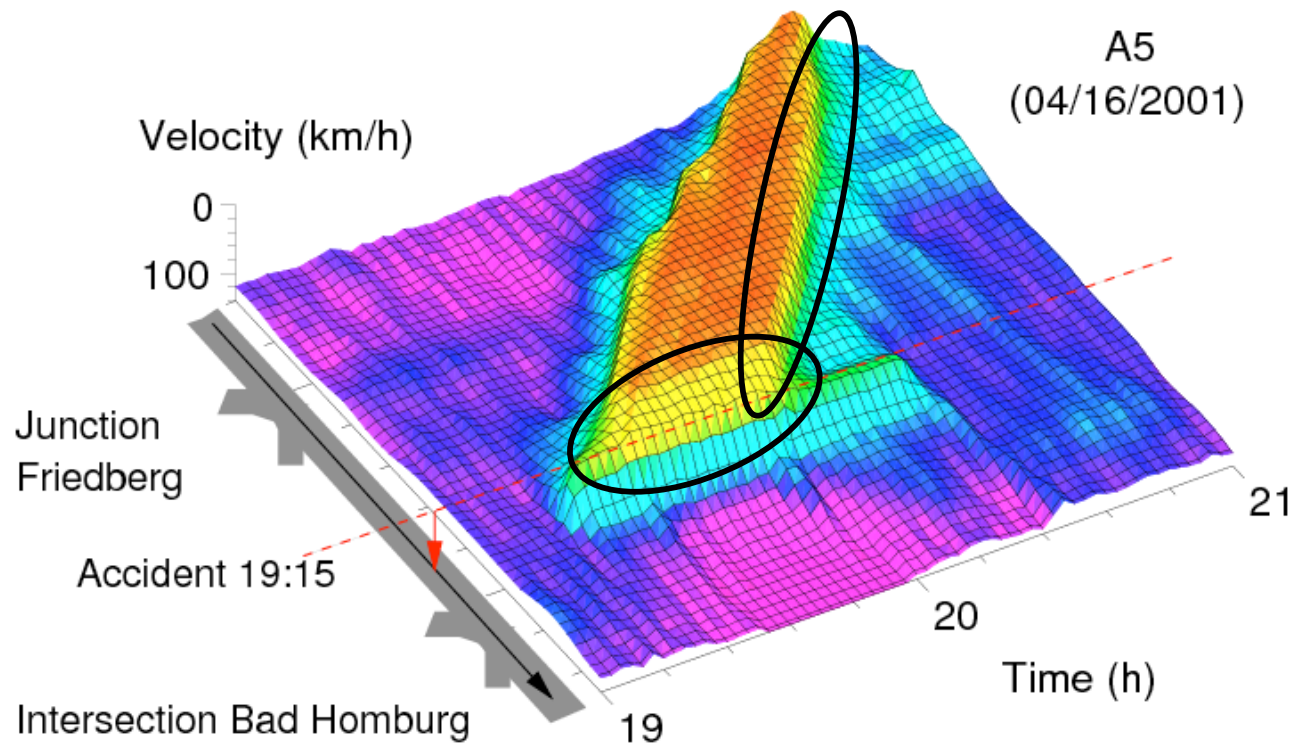
## Statistics of Message Transmission

Distance between communicating vehicles exponentially distributed  
→ Distributions for  $T_1$ ,  $T_2$ , and  $T_3$ ,

e.g. 
$$P(T_2 < t) = \Theta \left( t - \frac{r_{\text{up}} - 2r}{v} \right) \left( 1 - e^{-\beta(2r+vt-r_{\text{up}})} \right)$$

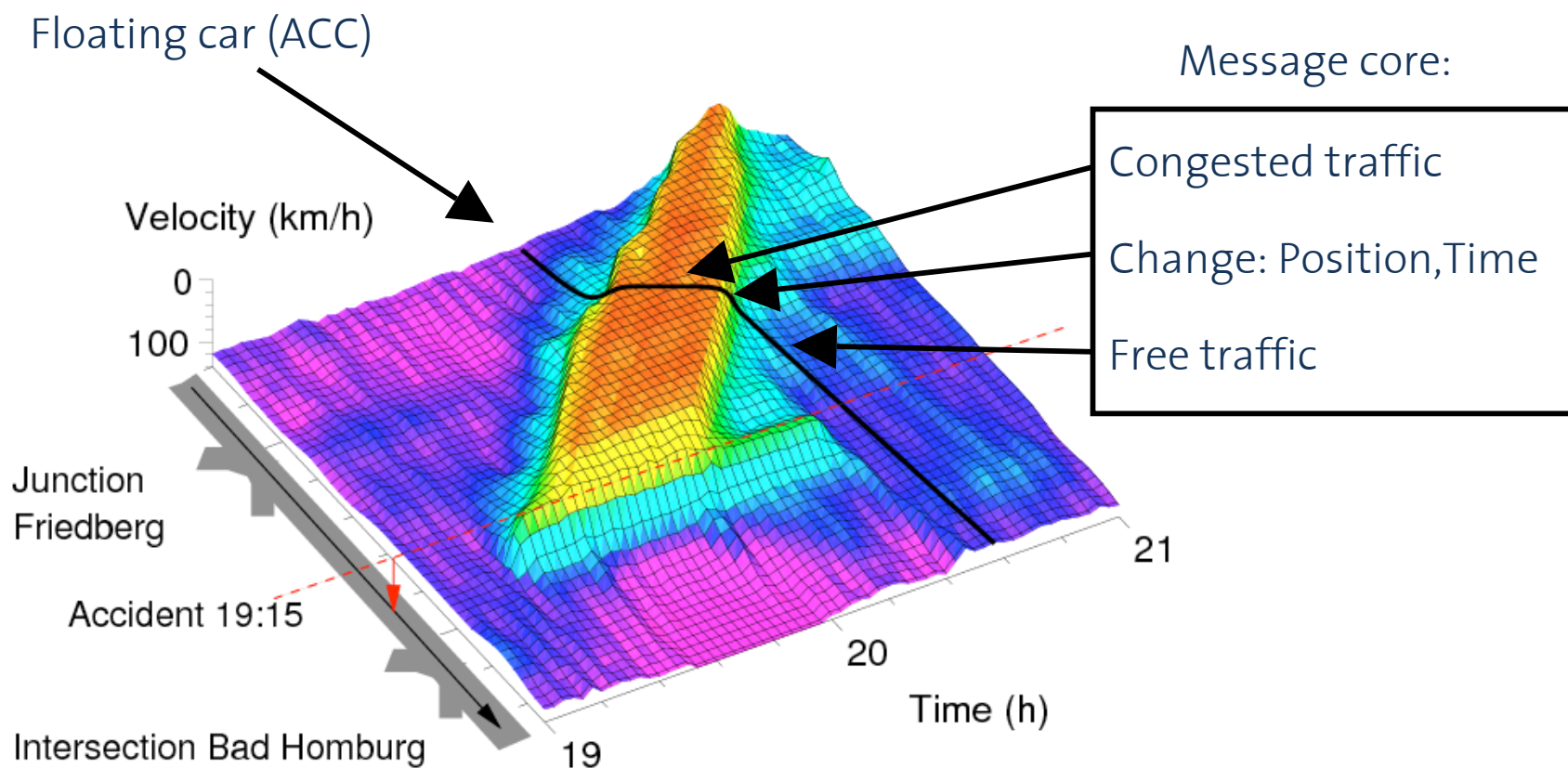


# Spatiotemporal Dynamics of a Traffic Jam

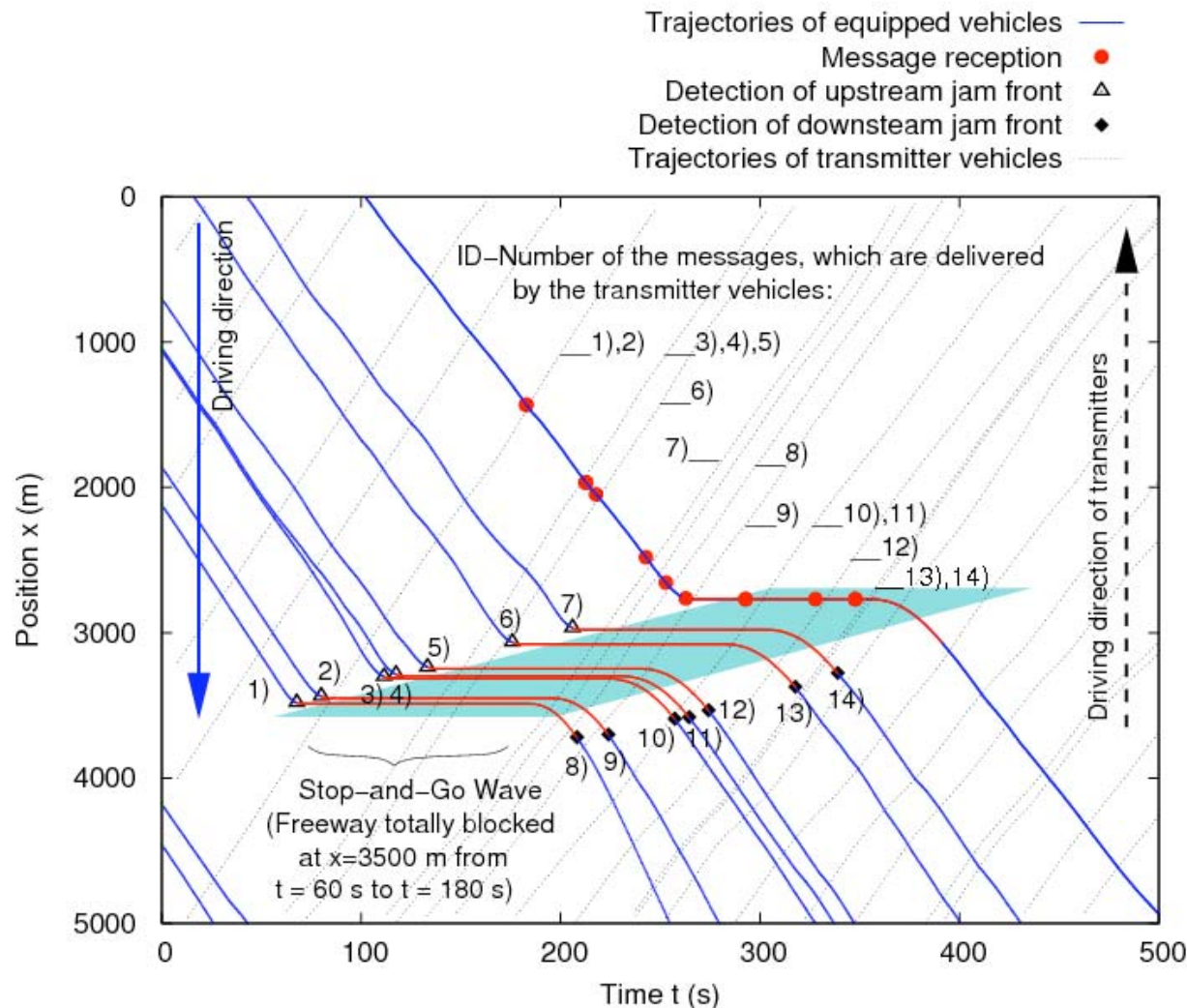


Downstream jam fronts

# Jam Front Detection - Message Generation

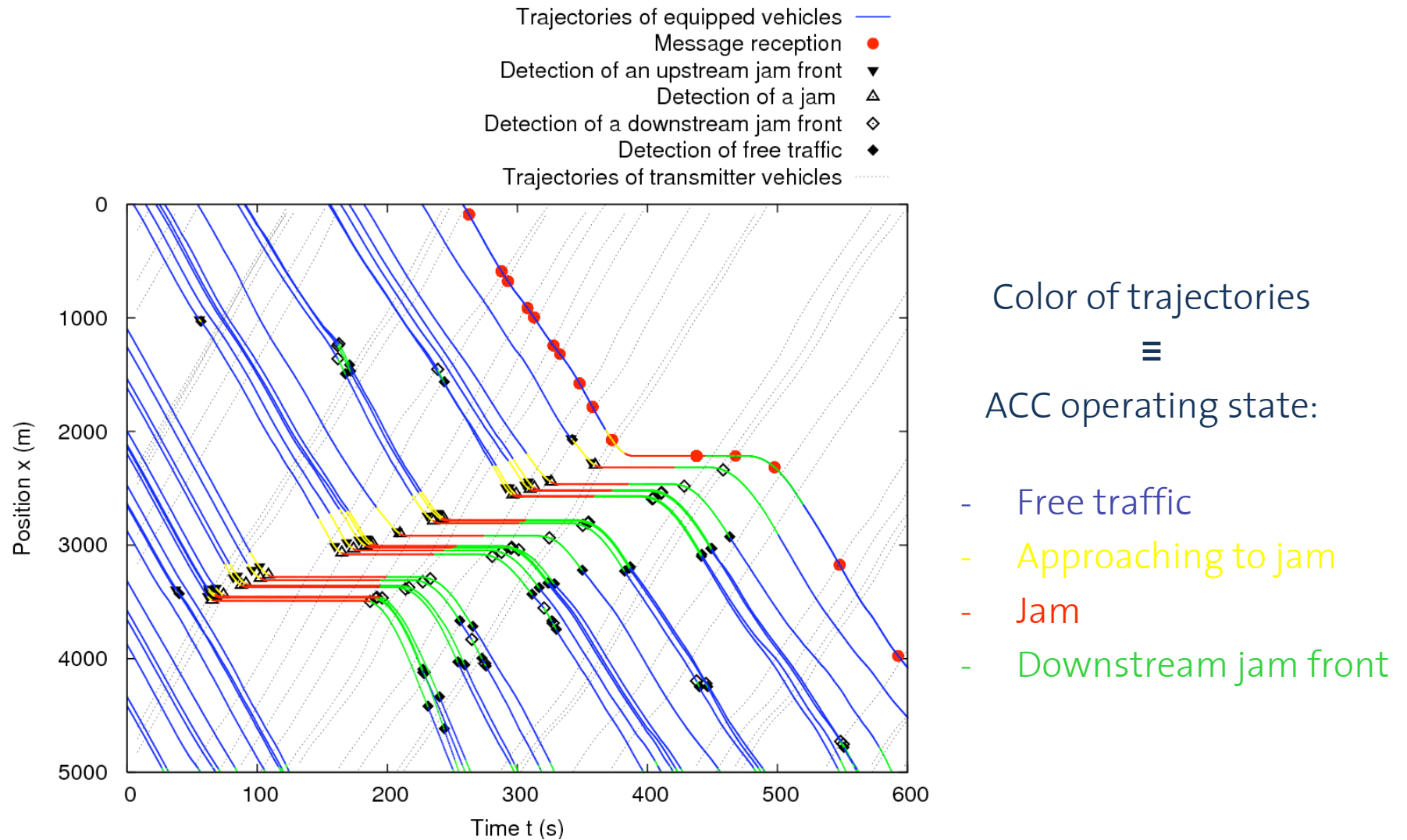


# Example: Information about a Stop-and-Go Wave



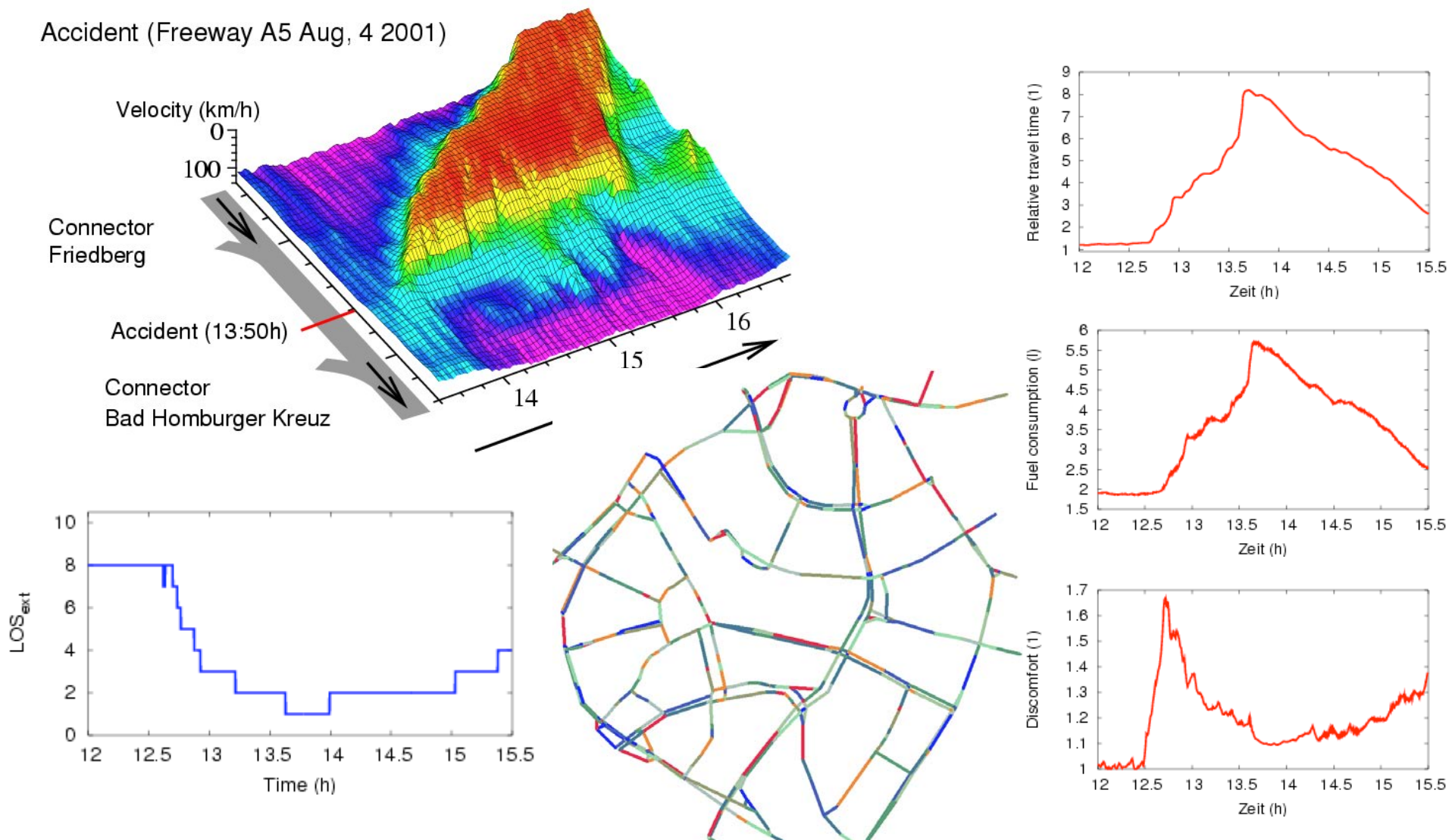
- 1) Upstream jam front at x=3481 m, t=68 s
- 2) Upstream jam front at x=3436 m, t=80 s
- 3) Upstream jam front at x=3302 m, t=111 s
- 4) Upstream jam front at x=3285 m, t=117 s
- 5) Upstream jam front at x=3236 m, t=133 s
- 6) Upstream jam front at x=3065 m, t=176 s
- 7) Upstream jam front at x=2966 m, t=206 s
- 8) Free traffic at x=3719 m, t=208 s
- 9) ...

# Traffic-Adaptive Driving Strategy for ACC



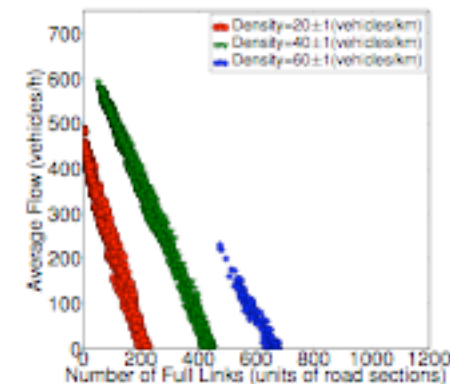
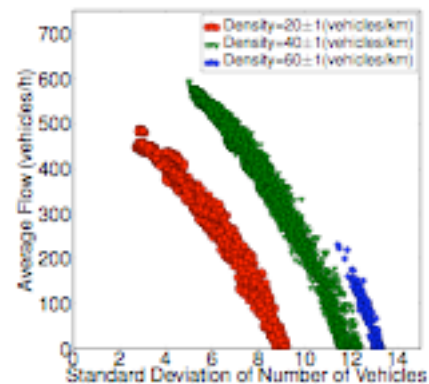
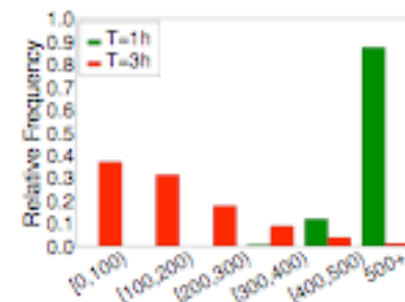
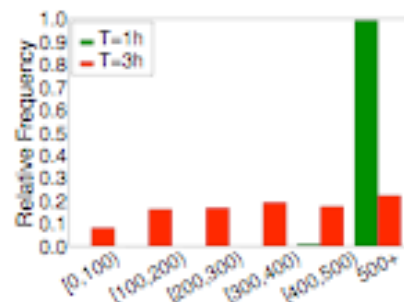
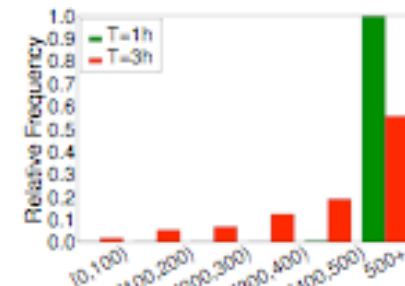
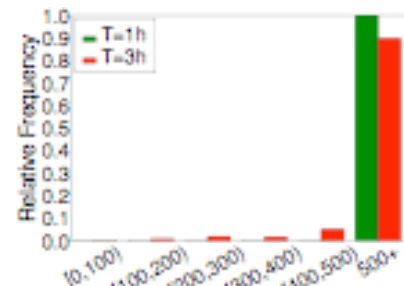
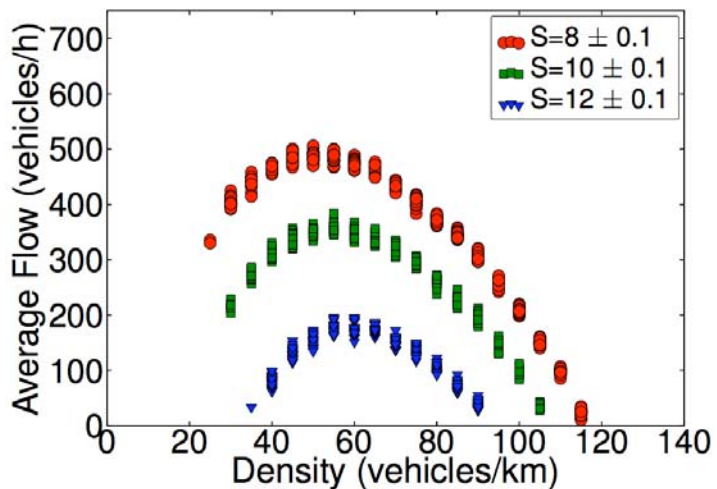
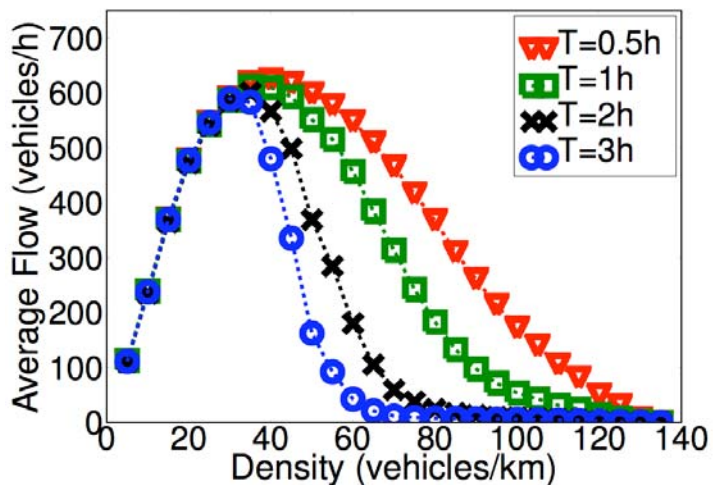
# Evaluation of a Driver-Oriented Level of Service

Accident (Freeway A5 Aug, 4 2001)



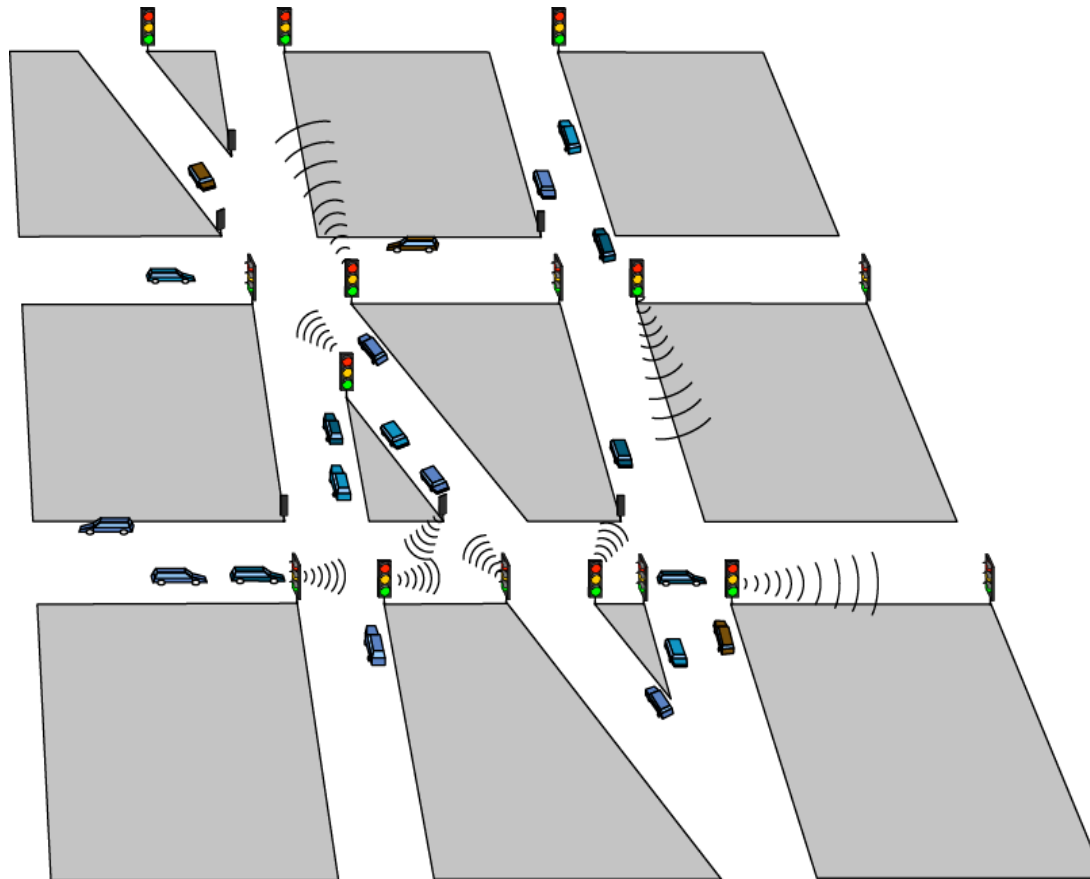


# Variability of Urban Traffic Flows



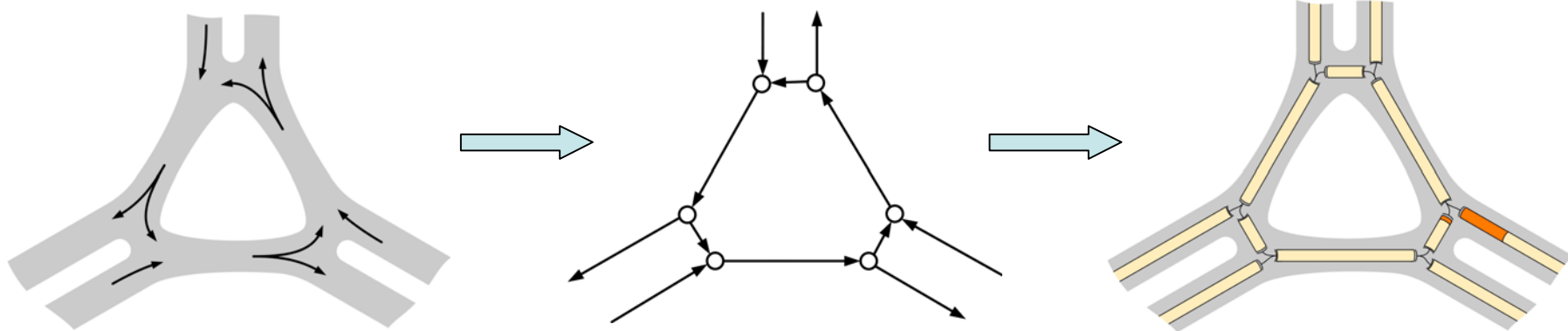
# Adaptive Traffic Light Control

- for complex street networks
- for traffic disruptions (building sites, accidents, etc.)
- for particular events (Olympic games, pop concerts, etc.)



## Road Network as Directed Graph

- **Directed links** are homogenous road sections
  - Traffic dynamics: congestion, queues
- **Nodes** are connectors between road sections
  - Junctions: merging, diverging



- **Intersections**
  - Traffic lights: control, optimization
- **Traffic assignment**
  - Route choice, destination flows

Local Rules,  
Decentralization,  
Self organization

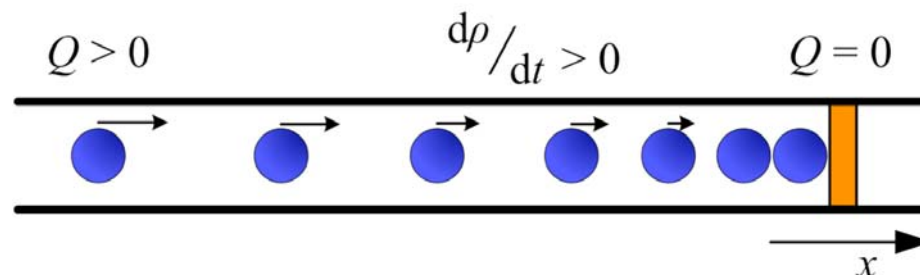
## Traffic Dynamics: Macroscopic Approach

- “Traffic is a fluid medium.”
  - Describing values:

$V$  ... velocity (in m/s)  
 $\rho$  ... density (in vcl/m)  
 $Q$  ... flow (in vcl/s)

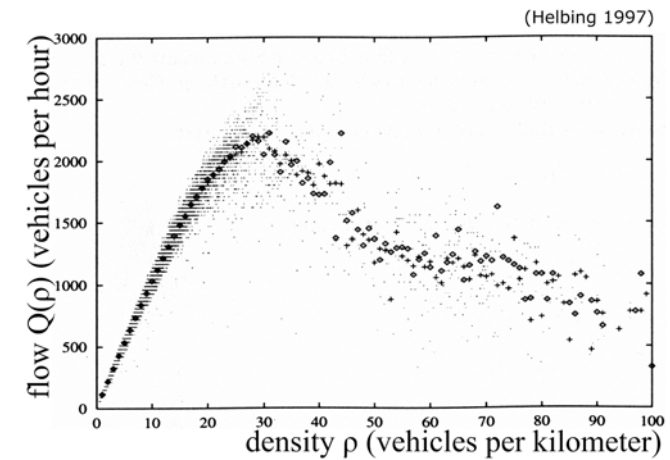
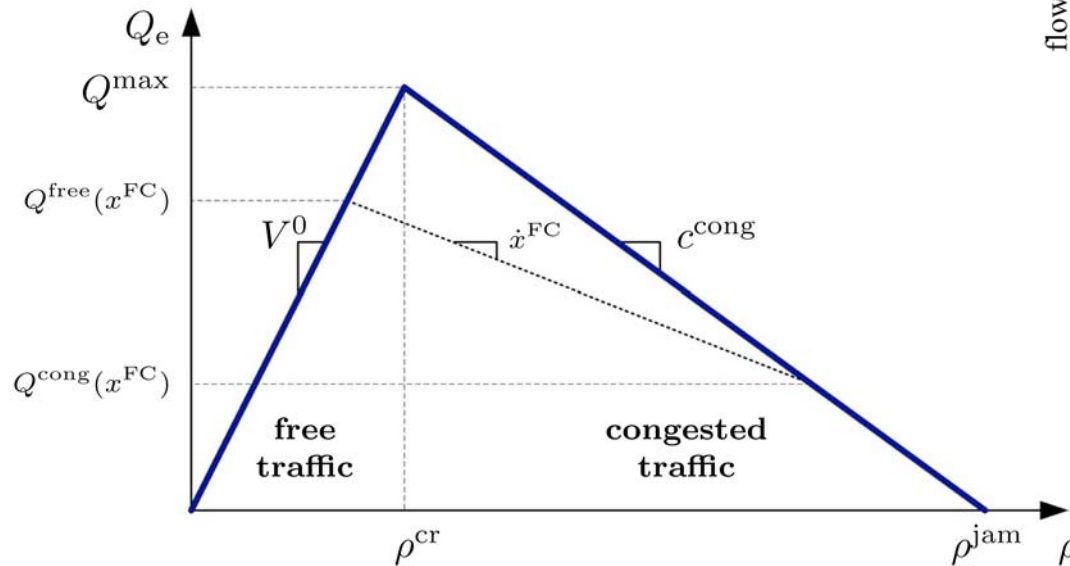
- Conservation of vehicles
  - Continuity equation:

$$\frac{\partial \rho(x, t)}{\partial t} + \frac{\partial Q(x, t)}{\partial x} = 0$$



# Traffic Dynamics: Fundamental Diagram

- “Flow  $Q$  and density  $\rho$  are empirically correlated.”



$$\frac{\partial \rho}{\partial t} + \underbrace{\frac{dQ_e(\rho)}{d\rho}}_{c(\rho)} \cdot \frac{\partial \rho}{\partial x} = 0$$

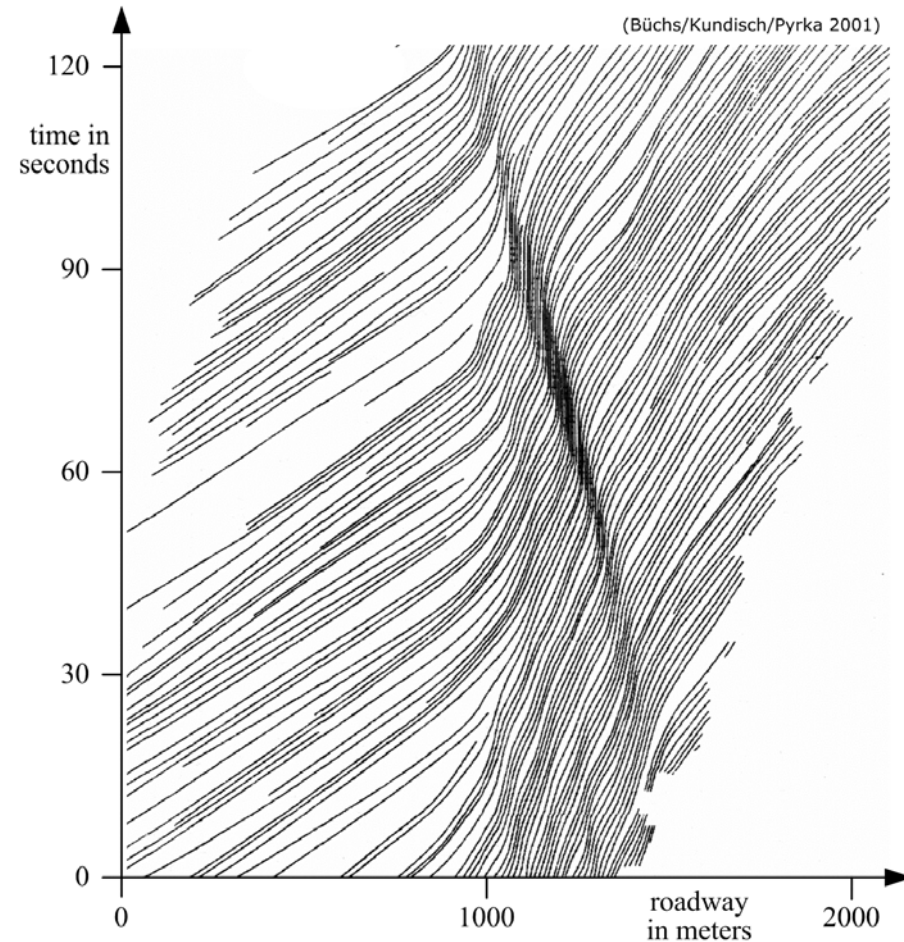
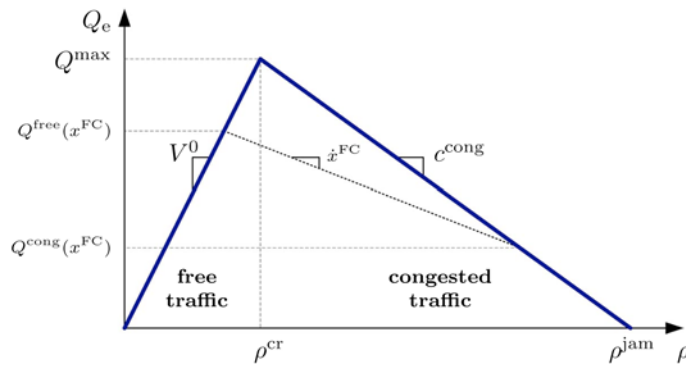
Derivation  $Q_e'$  plays  
important role!

# Traffic Dynamics: Shock Waves

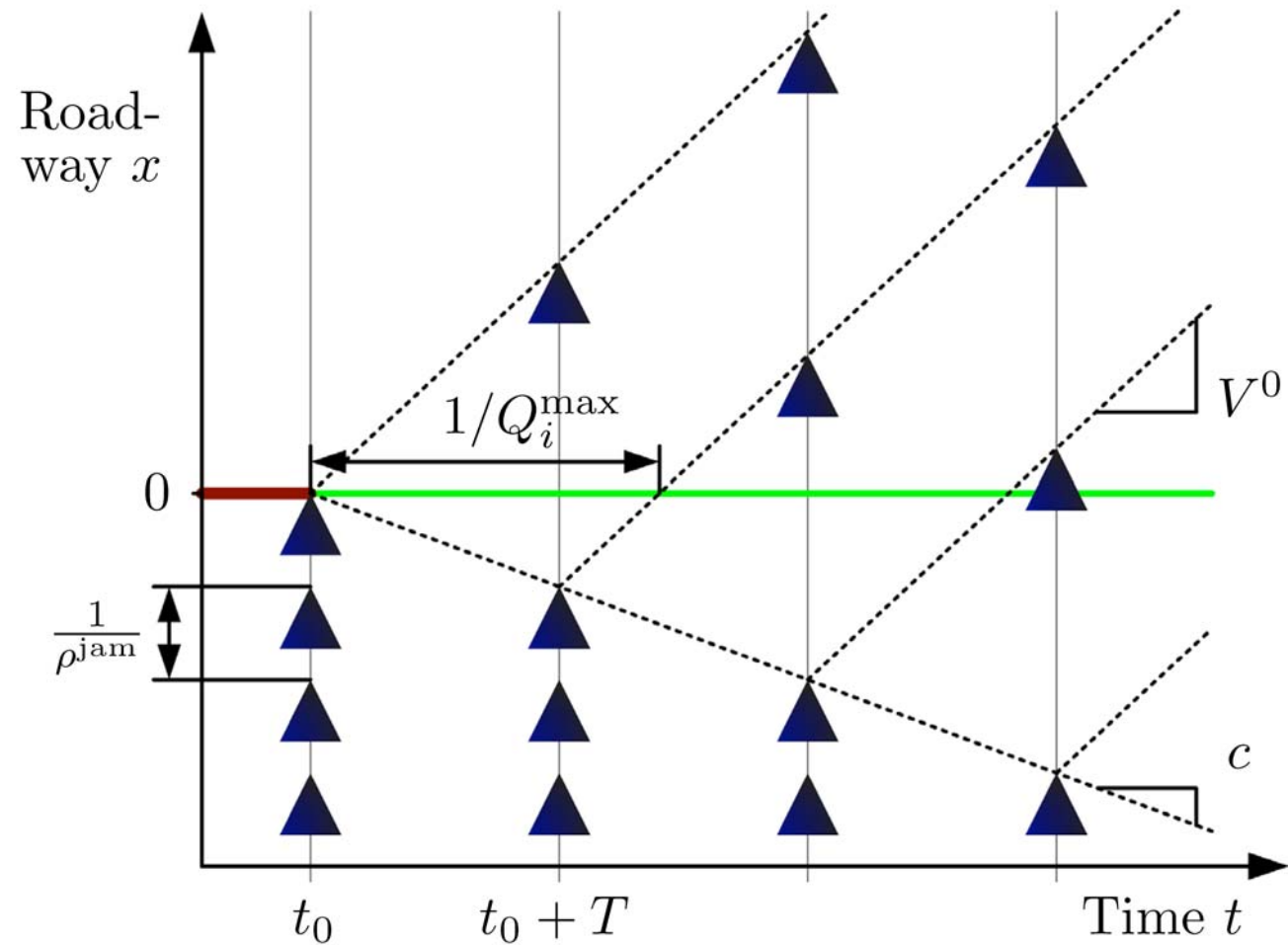
- Propagation velocity  $c(\rho)$

$$c(\rho) = \frac{dQ_e(\rho)}{d\rho}$$

- Free traffic:
  - $c(\rho) = V^0$
- Congested traffic:
  - $c(\rho) \approx -15 \text{ km/h}$  (universal)



# Characteristic Velocities







## A Queueing-Theoretical Traffic Model

The **continuity equation** for the **vehicle density**  $\rho(x,t)$  at place  $x$  and time  $t$  in road section  $i$  is

$$\frac{\partial \rho(x,t)}{\partial t} + \frac{\partial Q_i(x,t)}{\partial x} = \text{Source Terms}$$

We assume the fundamental **flow-density relation**

$$Q_i(\rho) = \begin{cases} Q_i^{\text{free}}(\rho) = \rho V_i^0 & \text{if } \rho < \rho_{\text{cr}} \\ Q_i^{\text{cong}}(\rho) = (1 - \rho / \rho_{\text{jam}}) / T & \text{otherwise} \end{cases}$$

$V_i^0$  = free speed on road section  $i$

$T$  = safe time gap

$\rho_{\text{jam}}$  = jam density

The **number**  $N_i$  of **vehicles in section**  $i$  changes according to

$$\frac{dN_i(t)}{dt} = Q_i^{\text{arr}}(t) - Q_i^{\text{dep}}(t) = Q_{i-1}^{\text{dep}}(t) + Q_{i-1}^{\text{ramp}}(t) - Q_i^{\text{dep}}(t)$$

$Q_i^{\text{arr}}$  = arrival rate of vehicles

$Q_i^{\text{dep}}$  = departure rate of vehicles

**Treatment of ramp flows** at downstream section ends:

$$Q_{i+1}^{\text{arr}}(t) = Q_i^{\text{dep}}(t) + Q_i^{\text{ramp}}(t)$$

## A Queueing-Theoretical Traffic Model

The **traffic-state dependent departure rate** is given by

$$Q_i^{\text{dep}}(t) = \begin{cases} Q_i^{\text{arr}}(t - T_i^{\text{free}}) & \text{if } S_{i+1}(t) \neq 1 \text{ and } S_i(t) = 0 \\ Q_i^{\text{cap}}(t) & \text{if } S_{i+1}(t) \neq 1 \text{ and } S_i(t) \neq 0 \\ Q_i^{\text{dep}}(t - T_{i+1}^{\text{cong}}) - Q_i^{\text{ramp}}(t) & \text{if } S_{i+1}(t) = 1 \end{cases}$$

The **capacity of congested road section** is:

$$Q_i^{\text{cap}}(t) = I_i Q_{\text{out}}(t) - \max[Q_i^{\text{ramp}}(t), (I_i - I_{i+1})Q_{\text{out}}, \Delta Q_i(t), 0]$$

$I_i$  = number of lanes

$Q_{\text{out}} = (1 - \rho_{\text{cr}} / \rho_{\text{jam}}) / T$  = outflow per lane from congested traffic

The **maximum capacity in free traffic** is:

$$Q_i^{\text{max}}(t) = I_i \rho_{\text{cr}} V_i^0 - \max[Q_i^{\text{ramp}}(t), (I_i - I_{i+1}) \rho_{\text{cr}} V_i^0, \Delta Q_i(t), 0]$$

Definition of **free** ( $S_i = 0$ ), **fully congested** ( $S_i = 1$ ) and **partially congested** ( $S_i = 2$ ) **traffic states**:

$$S_i(t) = \begin{cases} 0 & \text{if } l_i(t) = 0 \text{ and } Q_i^{\text{arr}}(t - dt - T_i^{\text{free}}) < Q_i^{\text{max}}(t - dt) \\ 1 & \text{if } l_i(t) = L_i \text{ and } Q_i^{\text{dep}}(t - dt - T_i^{\text{cong}}) \leq Q_i^{\text{arr}}(t - dt) \\ 2 & \text{otherwise} \end{cases}$$

$L_i$  = length of road section  $i$ ,  $l_i$  = length of congested road section

## A Queueing-Theoretical Traffic Model

Growth of the length  $l_i$  of congested traffic according to shock wave theory:

$$\frac{dl_i}{dt} = - \frac{Q_i^{\text{dep}}(t - l_i(t)/c) - Q_i^{\text{arr}}(t - [L_i - l_i(t)]/V_i^0)}{\rho_i^{\text{cong}}(Q_i^{\text{dep}}(t - l_i(t)/c)/I_i) - \rho_i^{\text{free}}(Q_i^{\text{arr}}(t - [L_i - l_i(t)]/V_i^0)/I_i)}$$

with densities

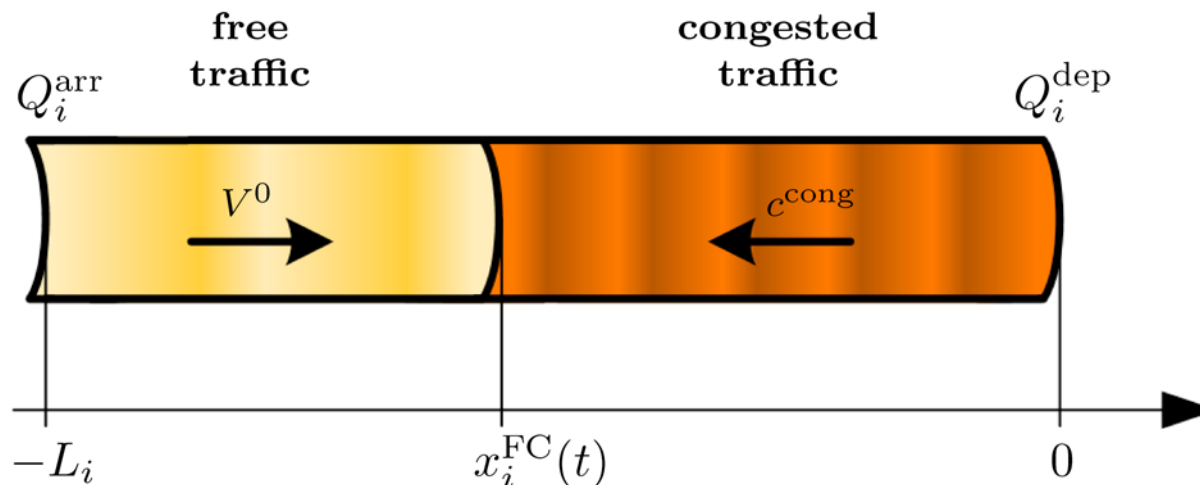
$$\rho_i^{\text{free}}(Q_i) = Q_i / V_i^0,$$

$$\rho_i^{\text{cong}}(Q_i) = (1 - TQ_i)\rho_{\text{jam}}$$

Delay-differential equation for the travel time  $T_i$  on section  $i$ , when entered at time  $t$ :

$$\frac{dT_i(t)}{dt} = \frac{Q_i^{\text{arr}}(t)}{Q_i^{\text{dep}}(t + T_i(t))} - 1 = \frac{Q_{i-1}^{\text{dep}}(t) + Q_{i-1}^{\text{ramp}}(t)}{Q_i^{\text{dep}}(t + T_i(t))} - 1$$

## Network Links: Homogenous Road Sections



- Movement of congestion

$$\frac{d}{dt} x_i^{\text{FC}} = \frac{\Delta Q(x_i^{\text{FC}})}{\Delta \rho(x_i^{\text{FC}})}$$

- Number of vehicles

$$\frac{d}{dt} N_i(t) = Q_i^{\text{arr}}(t) - Q_i^{\text{dep}}(t)$$

- Travel time

$$\frac{d}{dt} T_i(t) = 1 - \frac{Q_i^{\text{dep}}(t)}{Q_i^{\text{arr}}(t - T_i(t))}$$

## Network Nodes: Connectors

- Side Conditions

$$\sum_i Q_i^{\text{dep}} = \sum_j Q_j^{\text{arr}}$$

- Conservation

$$Q_i^{\text{dep}} \geq 0$$

$$Q_j^{\text{arr}} \geq 0$$

- Non-negativity

$$Q_i^{\text{dep}} \leq Q_i^{\text{dep,pot}}$$

$$Q_j^{\text{arr}} \leq Q_j^{\text{arr,pot}}$$

- Upper boundary

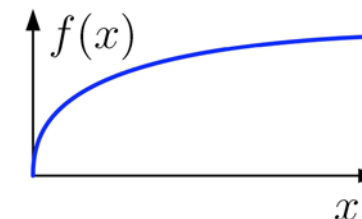
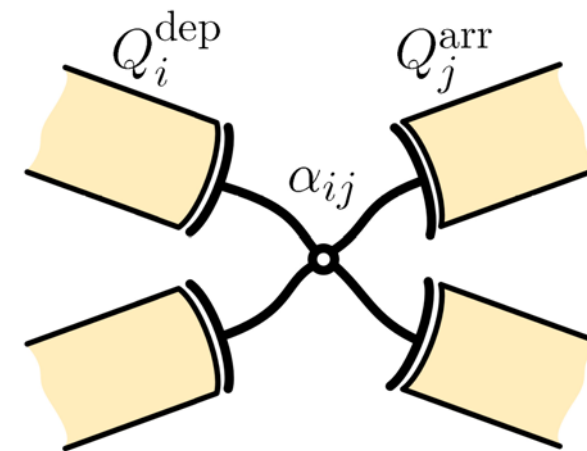
$$\sum_i \alpha_{ij} Q_i^{\text{dep}} = Q_j^{\text{arr}}$$

- Branching

$$F = \sum_i f(Q_i^{\text{dep}}) \rightarrow \max$$

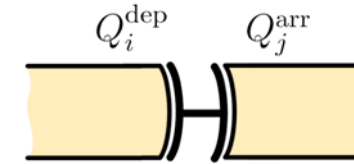
- Goal function

$$f(x) = x^p \quad \text{with } p \ll 1$$

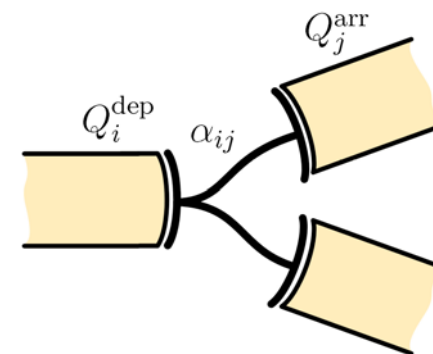


## Network Nodes: Special Cases

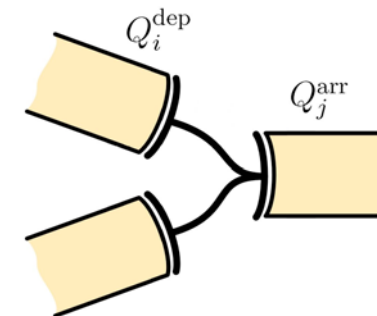
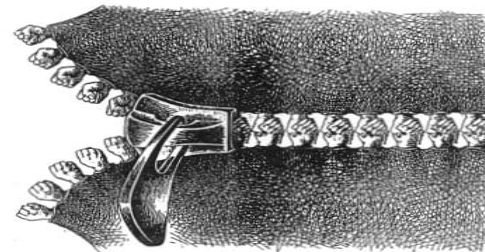
- **1 to 1:**  $Q_i^{\text{dep}} = Q_j^{\text{arr}} = \min \left\{ Q_i^{\text{dep,pot}}, Q_j^{\text{arr,pot}} \right\}$



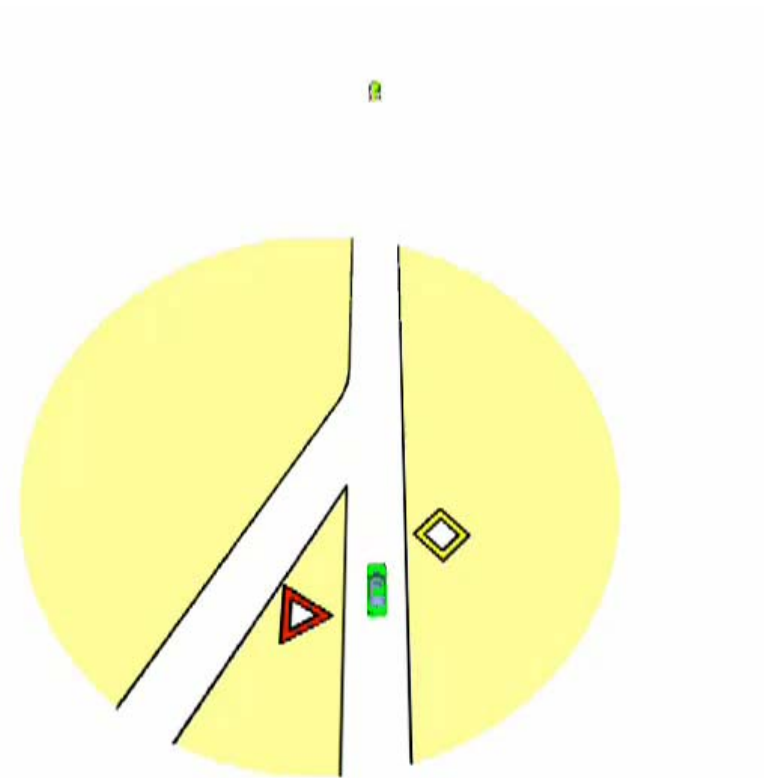
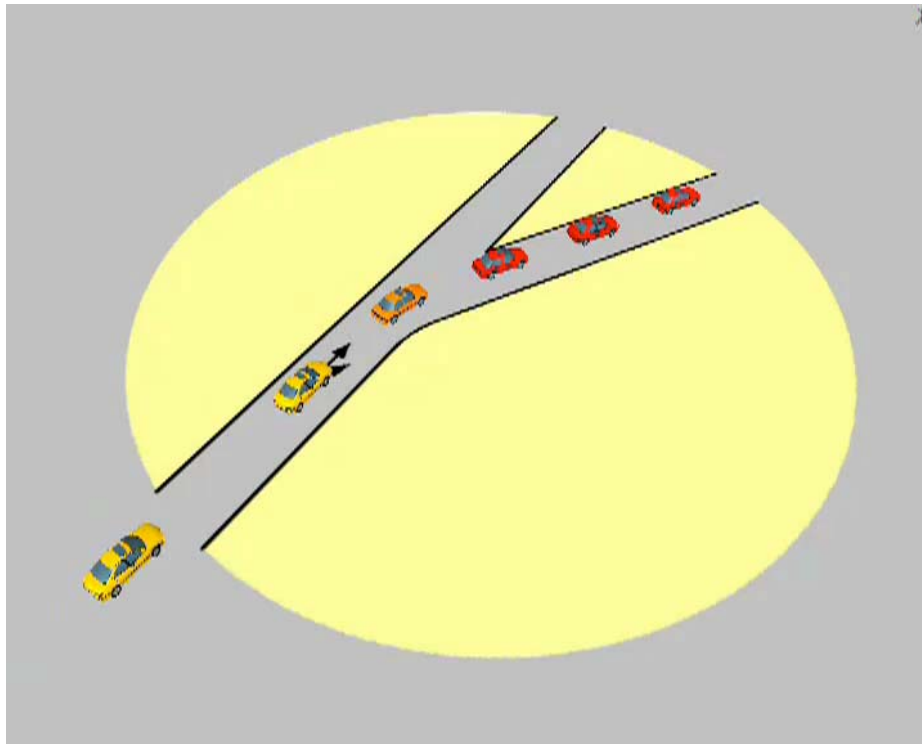
- **1 to n: Diverging**  $Q_i^{\text{dep}} = \min \left\{ Q_i^{\text{dep,pot}}, \min_j \frac{Q_j^{\text{arr,pot}}}{\alpha_{ij}} \right\}$   
 $Q_j^{\text{arr}} = \alpha_{ij} Q_i^{\text{dep}}$



- **n to 1: Merging**

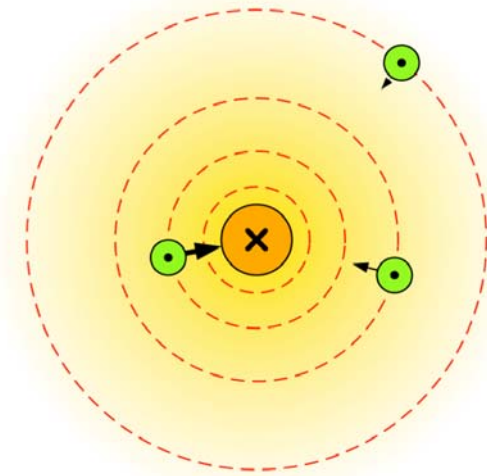


# Simulation of Diverges and Merges



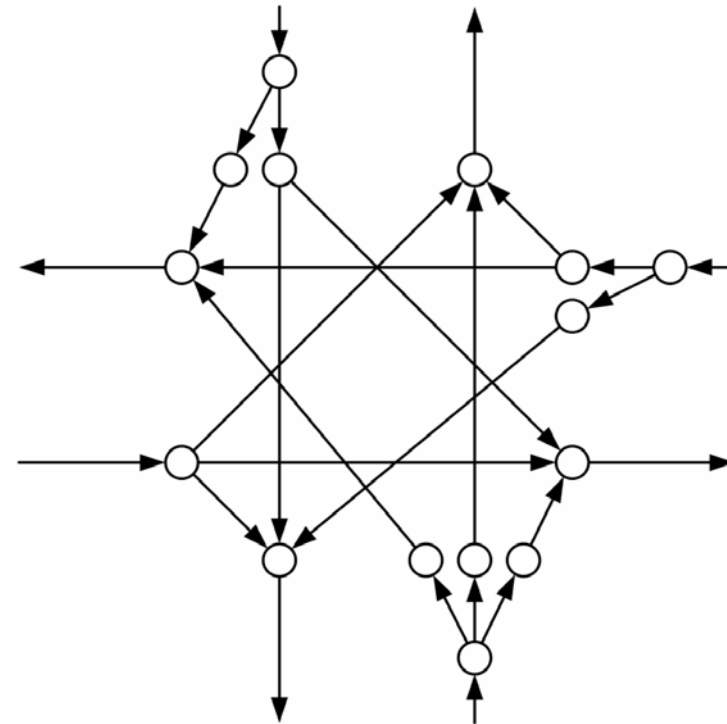
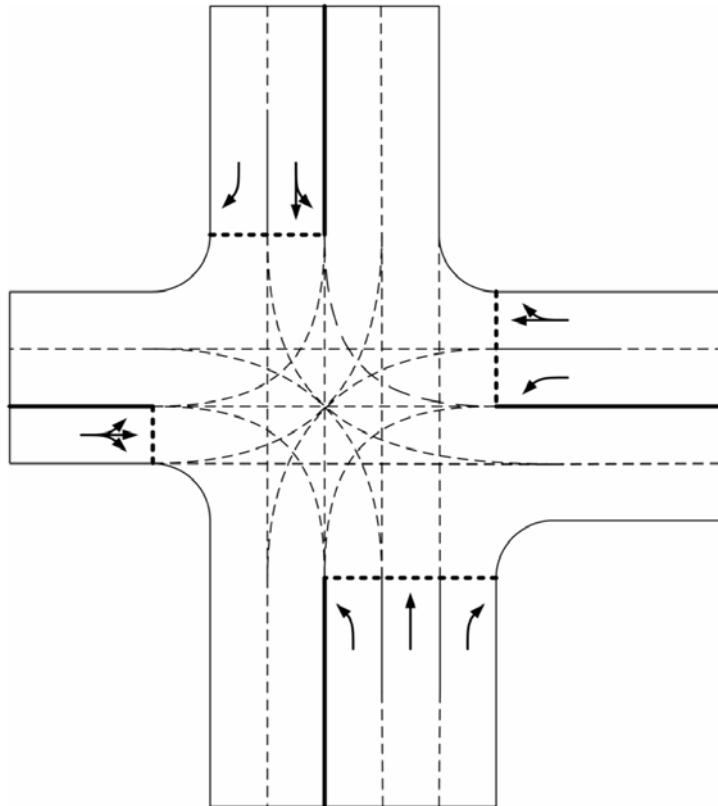
## Attractiveness of Sinks

Mathematically, sinks tend to attract their vehicles similar to electric charges in a wire





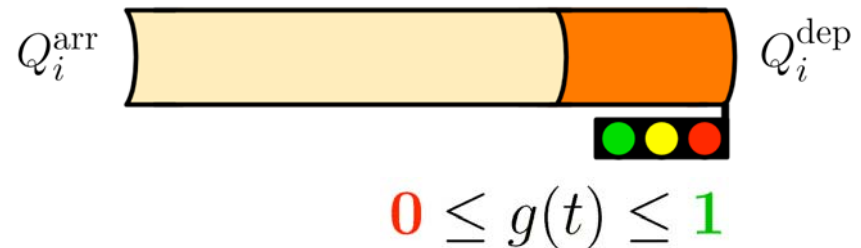
# Network Representation of Intersections



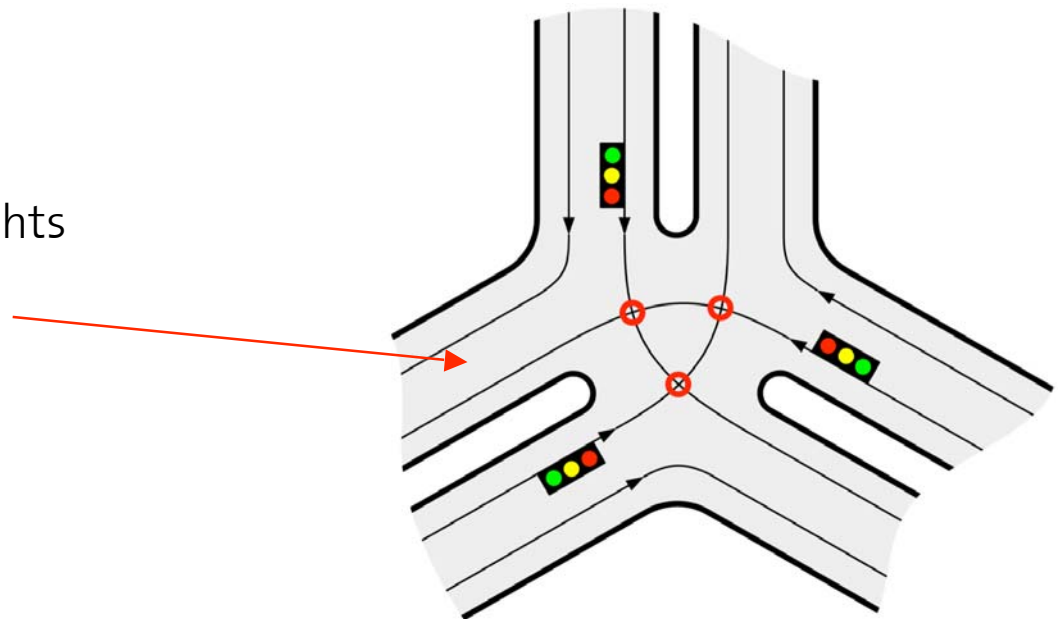
## Intersections: Modelling

- Traffic light
  - Additional side condition

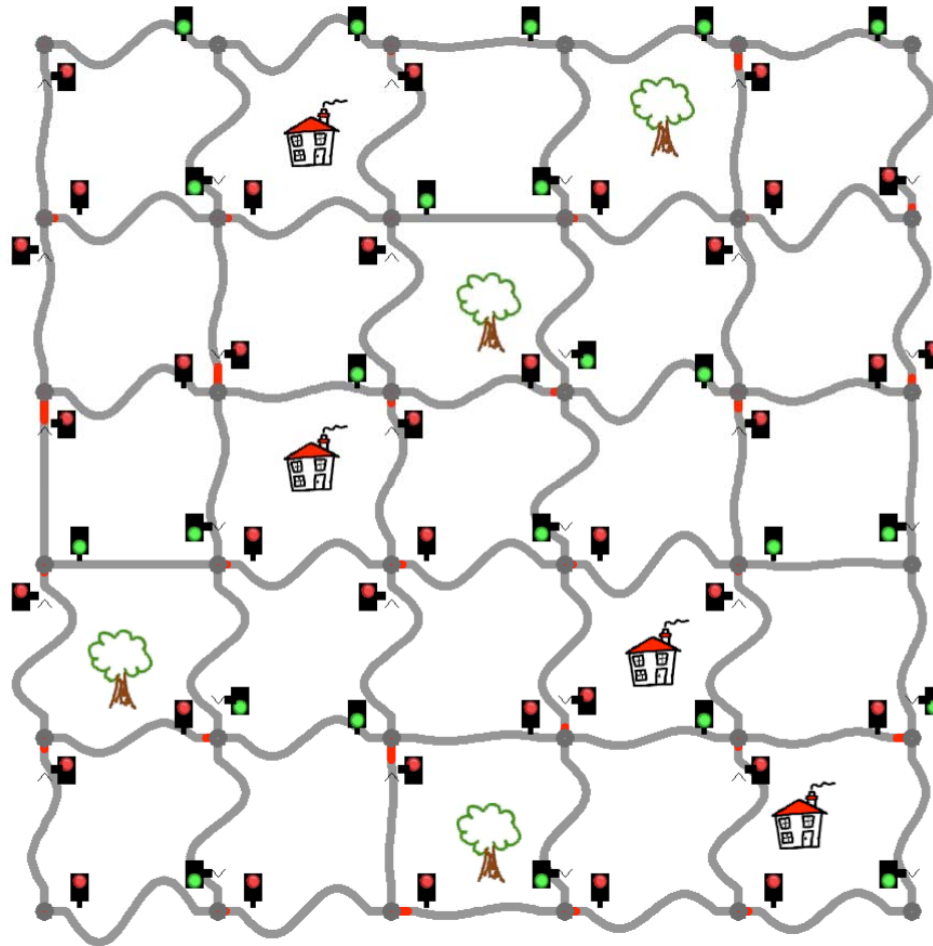
$$Q_i^{\text{dep}}(t) \leq g(t) \cdot Q_i^{\text{max}}$$



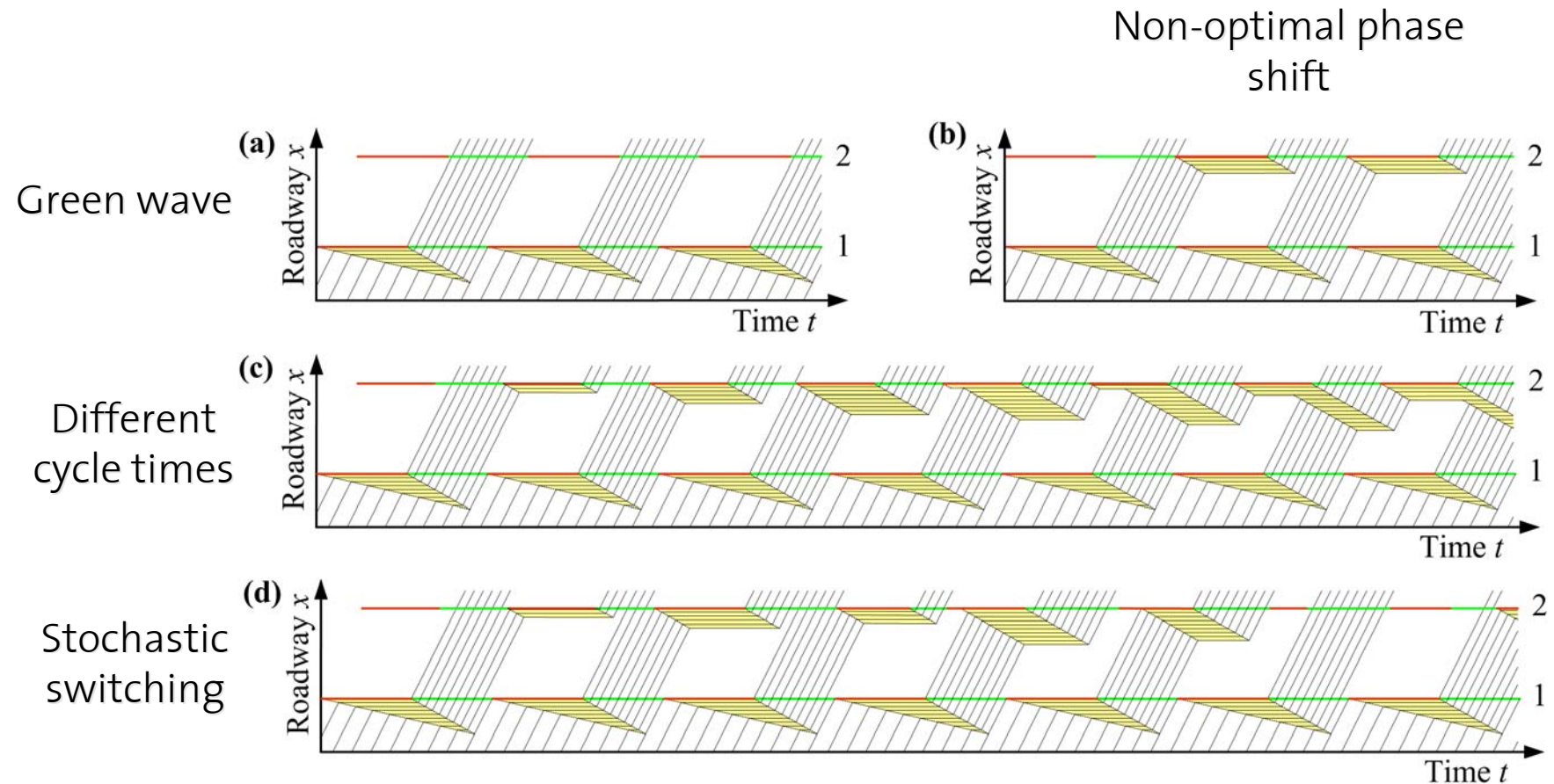
- Intersection
  - Is **only** defined by a set of mutually excluding traffic lights
  - Each intersection point gives one more side condition



# Simulation of Artificial Road Networks with Traffic Lights



# Interdependence of Subsequent Intersections



## Self-Organized Traffic Light Control

### Particular Challenges and Difficulties:

- Large variations in demand, turning rates, etc.
- Irregular networks, nodes with 5, 6, 7 links
- Switching times discourage frequent switches, reduce flexibility a lot!
- Queue front does not stay at service station (traffic light, intersection), instead propagates upstream and complicates queue dynamics
- Travel times are dependent on load/congestion level
- Delay times propagate in opposite directions
- Variety of service/turning directions is costly: reduces the fraction of green time for each direction
- Congested subsequent roads can diminish the effect of green times
- Minimum flow property reduces throughput of shared lanes
- Optimal sequence of signal phases changes, optimal solutions are aperiodic!
- Some directions may be served several times, while others are only served one time (i.e. it can make sense to split jobs!)

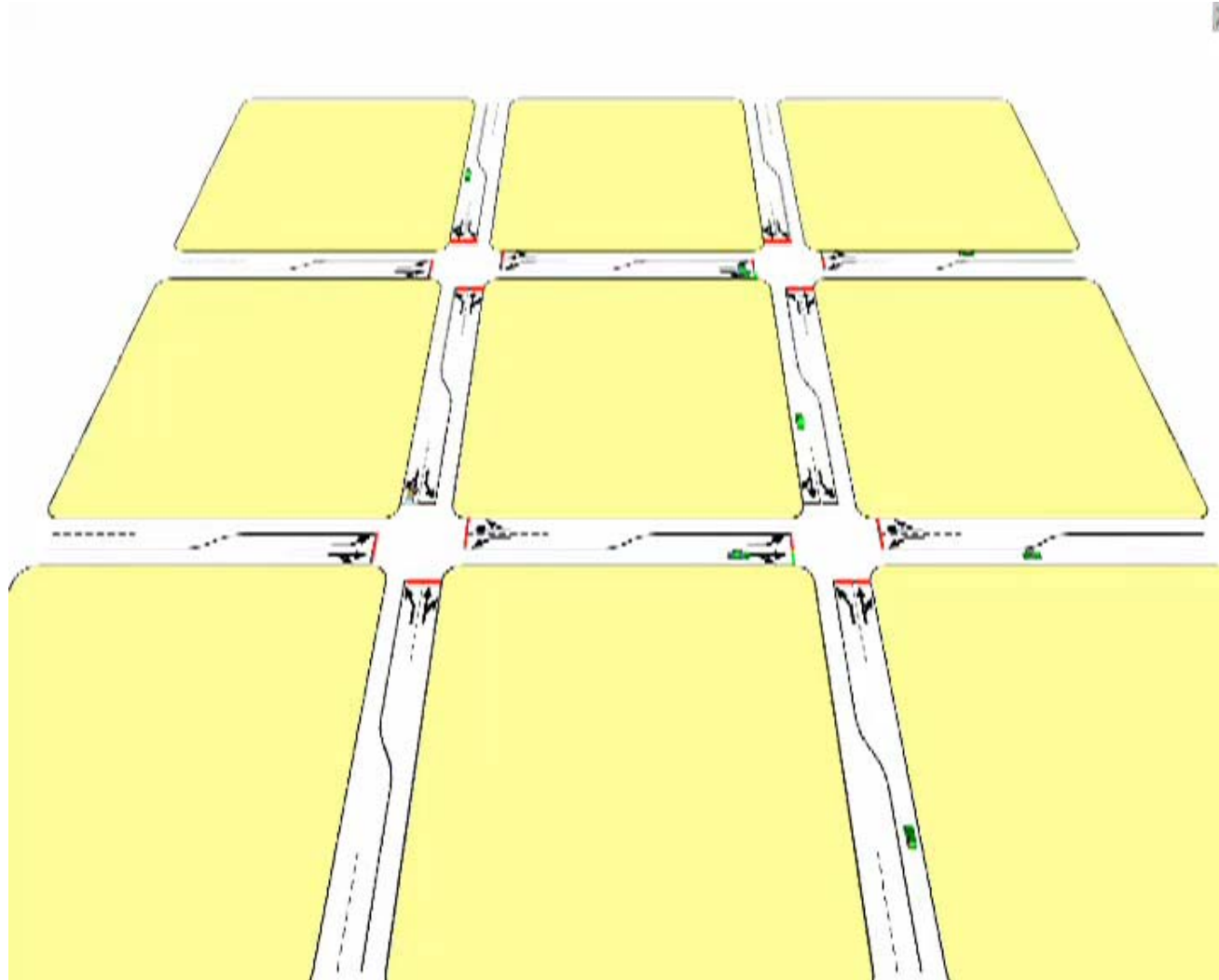
**Optimization problem is dominated by non-linearities and NP hard!**

# Operation Regimes of Traffic Light Scheduling

## I. “Gaseous” Free-Flow Low-Density Regime

- Demand considerably below capacity
- Application of the first-in-first-out/first-come-first-serve principle
- Individual cars get green lights upon arrival at intersection
- Default state is a red light!
- All turning directions can be served
- Low throughput because of small vehicle arrival rate

# Service of Single Vehicles upon Arrival



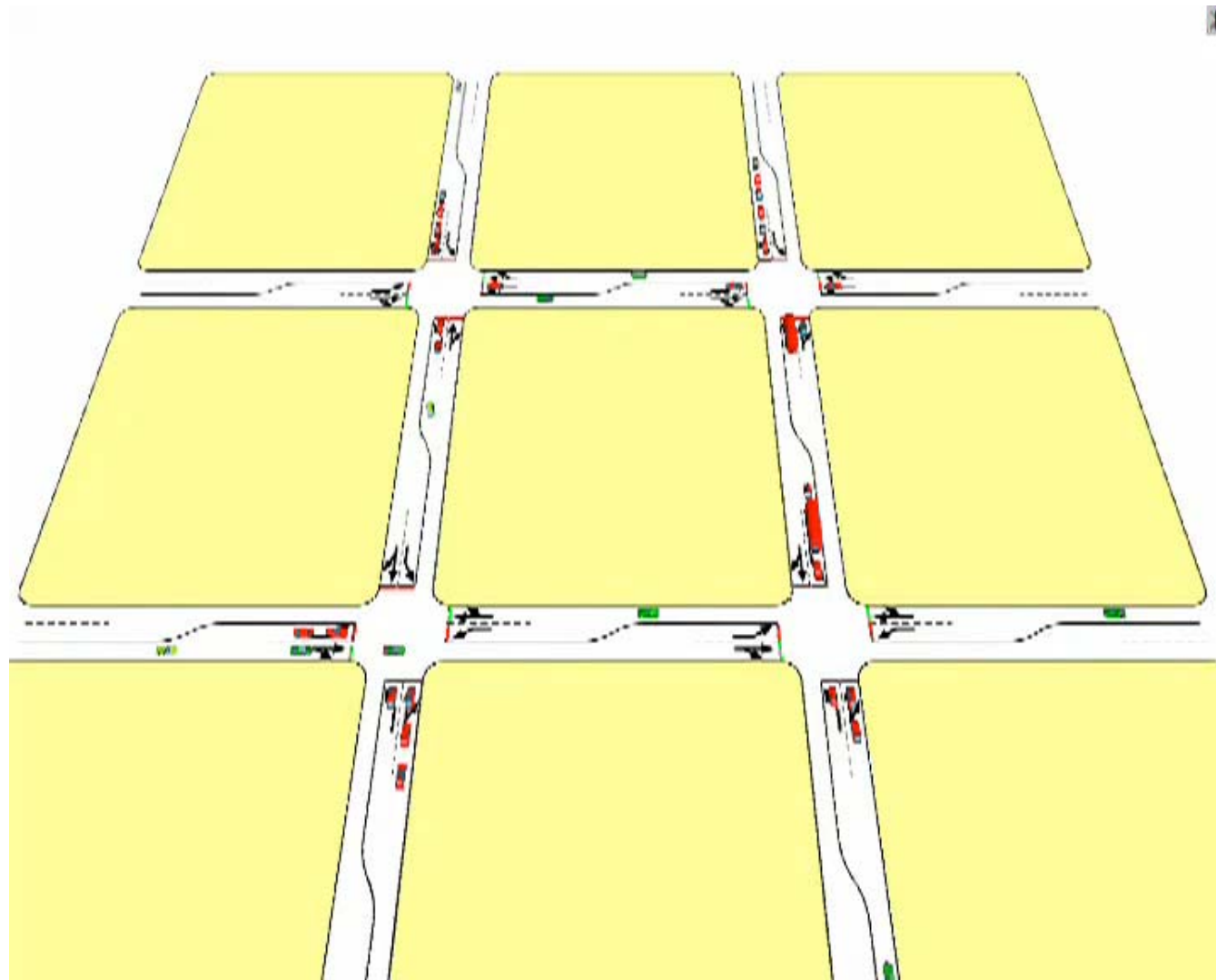
# Operation Regimes of Traffic Light Scheduling

## II. Droplet-/Platoon-Forming, Mutually Obstructed Regime

- Demand below and possibly close to capacity
- Simultaneous arrivals and, therefore, conflicts of usage likely
- Waiting times are unavoidable. Hence, vehicle platoons are forming
- The goal is to minimize waiting times
- Serving platoons rather than single vehicles increases throughput!
- Longer standing platoons are prioritized compared to shorter ones
- Moving platoons are prioritized compared to similarly long standing platoons.  
This is essential for traffic light synchronization and formation of **green waves**.



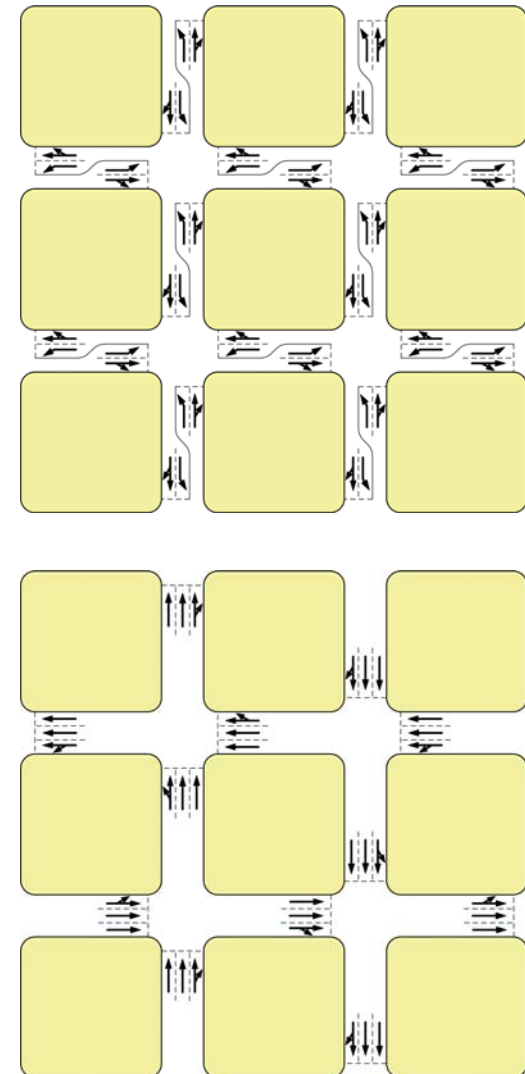
# Emergence of Green Waves



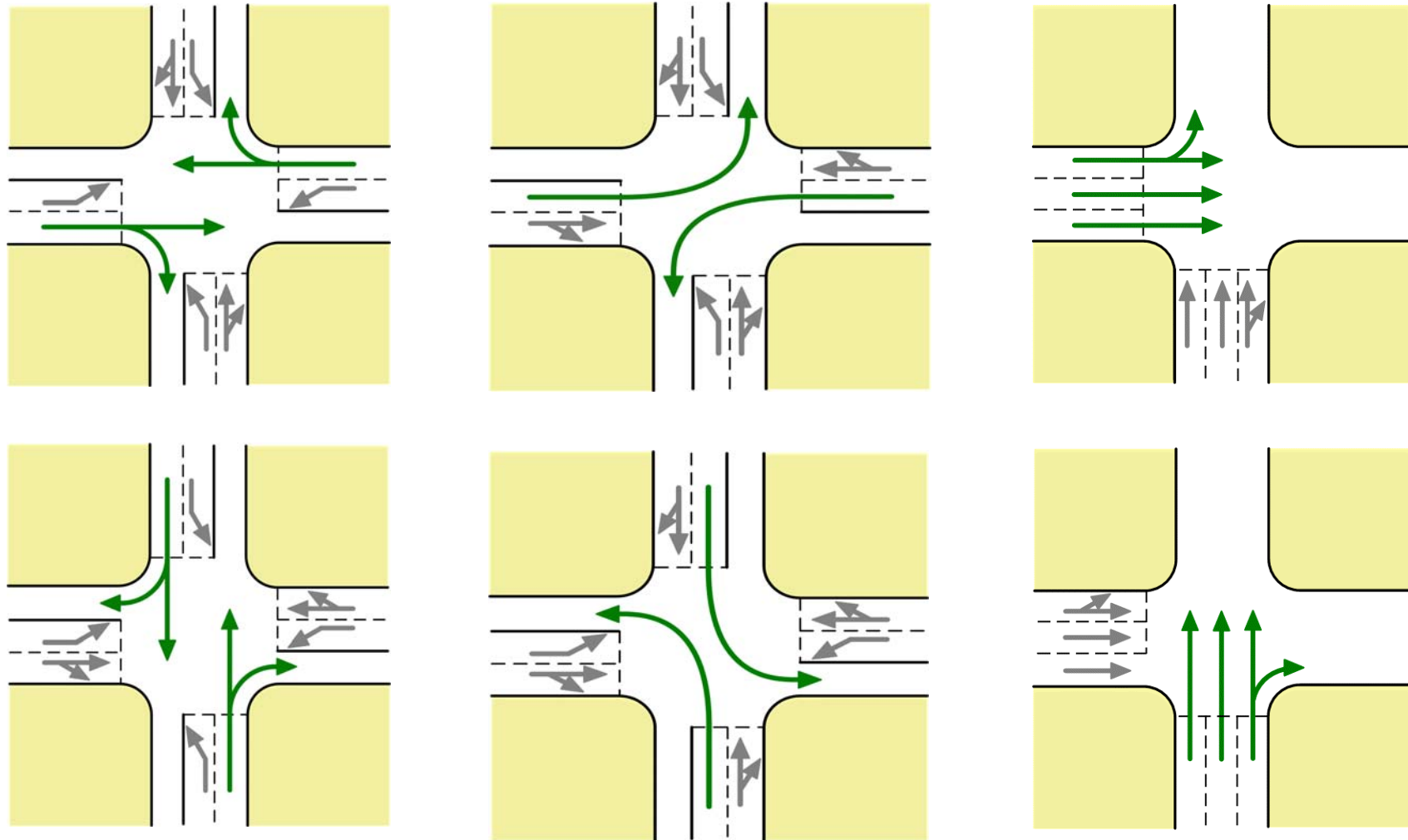
# Operation Regimes of Traffic Light Scheduling

## III. Condensed, Congested, Queue-Dominated Regime

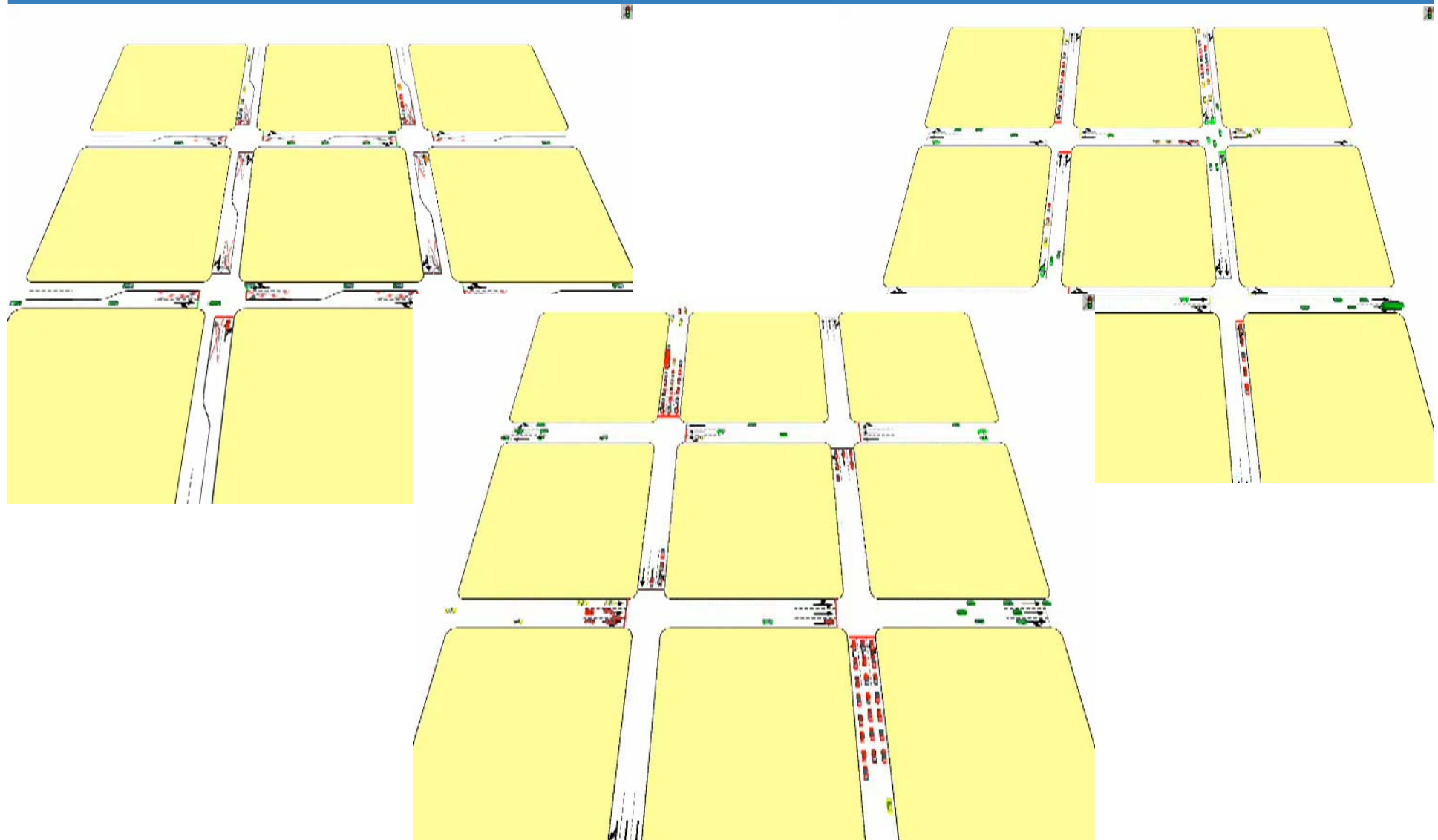
- Demand above capacity
- Goal becomes flow maximization, as queues form in all directions
- Application of flow bundling principle (similarly to platoon formation) is recommended: Reduction of service/turning directions, i.e. of heterogeneity, increases capacity

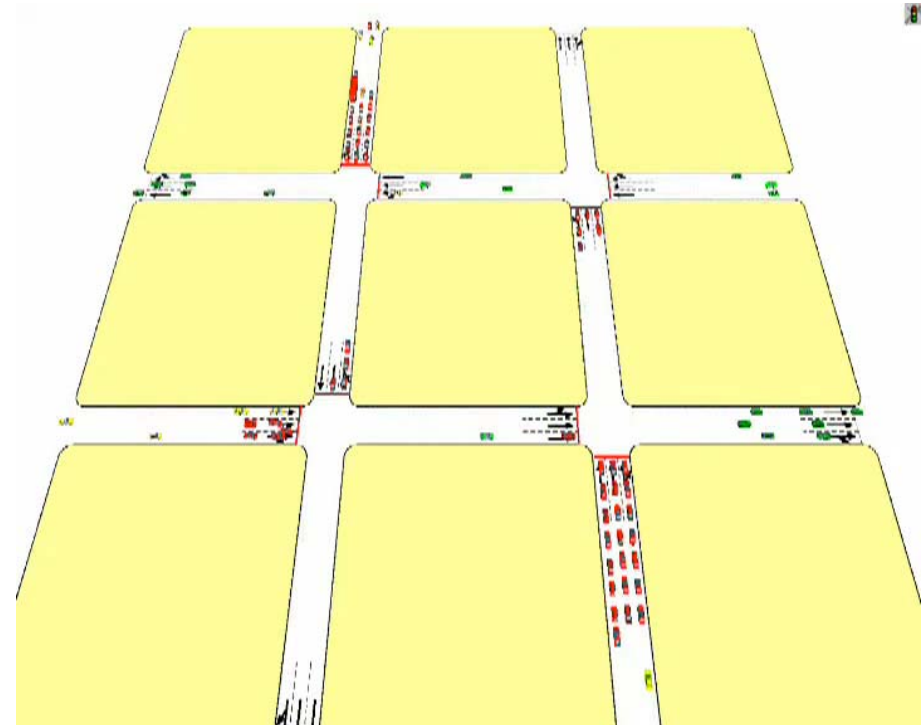
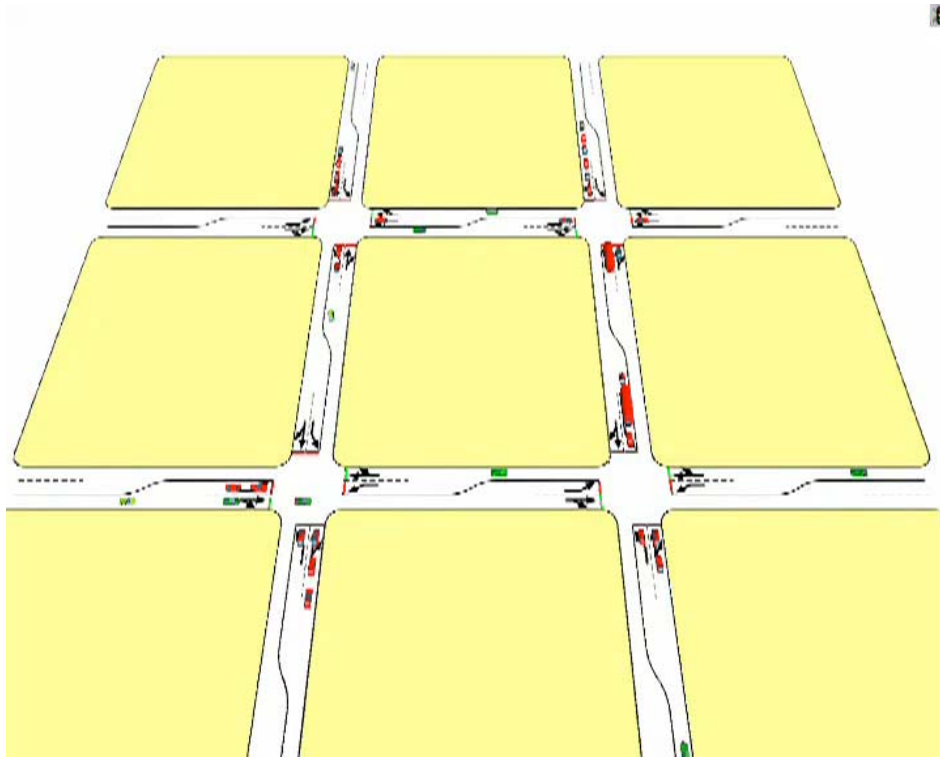


## Reduction of Traffic Phases Means Increase of Capacity

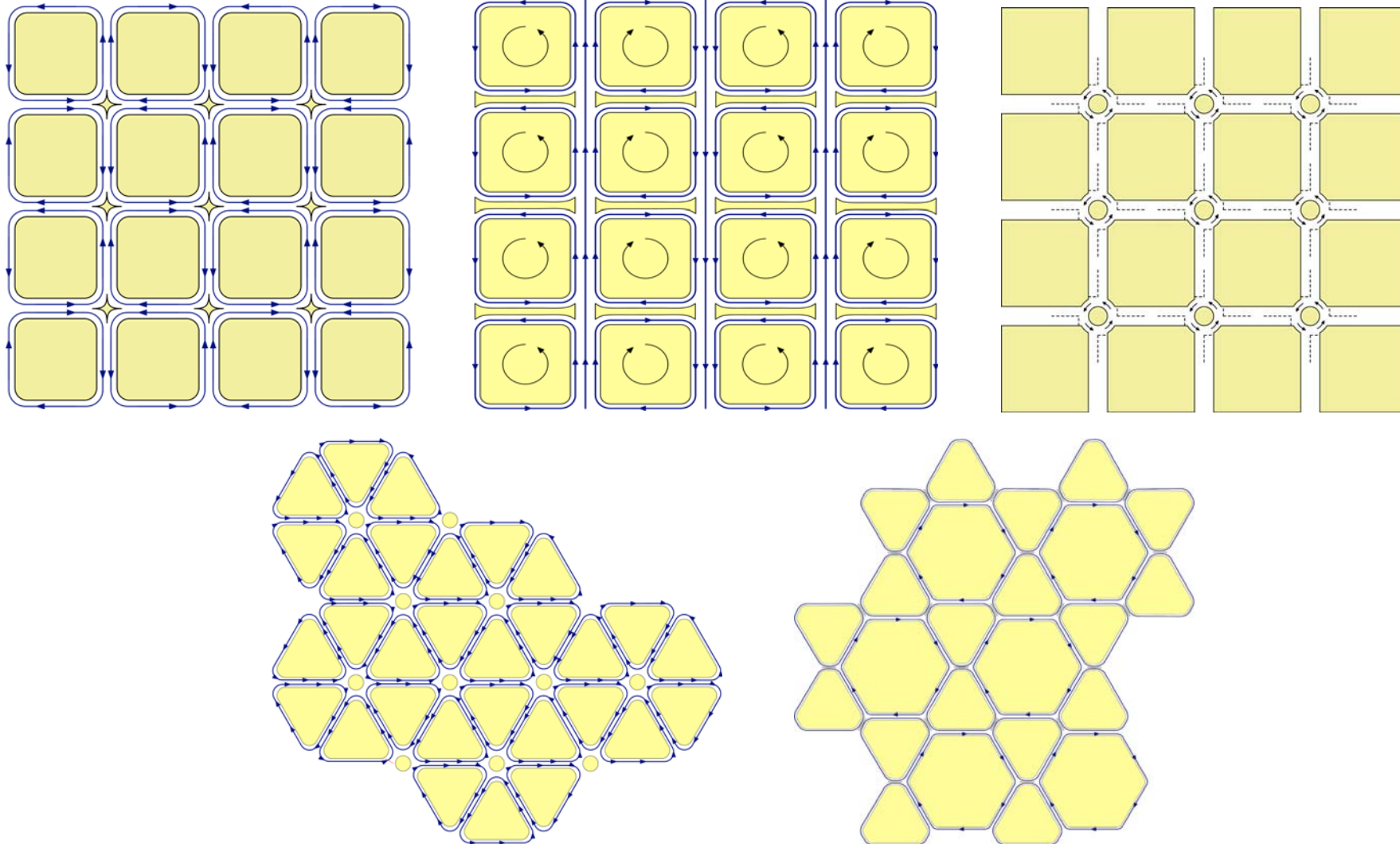


# Reorganizing the Traffic Network





# Intersection-Free Designs



# Self-Organized Traffic Flow at Unsignalized Intersections



## Operation Regimes of Traffic Light Scheduling

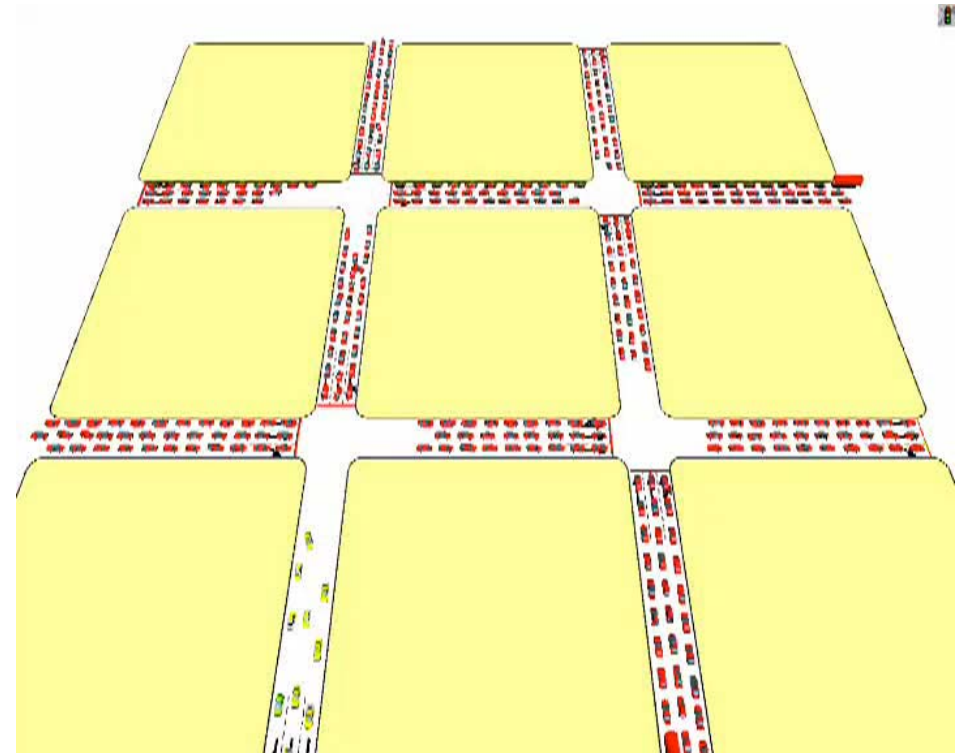
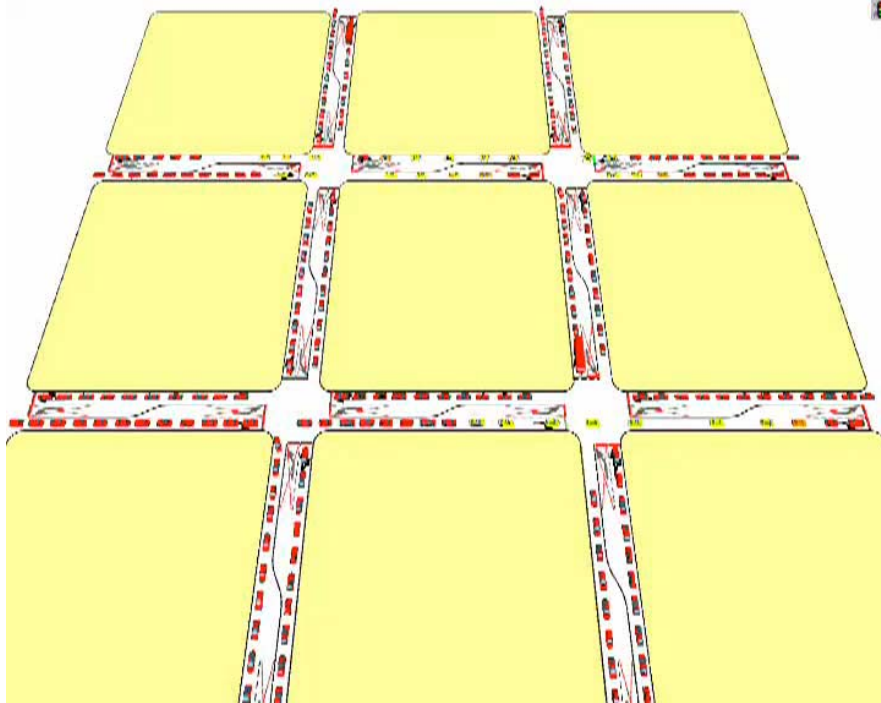
### IV. Bubble Flow, Heavily Congested Gap Propagation Regime

- Demand considerably above capacity
- Almost all streets are more or less fully congested
- Gap propagation principle replaces vehicle propagation
- Goal is to avoid stopping of gap (“bubble propagation”)
- Larger and moving gaps are given priority

*Best in terms of throughput is an approximately half-filled system. The load/occupancy corresponding to the maximum throughput should not be exceeded. The use of access control with traffic lights is, therefore, recommended. This defines a kind of CONWIP strategy for traffic.*



# Gap Propagation Regime



## Self-Organized Traffic Light Control

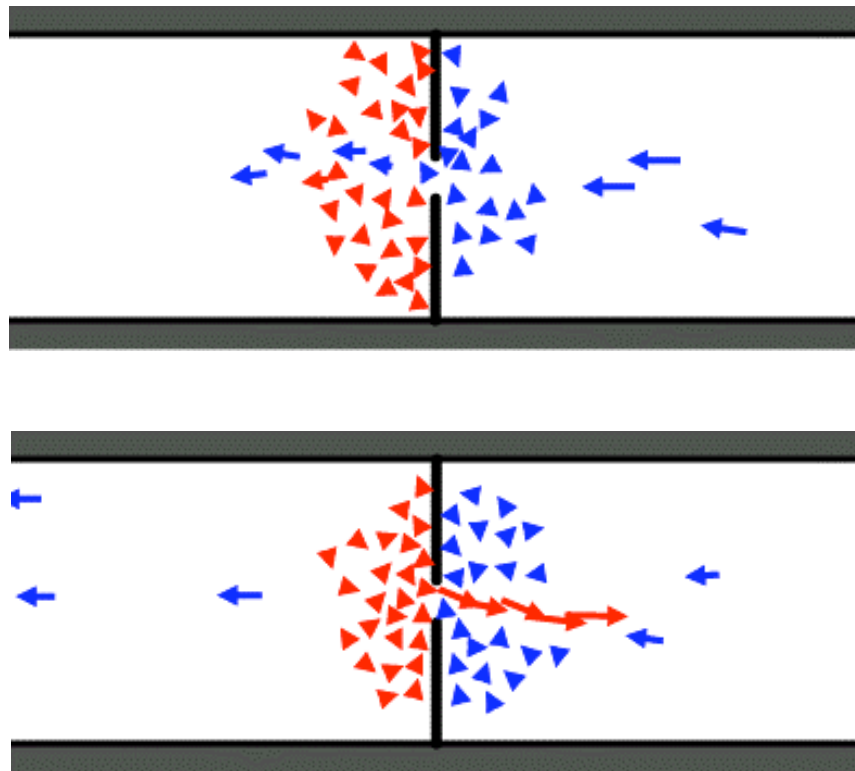
### Objectives:

- Search for a self-organization principle that flexibly switches between the different operation regimes.
- In addition, it should optimize operation within each operation mode.
- Green waves should emerge as a result of coordination/ synchronization among neighboring traffic lights
- Goal function needs to take into account both travel times and throughputs

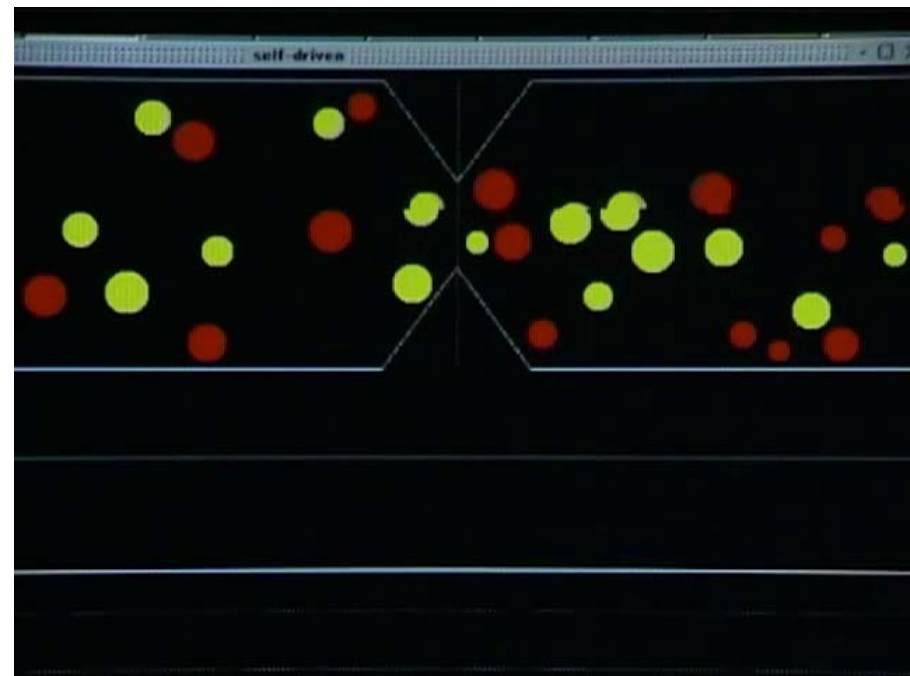
### Expected Advantages:

- More flexible adaptation to the local, varying traffic situation
- Improved traffic light scheduling during situations such as accidents, building sites, failures of traffic lights, mass events, evacuation scenarios, etc.
- Increased robustness with respect to fluctuations and failures by decentralized control concept and collective intelligence approach

# Self-Organized Oscillations at Bottlenecks and Synchronization

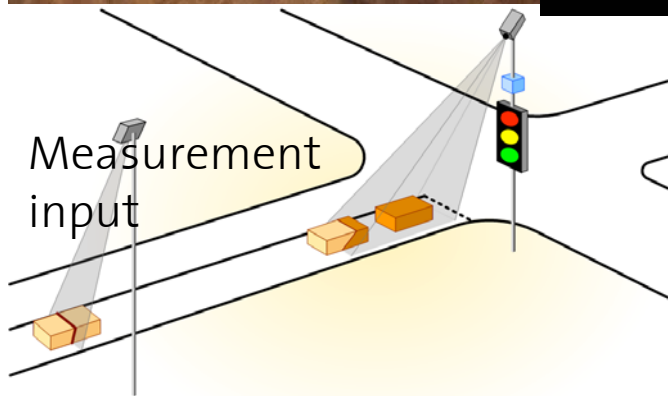
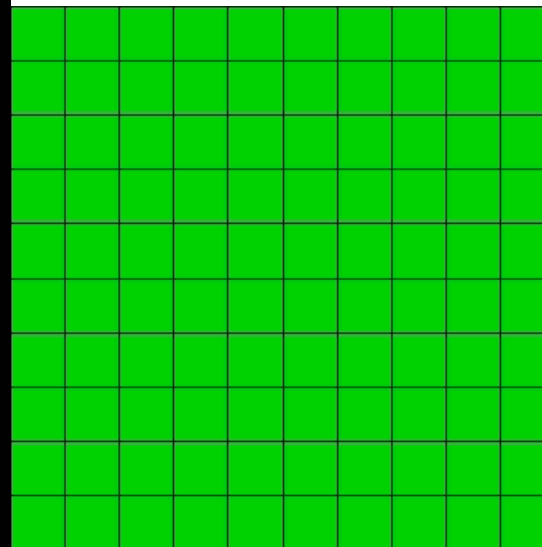
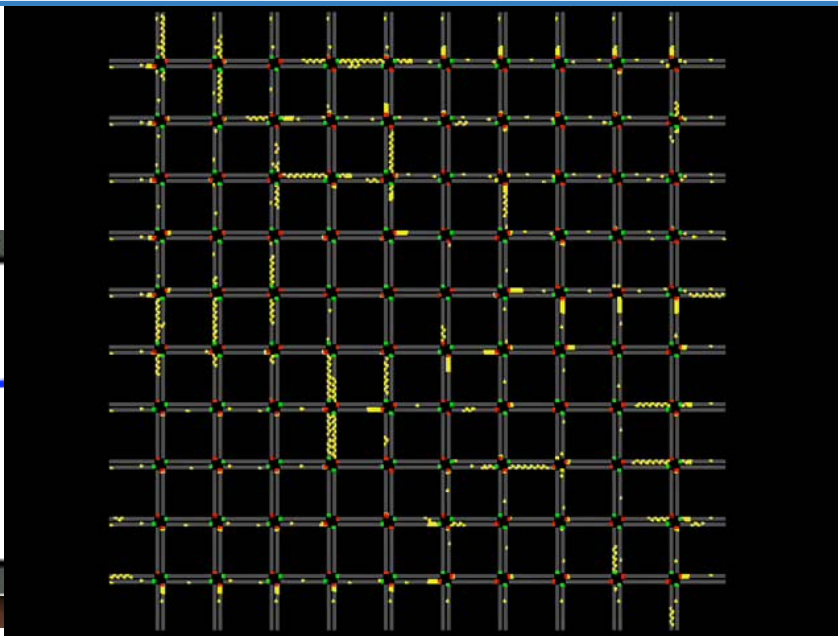
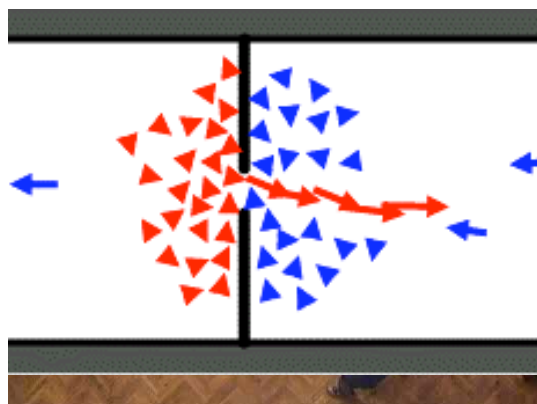


- **Pressure-oriented**, autonomous, distributed signal control:
  - Major serving direction alternates, as in pedestrian flows at intersections
  - Irregular oscillations, but ‘synchronized’
- In huge street networks:
  - ‘Synchronization’ of traffic lights due to vehicle streams spreads over large areas

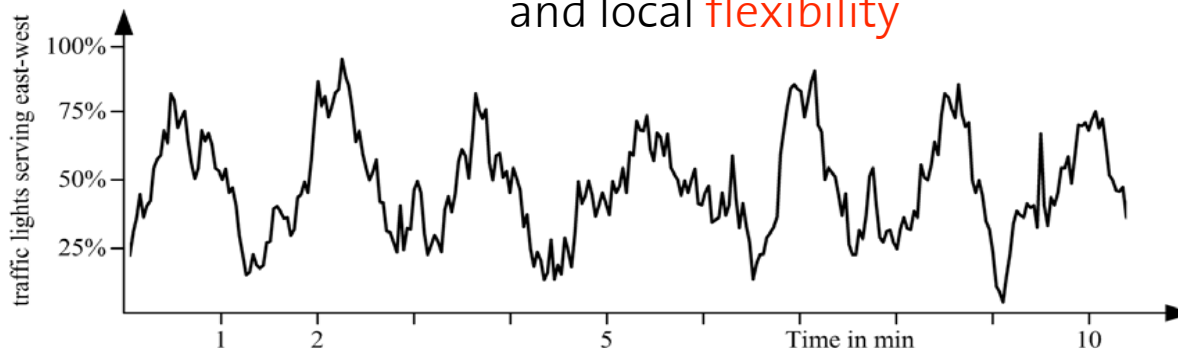


# Decentralized Concept of Self-Organized Traffic Light Control

Inspiration: Self-organized oscillations at bottlenecks



Published in *JSTAT* (2008)



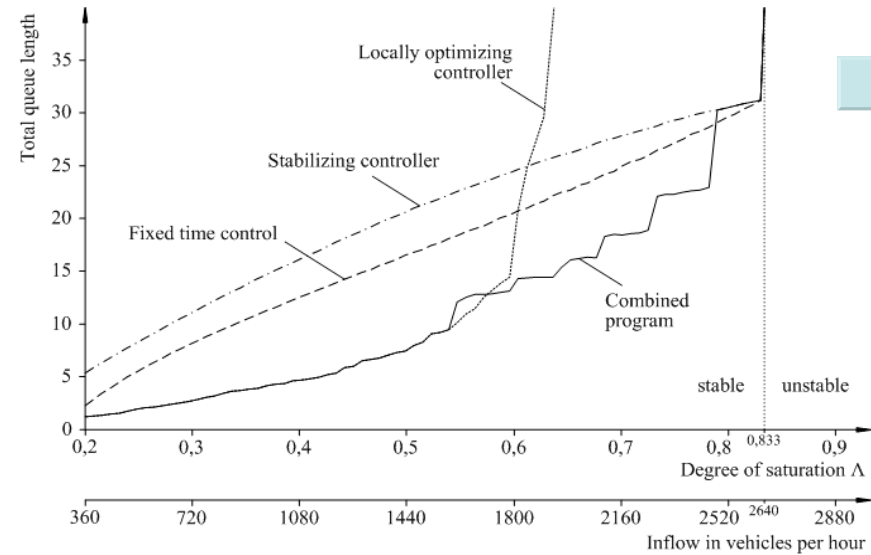
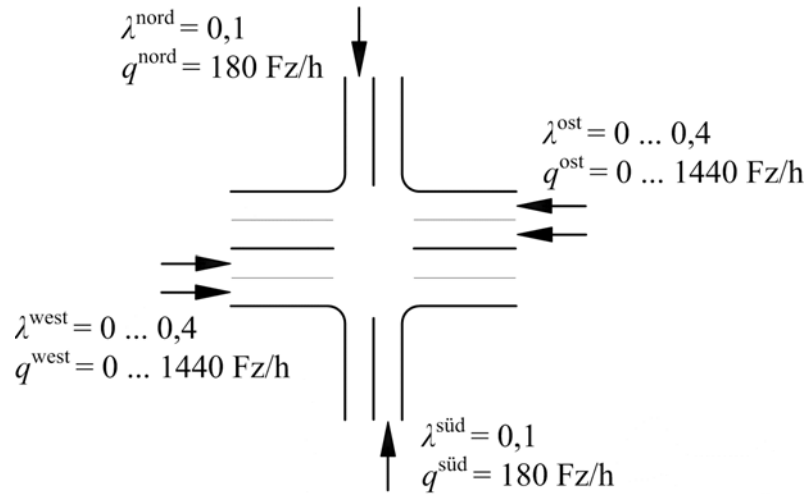
Optimal compromise between **coordination** and local **flexibility**

## Properties of the Self-Organized Traffic Light Control

- Self-organized red- and green-phases
  - No precalculated or predetermined signal plans
  - No fixed cycle time
  - No given order of green phases
- Green phases depend on respective traffic situation on the previous *and* the subsequent road sections
  - Determined by actual queue length and delay times
  - Default state is red light
  - At light traffic conditions, single vehicles trigger green light
- Distributed, local control
  - Greater flexibility and robustness
  - Usage of sensors (optical, infrared, laser, ...)
  - No traffic control centre needed
- Pedestrians are handled as additional traffic streams
- Public transport may be treated as vehicles with a higher weight

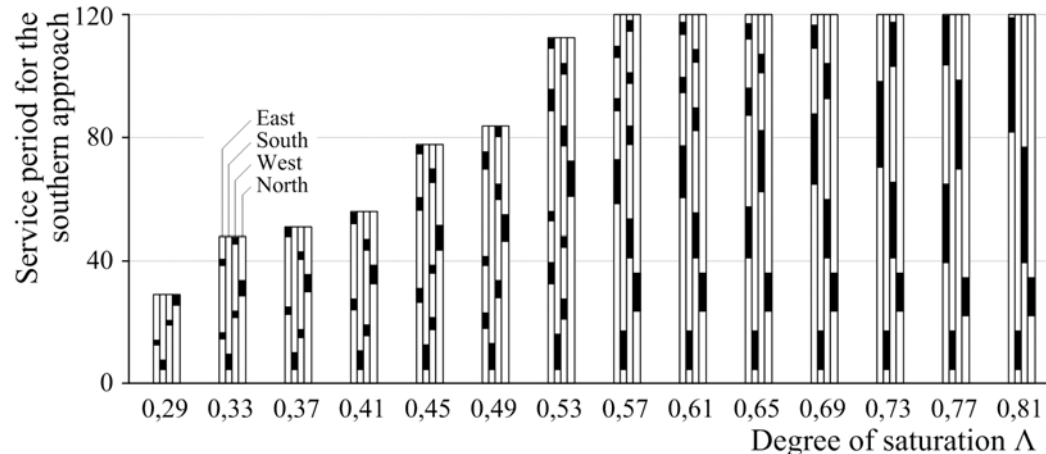
# Simulation Study: Isolated Intersection (1)

With constant arrival rates:



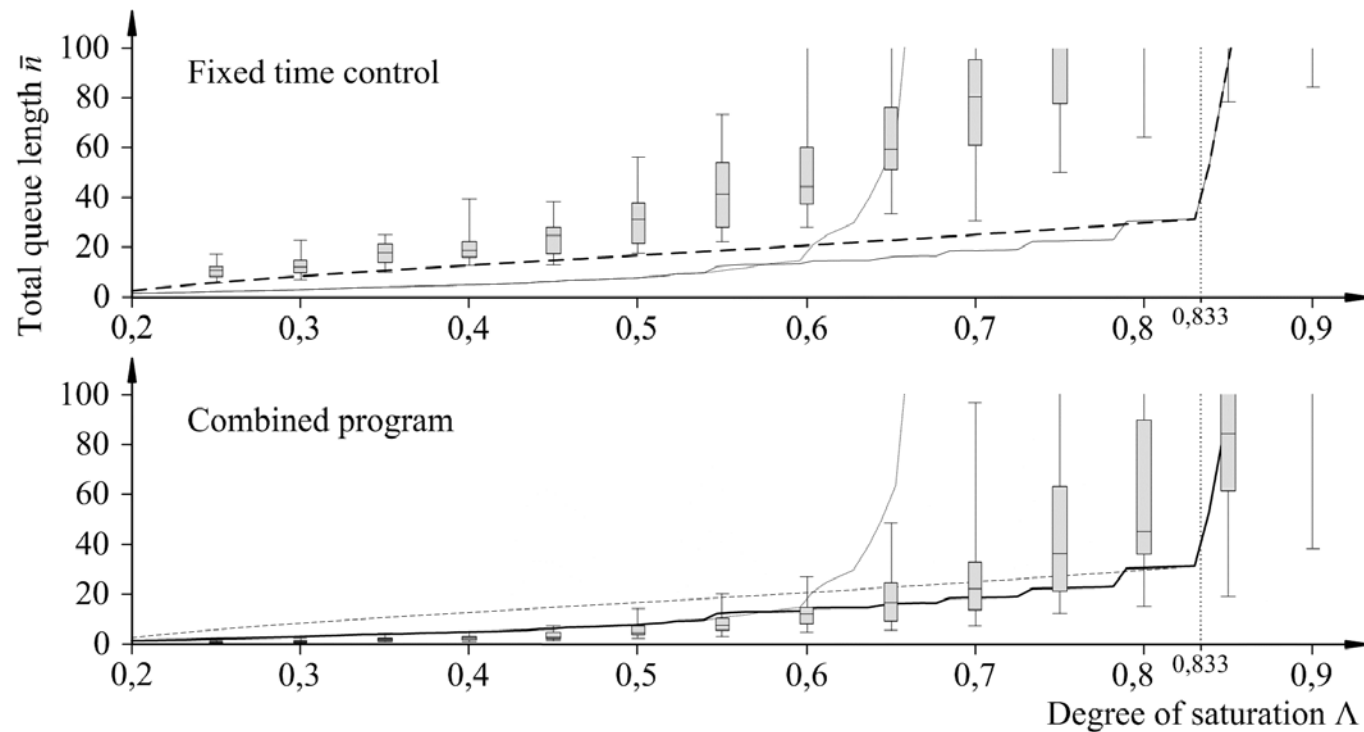
The switching sequence adapts to the arrival patterns.

We observe a **flexible switching** regime with **maximum red-times**.



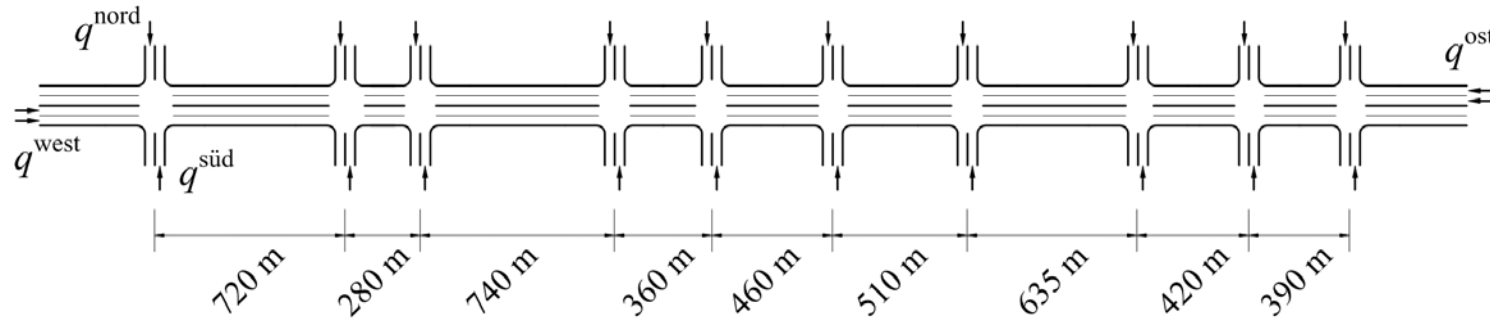
## Simulation Study: Isolated Intersection (2)

With stochastic arrivals:

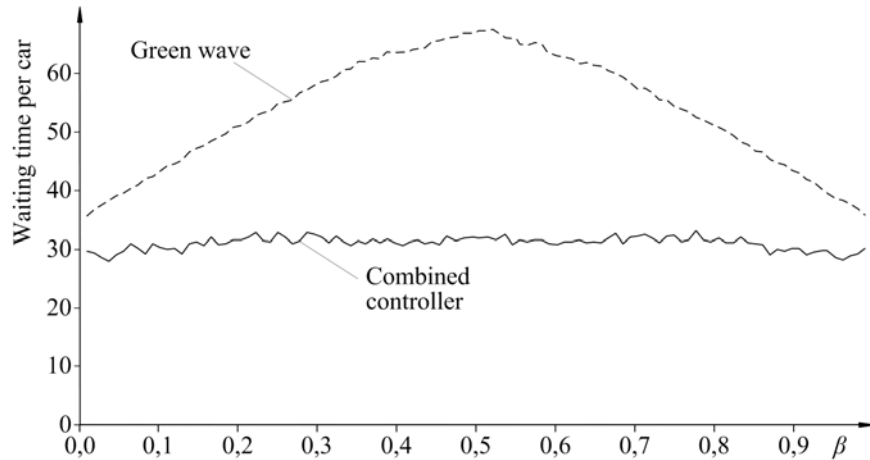


Due to the flexibility, we observe a reduction in both, the total **waiting time** and its **variance**.

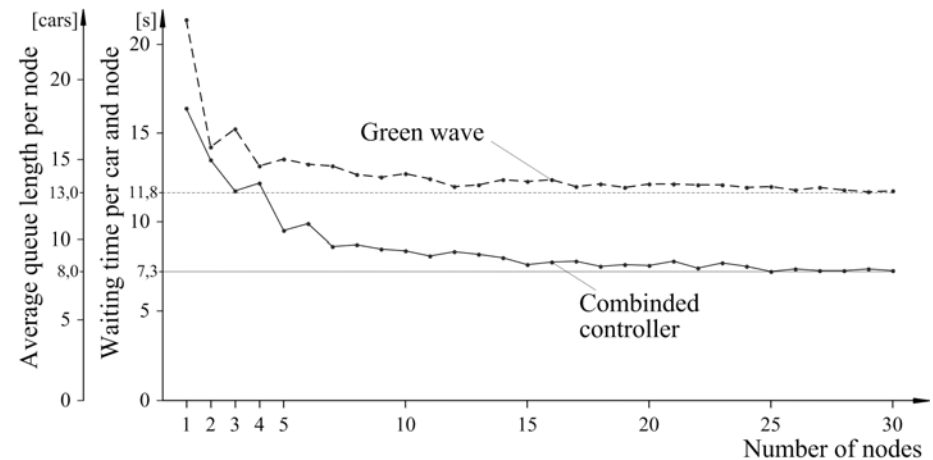
# Simulation Study: Coordination along an Arterial (1)



Varying the direction of the main flow

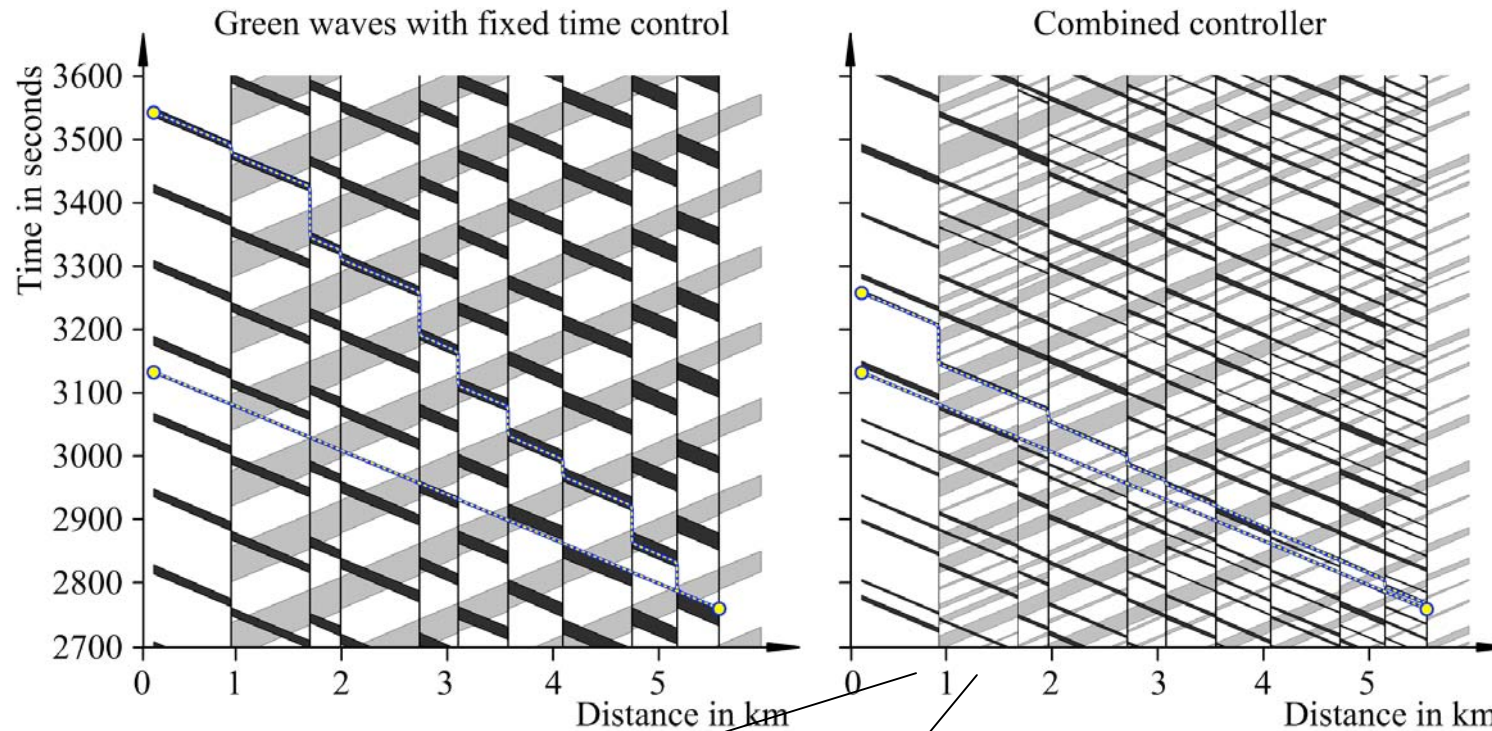


Varying the number of nodes along the arterial





## Simulation Study: Coordination along an Arterial (2)



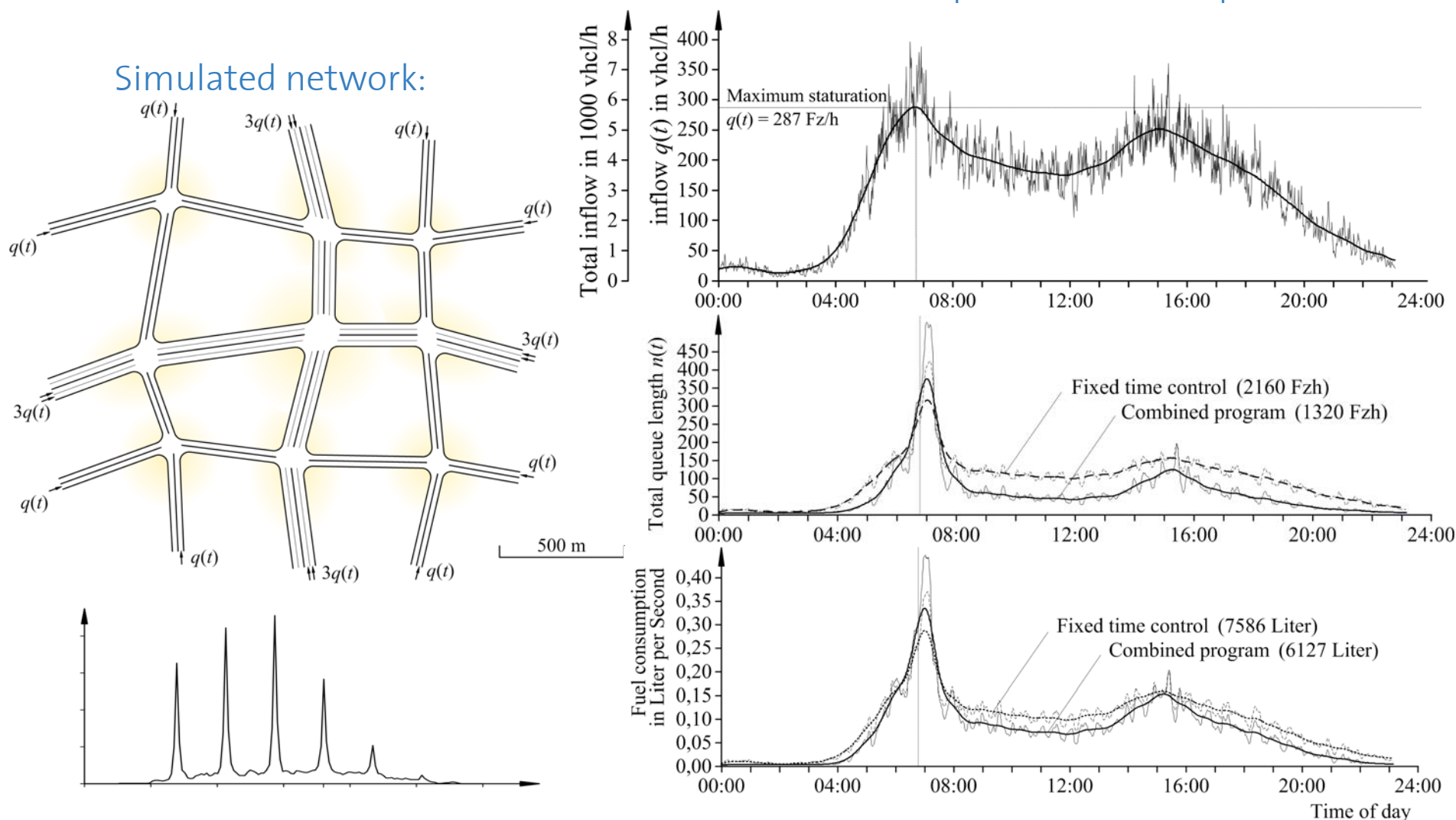
Irregular switching patterns are equalizing irregular traffic patterns, and thereby minimizing waiting times.

Principles:

1. Platoon formation
2. Flexible scheduling of platoons
3. Minor streams are served during time gaps.

# Coordination in a Network

Traffic demand is specified with empirical data:



# Application Example: City Center of Dresden

Simulation “Pirnaischer Platz”



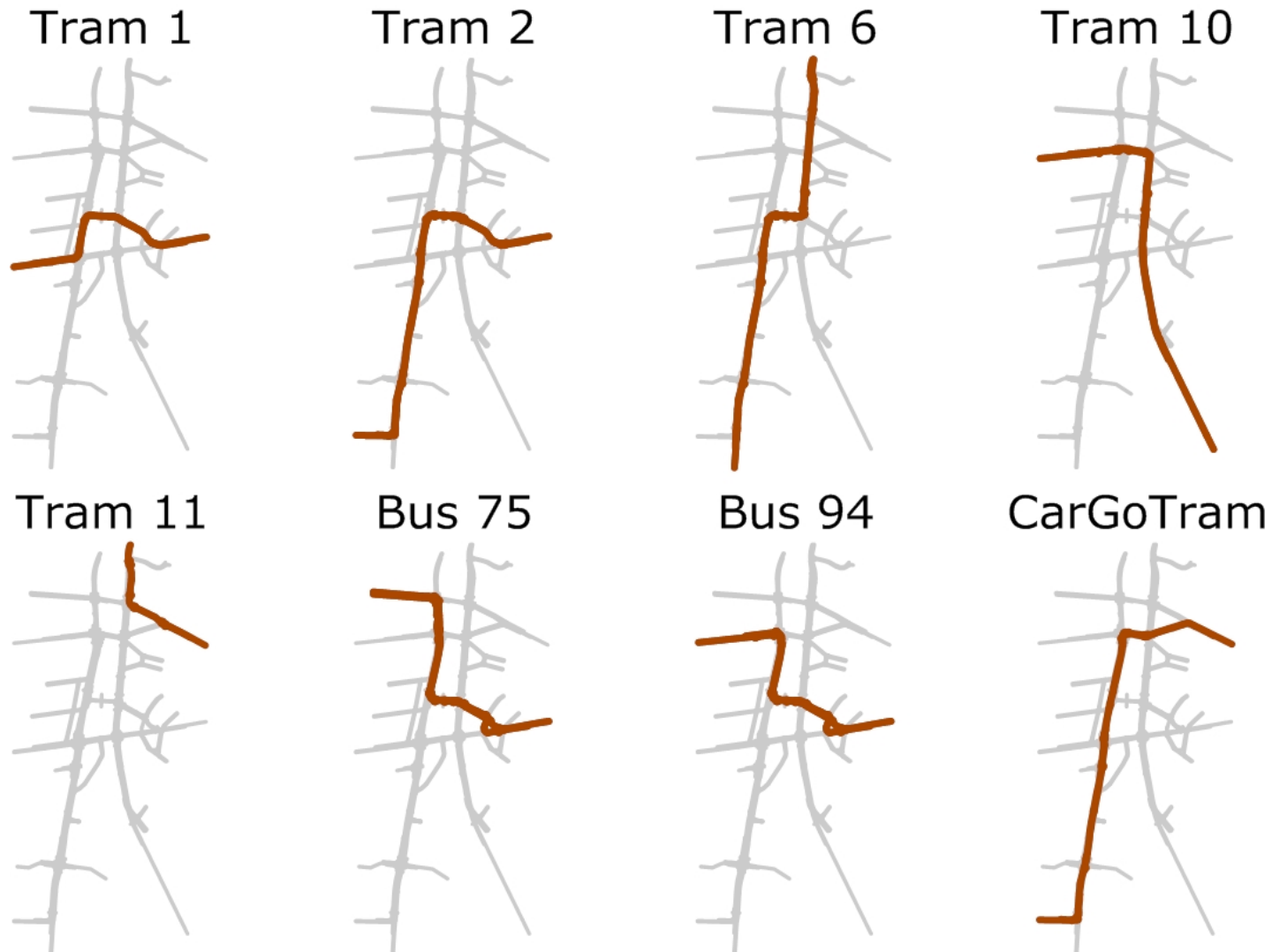
# Towards Self-Organized Traffic Light Control in Dresden



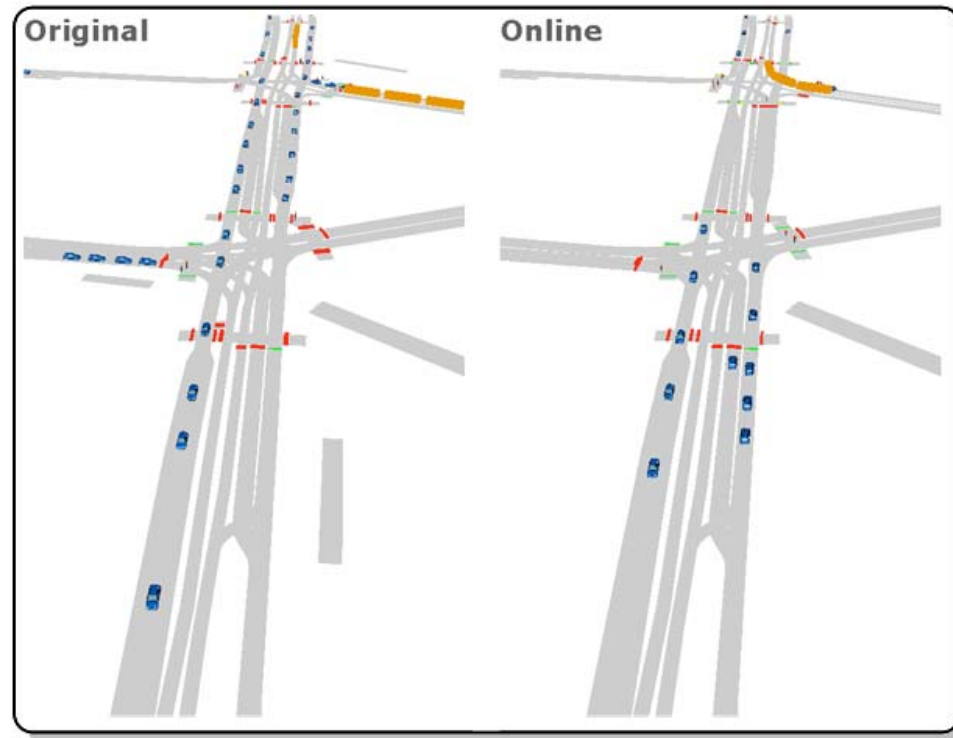
# The Measurement and Control Area



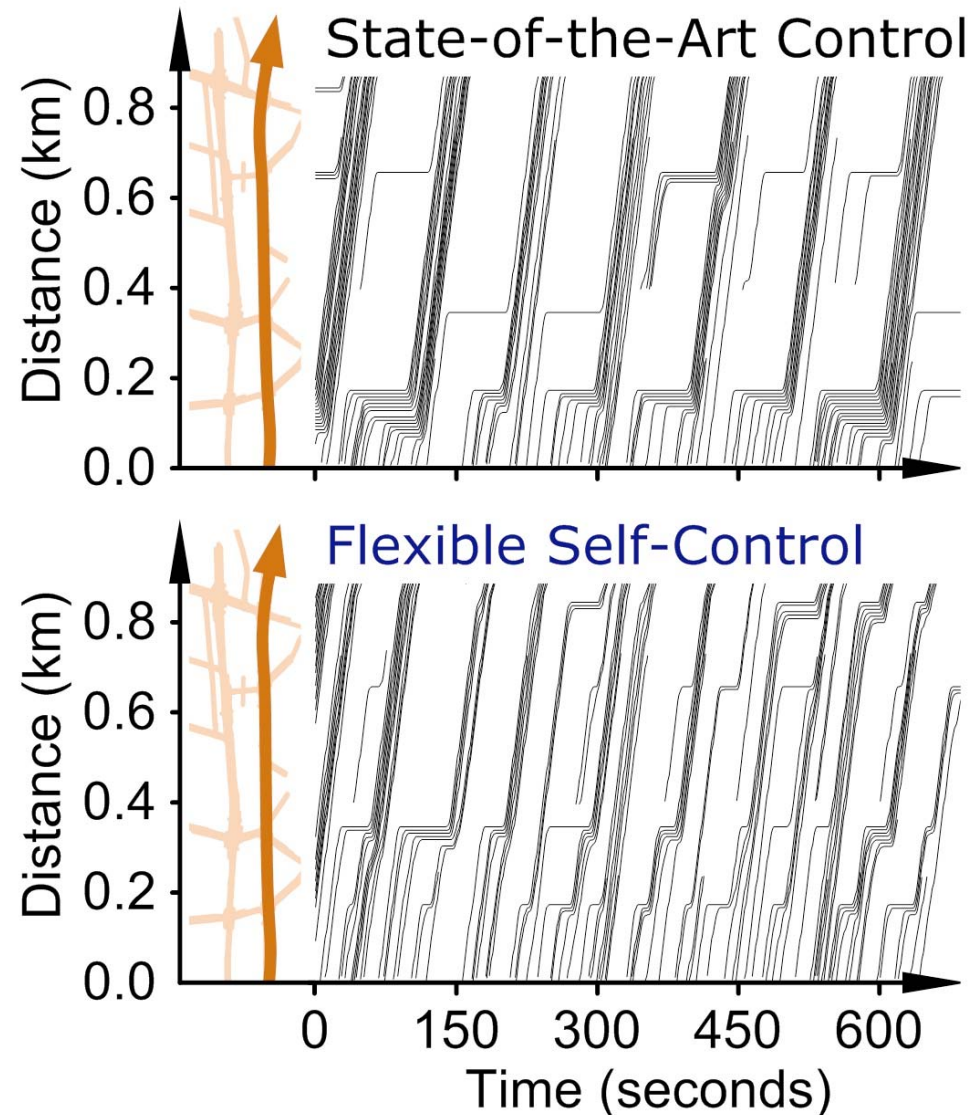
## Disturbance of Traffic Coordination by Bus and Tram Lines



# Comparison of Current and Self-Organized Traffic Light Control

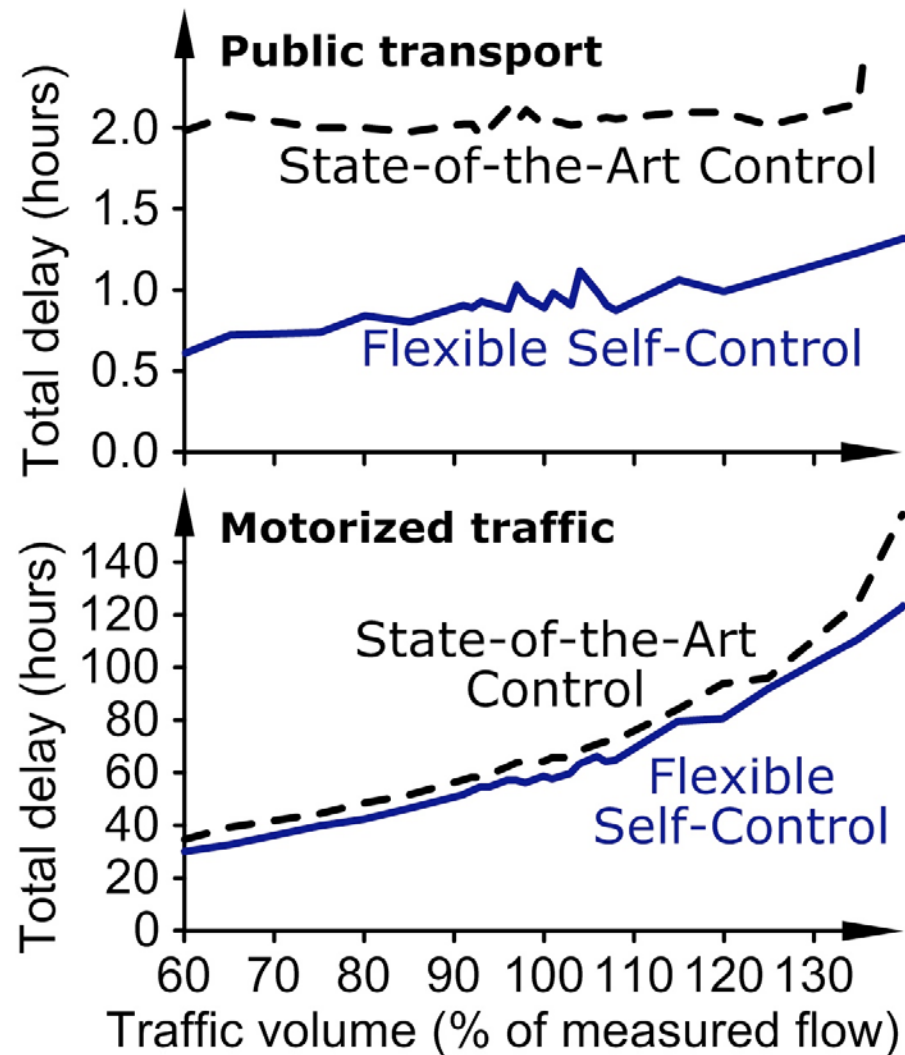


# Synchronize Traffic by Green Waves or Use Gaps as Opportunities?

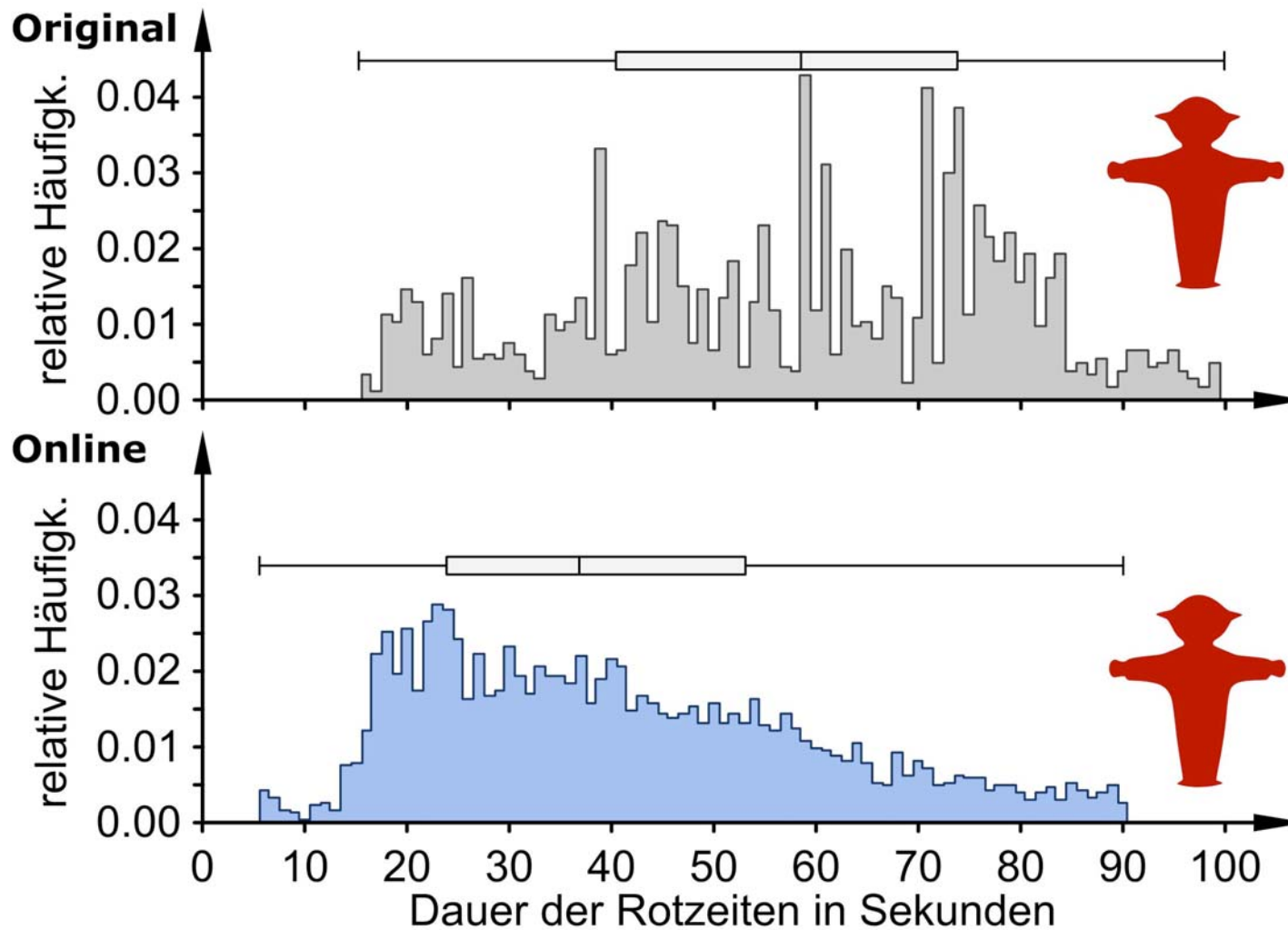




## Performance in Dependence of the Traffic Volume



## Red Time Distribution for Pedestrians



## Gain in Performance



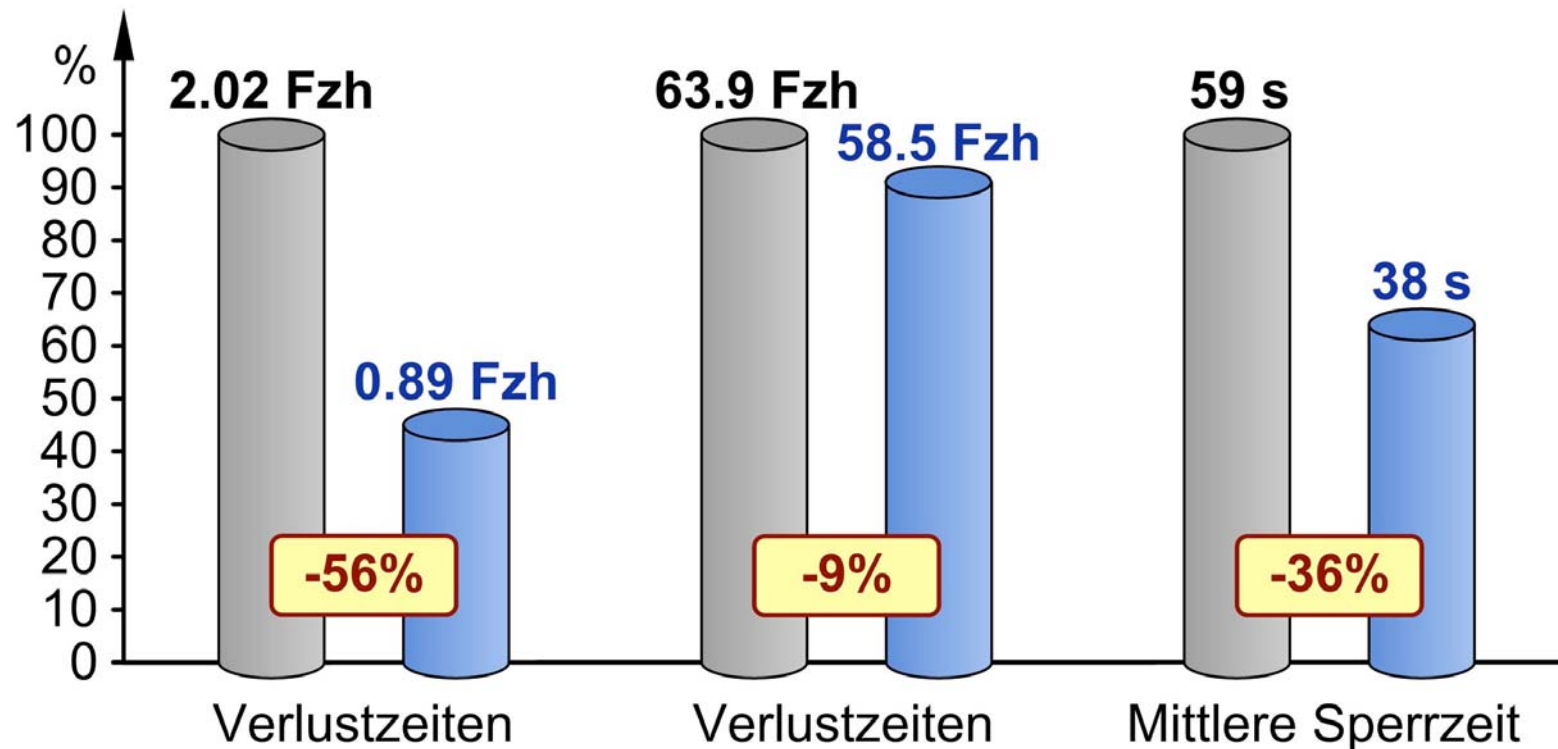
**Öffentlicher  
Personenverkehr**



**Kraft-  
fahrzeuge**

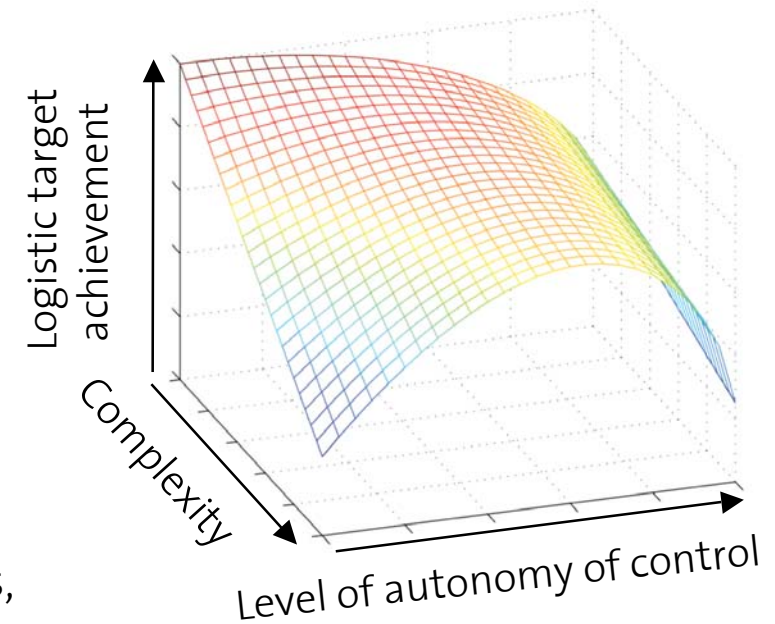


**Fußgänger  
und Radfahrer**



## Centralized Control and Its Limits

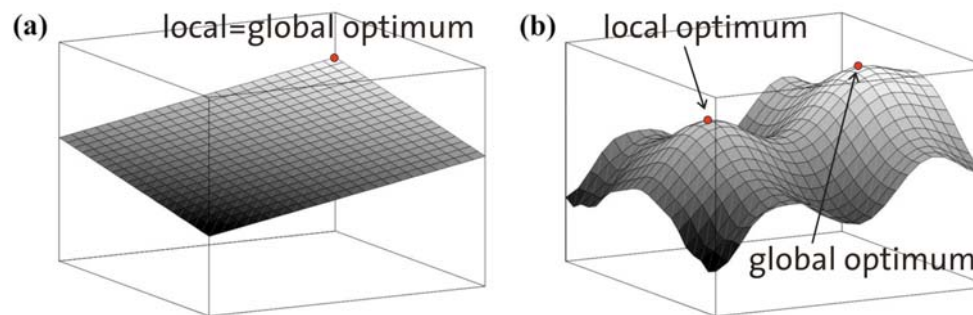
- Advantage of centralized control is large-scale coordination
- Disadvantages are due to
  - vulnerability of the network
  - information overload
  - wrong selection of control parameters
  - delays in adaptive feedback control
- Decentralized control can perform better in complex systems with heterogeneous elements, large degree of fluctuations, and short-term predictability, because of greater flexibility to local conditions and greater robustness to perturbations



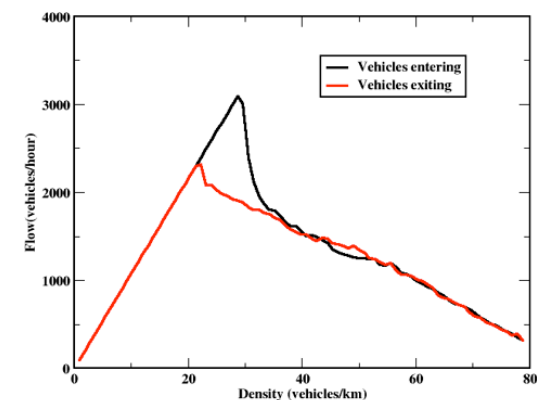
(Windt, Böse, Philipp, 2006)

## Discussion: Weaknesses of Classical Optimization

- Optimization routine may get stuck in a **local optimum**
- One can only optimize for one goal at a time, but usually, one needs to meet several objectives. **Usually, there is one optimal solution, but heterogeneity may be important for system performance.**

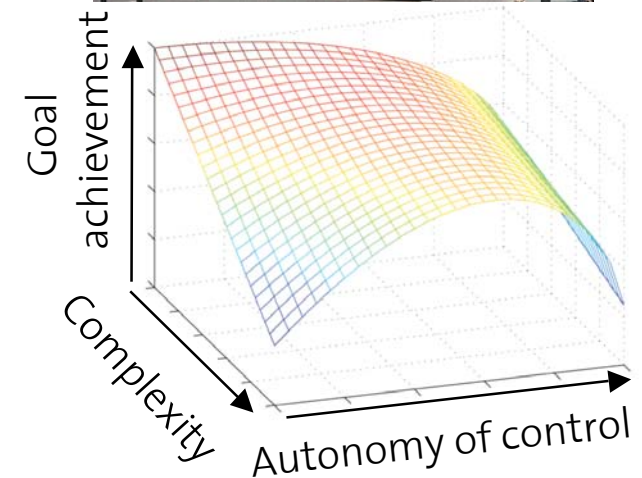


- **Evolutionary dead ends:** The best solution may be the combination of two bad solutions (i.e. gradual optimization may not work)
- **Optimization may destabilize the system**
- **Example:** Utilization of maximum road capacity will eventually cause **capacity drops**



## Weaknesses of Classical Optimization II

- **NP-hardness:** Complexity of optimization problem often prevents exact online optimization
- Optimization based on average or past data optimizes for a non-existent situation, i.e. it the applied solution is NOT optimal in reality
- **Example:** Today's traffic light control
- Often, there is a lack of data to determine model parameters accurately
- **Example:** Portefolio optimization
- I. Kondor: „The complexity of financial systems exceeds what is knowable“
- Other problems: Information delays or overloads, and inconsistent information
- **Problem:** What ARE the relevant indicators or control variables?



(Windt, Böse, Philipp, 2006)

**ETH**

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Swiss Federal Institute of Technology Zurich

Thank you for your interest!  
Any Questions?

